# Mansoura Engineering Journal

Volume 8 | Issue 1

Article 1

6-1-1983

# Behaviour of Buildings Supported on Soils with Non-Linear Properties.

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# **Recommended Citation**

Abu El-Magd, Sherief (1983) "Behaviour of Buildings Supported on Soils with Non-Linear Properties.," *Mansoura Engineering Journal*: Vol. 8 : Iss. 1, Article 1. Available at: https://doi.org/10.21608/bfemu.2021.180153

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#### BEHAVIOUR OF BUILDINGS SUPPORTED ON SOILS

#### WITH NON-LINEAR PROPERTIES

# By

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#### Summary:

This paper investigates the effect of neglecting the non-linear behaviour of the soil in a structure-soil interaction analysis of plane walls with openings. In most cases, the use of elastic properties for the soil was found to be con-servative. Only when the soil stiffness increases with the applied load, con-sidering the non-linear soil properties can yield higher stresses in the frame. The basis of the study is a plane-strain finite element analysis of the soil which supports a wall idealised as a frame. The wall has elastic properties whereas the soil is represented both by an elastic half-plane and by a hyper-bolic relationship between stress and strain.

An internating observation made was that while the rate of increase of settle-mont deermaked with increase of load for dense sand it increased for lean clay. This type of behaviour is not commonly recognised for sand in laboratory tests. The behaviout of lear clay is prohably due to its incomplete confinement

#### Introduction:-

In most cases when a structure-soil interaction analysis is carried out, the soil is considered to have elastic properties. However, most soils have non-linear relationships between stress and strain. The effect of considering the non-linear properties on both the contact pressure and maximum stresses in the frame is studied in this paper.

For the problem under consideration, the soil behaviour is three-dimensional rather than plans-strain. Three-dimensional non-linear finite element solutions are, however, very expensive and can be subject to stability problems. Consider-ation is given to extrapolating the plane strain results to the three-dimensional case.

#### Choice of model for Non-linear Analysis:

A Hyperbolic relationship between stress and strain is used to model the soil characteristics. The Hyperbolic model takes into account three important har-acteristics of the stress-strain behaviour of soils. They are non-linearity, stress dependency and in-elasticity. In this model the tangent modulus of elasticity is given by equation(1) and the tangent value of Poisson's ratio is given by equation(2), ref.(1).

$$E_{t} = \begin{bmatrix} 1 - \frac{Rf}{2c} \frac{(1-Sin\phi)(\sigma_{1} - \sigma_{3})}{Sin\phi} \end{bmatrix}^{2} k P_{a} \left(\frac{\sigma_{3}}{P_{a}}\right)^{n} \cdots \cdots (1)$$

$$E_{t} = \frac{G - F \log\left(\frac{\sigma_{3}}{P_{a}}\right)}{\begin{bmatrix} 1 - \frac{d(\sigma_{1} - \sigma_{3})}{2c\cos\phi + 2\sigma_{3}\sin\phi} \end{bmatrix}^{2}} \cdots \cdots (2)$$

Where

 $\sigma_1$  and  $\sigma_3$  are the major and minor principal stresses,  $P_{\rm a}$  is the atmospheric pressure.

the definition and role of each of the hyperbolic parameters are given in Table (1)

The hyperbolic relationships are chosen because they have proven quite useful for a wide variety of practical problems for the following reasons:-

- (1) The parameter values can be determined from the results of conventional triaxial compression tests.
- (2) The same relationships can be used for effective stress analyses (using data from drained tests) and total stress analyses (using data from un-consolidated undrained tests)

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(5) Values of the parameters have been calculated for 150 different soils by Wong and Duncan. (1)

The incremental method is chosen to carry out the non-linear analysis because it provides a knowledge of the displacements, streams and strains after dif-ferent stages of loading which is quite useful. The Runge-Kutts echamm is used to improve the accuracy of the incremental method<sup>(2)</sup>

The incremental stress-strain relationship for an isotropic material under plane-strain conditions is given by:

$\begin{bmatrix} \bullet & \sigma_x \\ a & \sigma_y \\ a & \tau_{xy} \end{bmatrix} = \frac{\mathbf{E}_{\pm}}{(1 + \mathbf{Y}_{\pm})(1 - 2\mathbf{y})}$	[(1-V+)	VE	0 ]	[ + (, ]	
1	VE	(1-YE)	0	4 6.	
[ a T xy] (1+ ve)(1-29)	10	0	0 (1-2Yc)/2	0 8xy	(3)

(4)

The modulue of elasticity and Poisson's ratio for each element during each increment are re-etaluated in accordance with the stresses in the element. Thus, the non-linear stress-strain relationship is approximated by a series of linear relationships

In order to represent post-failure behaviour of soils more accurately, Clough and Woodward (3) suggested that it is dusirable to express the strees-strain relationship in an alternative forms

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in which  $H_0$  is the Bulk Modulus = E/2(1+v) (1-2v) and  $H_0$  is the shear modulus = E/2(1+v). The fact that colls have high resistance to Volumetric compression aftar failure but very low resistance to shearing may be represented by reducing the volue of  $H_0$  is mero aftar failure, while the volue of  $H_0$  is maintained at the mame volue as it had in the increment hefore failure.

If His strate level decreases in an element at some increment compared with the previous increment, the unloading-releading modulus,  $E_{\rm UF}$  given by equation (5) is used - - K - P / 5, 18

$$Fur = rur = (F_a) \qquad \dots \qquad (5)$$

Kur is the unloading-reloading modulus number

The Analytical Approach

here

a) Wall: The wall is treated as a frame with rigid arms as shown in Fig.(1) Further details of this technique are given in ref (4).

Walls with two opening ratios were used in the analysis. A wall with (bw/b) = (hw/h) = 0.8, see Fig.1, represents a flexible wall, and so wall with (hw/b) = (hw/h) = 0.4 represents a rigid one. Both walls are 4 storeys high and have a length/height ratio of 2.

- b) Foundation: A strip footing is represented by line elements. Full contect is assumed between the footing and the soil.
- c) Soil: Plane-strain quadratic hybrid elements, with three degrees of freedom per mode are used to represent the soil: The finite element much used is whown in Fig.(2). A very thin column of elements is used much the four columns of elements under the wall in order to obtain a more accurate setimata of the contact pressure under the sdge of the wall.
- The non-linear soil behaviour is represented in the model as explained in the provious section. Two types of soils were considered in this analysis. The hyperholic parameters of each type are given in Table 2. The dense sand, taken from ref.(5), was chosen to represent a very stiff soil, while the lean clay, taken from ref.(1), was chosen to represent a very flexible one.
- 4) Londing: The loads were applied in four equal increments of 50  $\text{KN/m}^2$  each. The first load increment was applied at ground level, the second et first storey level and so on, in order to represent the increase of loads during construction. The total applied load (200  $\text{KN/m}^2$ ) is probably higher than the miximum practical loads on auch buildings. However, it was chosen in order to reach a state

of shear failure in the soil under the edges of the footing. The effect of nuch failure in the soil on the behaviour of the mettling walls must be investigated.

Although the practical loads on walls with big openings could be less than those on walls with small openings (as the loads in practice are mainly dead incid), the same loads were applied to all walls so that comparison could be more readily carried out.

#### Behaviour of Soil under Load:

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Before considering the results of the interaction analysis, the basic behaviour of the soil model used under load should be investigated. For this purpose, the soil model was loaded, incrementally, with a loaded area at the surface. The results of this analysis show the besic difference between the behaviour of the two types of soils used. The rate of increase of settlement with the increase of load decreased for dense sand and increase of settlement with the increase that the stiffness of dense sand and increase of settlement with the increase with the increase of applied load in the range considered. It has to be noted here that the total applied load (200 kM/m<sup>2</sup>) is very small compared with the bearing capacity of dense and, while it is almost equal to half the bearing capacity of the lean clay. The behaviour of dense sand under load will change to that of lean clay as the load approaches its bearing capacity.

The distribution of elastic moduli for both types of soll is shown in Fig. 4. It can be seen from the contours in this figure that, near the sufface, the values of the elastic modulus under the loaded area are much greater than those outwith it. Nowever at a depth  $\geqslant$  a, the lateral distribution of the elastic moduli becomes more even (where a is helf the length of the loaded area)

#### Discussion of Resalts :

The results for contact pressure under the walls and the maximum strasses in them, obtained from the non-linear analysis, are compared with those from an equivalent linear analysis in Fig. 5 to 8. The basis of the equivalency is that the linear analysis would have a central settlement equal to that obtained by a non-linear analysis, under the same total load. According to this definition, the modulus of elasticity equivalent to dense sand and lean clay was found to be 52.5 N/mm and 1.63 N/mm<sup>2</sup>, respectively.

The contact pressure distributions, Fig. 5 to 8. for each load increment are due to this increment of loads only, so that the results for different load increments can be readily compared. The results at the end of the non-linear analysis are also given. We (5)

Comparing the results of the linear and non-linear analysia, the following con clusions can be drawn :

1. The contact pressure distributions under walls supported by lean clay are diffurent from those under walls supported by dense sand. While the contact pressure distribution for the former case tends to become more uniform than that predicted by linear analysis, Fig. 6 and Fig. 8, the contact pressure for the latter case tends to concentrate towards the edges, Fig 5 and Fig. 7.

latter case tends to concentrate towards the edges, Pig 5 and Pig. 7. The reduction in the edge contact pressure under the valle on lean clay ( as compared with the elastic case ) could be caused by the distribution of elastic moduli near the surface of the soil, The values of elastic moduli under a loaded area are such greater than those outwith it, as can be seen in Fig. 4. The same trend will occur under loaded walls. This will reduce the con tribution of the set outwith the wall in resisting the applied loads. i.e. decrease the edge contact pressure. The tendency of lean clay to be more flexible as the applied load increases could be another factor in decreasing the contact pressure under the edges of the footing. A further reduction in the edge contact pressure can occur if the soil under the edges of the footing reaches obser failure because of the high values of contact pressure there. The reduction in the edge contact pressure is about 55% under valls with open-inge ratios of 0.4 and 0.8. Shear failure started after the application of the second load increase there shear failure occurred in the surface element under the edge of the footing. As the load increased the shear failure spread from the failed surface element. The condition of shear failure is :

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#### $\frac{1}{2}(\sigma_1 - \sigma_3) \ge (c \cos \phi + \sigma_3 \sin \phi)(1 - \sin \phi)$

Where of and or are the major and minor principal strenges.

c and  $\phi$  are the cohesion intercept and friction angle. When this condition is estimized the shear modulum of the element is reduced to zero. No dramitic change occurred in the edge contact pressure after fullure because the bulk modulus is multiplied after shear failure as mentioned

follower he cause the bulk modulus is minimized after shear follower as mentioned earlier. For the causes of walls on dense sand, however, the edge contact pressure of the non-linear case increased instead of decreasing relative to that given by the linear analysis. The reason may be that the stiffness of the danse send increases with the increase of the applied loade, as discussed in the previous section. This behaviour under load seams that the sand under the edges of the footing will be stiffer than that under the interior parts because of the concentration of the contact pressure there. As the stiffness of the sand under the edges increase, its share of the load will increase and so will the edge contact pressure. Hence, the tendency of the edge contact pressure to decrease because of the increase of sand the lendency of the edge contact pressure to increase because of the increase of sand stiffness with lead. The result for the walls enalysed was a slight increase in the edge contact pressure (5% for the wall with openinge ratios = 0.8 and 15% for that with openinge ratios = 0.4 )

- 2. As a result of the decrease in the edge contact pressure for Valls on lean clay the miximum atresses in these walls decrease. Fig.9. The reduction is about 49% for both rigid and flaxible valls. On the other hand, the maximum stresses for valls on dense sand increase slightly as a result of the increase in the edge contact pressure. This increase ranges from 20% for rigid valls to a result of the rigid valls to 82 for flaxi hie ones.
- 5. The non-linear analysis yields similar differential settlement results as compured with the linear analysis. As mentioned above, the modulus of elasticity of the linear analysis was chosen such that the total settlement is equal to that predicted by the non-linear analysis under the same total load. Using the squivaleot modulus, not only the total settlements under the walls supported by linear and non-linear soils are equal, but also the differential settlements in both cases are nearly equal. In other words, the sflect of considering the non-linear properties on the differential settlement is negligible when compared with an equivalent linear analysis. The reason for this may be due to the case of loading considered. Because the load was uniformly distributed, the elastic moduli underneath the wall's footing were reasonably uniform, i.e. similar to the linear case. the linear case.
- 4. The increase in the edge contact pressure under walls on dense and is more evident for rigid value than flexible ones. The contact pressure is more con-centrated towards the edges of the footing under the rigid value (bw/b=hv/h=0.4) than under flexible ones (bv/b = hv/h = 0.8) using a linear analysis, compare Fig. 5 with Fig. 7. Hence, the effect of sand stiffening under the edges of the footing, which is the cause of the increase in the edge contact pressure in the non-linear analysis, will be stronger for the rigid wall case. The effect of soil non-linearity would be more evident for rigid walls on hean clays as well, i.e. the decrease in the edge contact pressure would be greater under them than under flexible walls. However, the decrease in the edge contact pressure under the rigid and flexible wells analysed is almost the same. The reason for this is that the lean clay used in the analysis is so eoft that both walls (with openings ratios of 0.4 and 0.8) are rigid relative to it. This can be seen if the contact pressure under both walls using linear analysis is compared, Fig. 6 and Fig. 8. and Fig. A.

#### CORRELATION BETWEEN LINEAR TWO-AND THREE-DIMENSIONAL ANALYSIS

In order that the results of the two-dimentional analysis can be extrapolated to the more realistic three-dimentional case, a correlation between the results of both encode is investigated. For this purpose, the mane value under the same loads are analysed with two-dimentional plane strain finite element for the soil (as described in this paper) and using an elastic half space model hoving the same soil propertiee. A computinon between he results of the half-space and half-plane cases is given in "able 5. These results indicate that:

#### Mansoura Bulletin Vol. 8, No. 1, June 1983.

- 1. Contral settlement of the half-plane model is greater than that of the half-
- 2. Differential settlement of the half-plane model is greater than that of the Minnertial sectionent of the main-prane model is gracter than that to the half-space model by a factor ranging between 1.5 and 4.4. The reason that the factor of increase of central settlement is constant while that of differential mettlement varies may be because the former is a function of soil stiffness only, while the latter is a function of hoth structural and soil stiffnesses. This may also be the reason for the difference in mignitude of the factor of increase for both settlements.
- j. If the maximum stresses in the walls on the half-plane are factorised to the half-space case (divided by the factor for differential settlement) the Result-ing stresses will be emaller than those in the walls on the half-space model by 18-37%

by 18-39% The helf-plane elements were 1 metre thick (equal to the width of the footing). IF, instend, the thickness is increased to 10 m (in order to obtain the same central settlement results as those given by the half-space model) the results would not have to be factorized. Computer runs with finite elements of thick-neans = 10 m indicate that the half-plane model would yield similar differential mettlement and maximum stresses as the half-space model for flexi ble valls. The half-plane model, however, would overestimate the differential mettlement by hot more than 70% and the maximum stresses by not more than 30% for rigid walls. More work is needed to determine the thickness of the half-plane model for different footing widths such that its stiffness would be equivalent to the half-space model.

#### CONCLUSIONS :-

CONCLUSIONS:-The affact of considering non-linear properties on the interaction between the structure and its supporting soil is examined in this paper. This effect depende on the load-settlement characteristics of the soil. If the soil stiffness decreases with the applied loads (i.e. as in Fig. 5a), considering soil non-linearity will lead to a considerable reduction in the maximum stresses in the wall when compared with linear analysis. On the other hand, an increase in each stiffness with applied load (Fig. 5b), can yield elightly higher maximum stresses. That latter type of behaviour is not often discussed in the soil mechanics literature. This may be because it is not easy to produce in laboratory tests. In general the non-linear analysis indicates that an elastic analysis would give results which tend to be conservative as for as prediction of stress due to differ-ential mettlement is concerned. The only exceptions are the cases of long buildinge (relative to the depth of the compressible stratum) or enhesionless soils when the confining pressure is relatively high. Considering coll non-linear the little effect on the ratio between contral and

Considering coil non-linearity has little effect on the ratio between central and differential settlement. In other words, a linear analysin with an equivalent elastic modulus can yield similar differential settlement results as a non-linear one if the central deflection of both analyses are equal.

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Preside Lat	Kane	Puncilion				
E. Eur	Mednius Number					
-at	Nodulux exponent	Relate E, and Eur to Py				
	Cobcasion itercept	and the second of				
1	Priction angle	, selate $(\sigma_1 - \sigma_2)$ in $\sigma_1$				
4	Failure ratio	Kelates $(\sigma_1 - \sigma_3)_{uit}$ to $(\sigma_1 - \sigma_3)_f$				
19	Volsson's ratio parameter	Value of vist of * P				
¥.	ditta	Decrease in v for tentfuld increase in $\sigma_3^{L}$ .				
.4	ditto	Nate of increase of v with strain				

TABLE (1) - SUPERRY OF HYPERBOLIC PARAMETERS

4

r Nia <sup>3</sup>	k	4ur		d	Gt	E	C KN/m <sup>2</sup>	¢ degrees	<sup>8.</sup> t	*o
Dense 17.5 Lean e	1600	1900	1.0	0,25	0.45	0,17	0.0	43	0.9	0.3
6	80	200	0.85	4.2	0.3	0.25	40	10	0.8	0.7

k is the coefficient of earth pressure at rest.

TABLE (2) - VALUES OF NON-LINEAR PARADETTES OF THE TWO TYPES OF SOILS USED 15 THE ANALYSIS.

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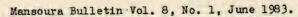
case considered	i-space model	}-plane model	isctor
1. $hw/h = bw/h = 0.4$			
. E = 4.45 104/m <sup>2</sup>			
settlement (a)	0.1	1.084	10.8
differential settlement (mm)	2.73	4.9	1.75
maximum stress (N/mm <sup>2</sup> )	0.85	1.22	187
hw/h = hw/b = 0.4			
E = 22.25 191/m <sup>2</sup>			
settlement (m)	0.021	0.224	10.7
differential settlement (mm)	2.2	4.7	2.14
maximum stress (N/mm <sup>2</sup> )	0.732	1.1	267
3. $hw/h = bw/b = 0.8$			
$E_{s} = 4.45 \text{ MN/m}^{2}$			
settlement (m)	0.109	1.11	10
differential settlement (mm)	21.7	56.4	2.56
maximum stresses (N/mm <sup>2</sup> )	2.76	5.15	272
hu/h = bu/b = 0.8			
E = 22.25 MW/m <sup>2</sup>			1
settlement (m)	0.023	0.24	10
differential settlement (mm)	8.0	35.2	4.4
maximum stress (N/mm <sup>2</sup> )	1.257	3.36	397.

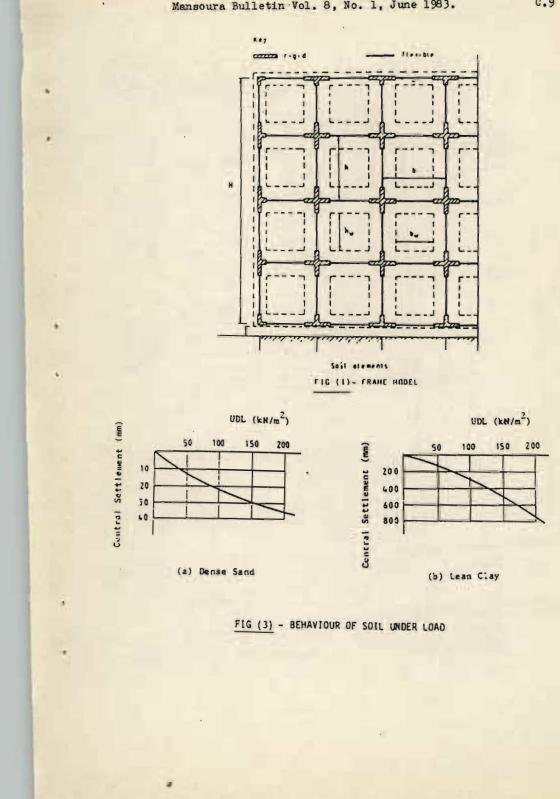
 The percentages are the ratios with which the maximum stresses will be underestimated if the 1-plane results are factorised to give the same differential settlement as the 1-space case.

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for definition of symbols see Fig (1)
 Es is the elastic modulus of the soil .

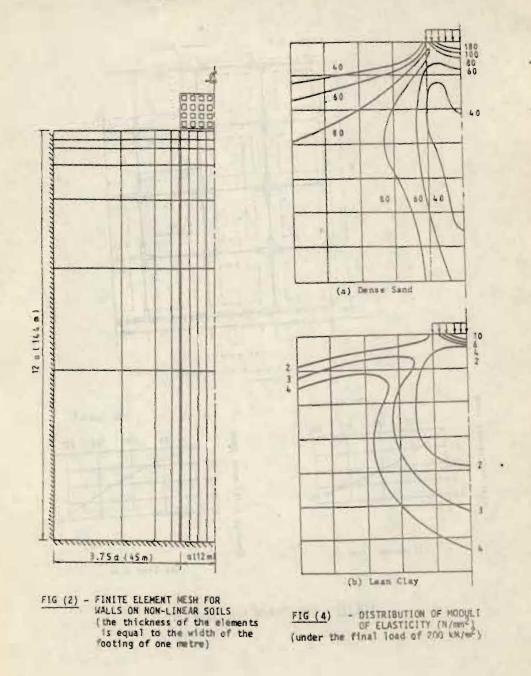
TABLE (3) - RELATION BETWEEN HALF-SPACE AND HALF-PLANE MODELS



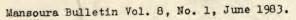


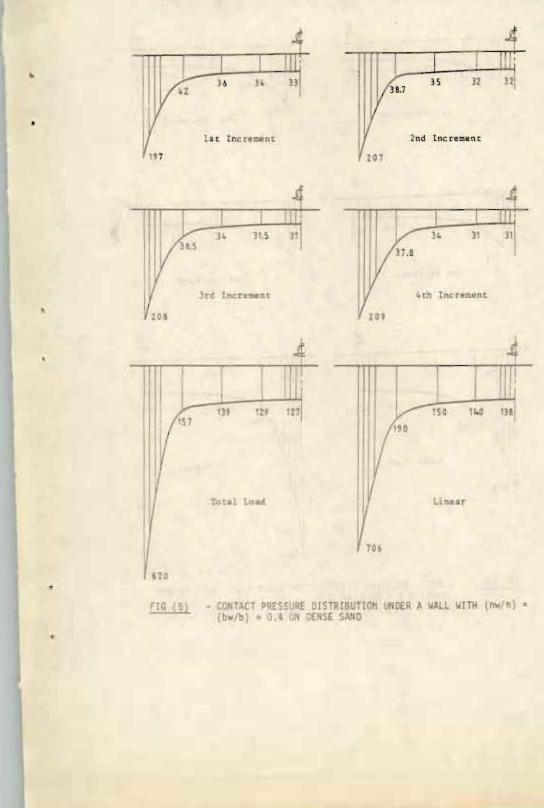
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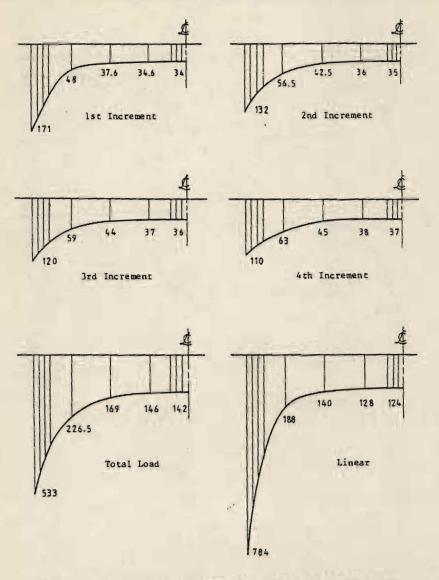
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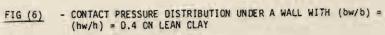


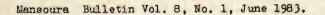
C.11

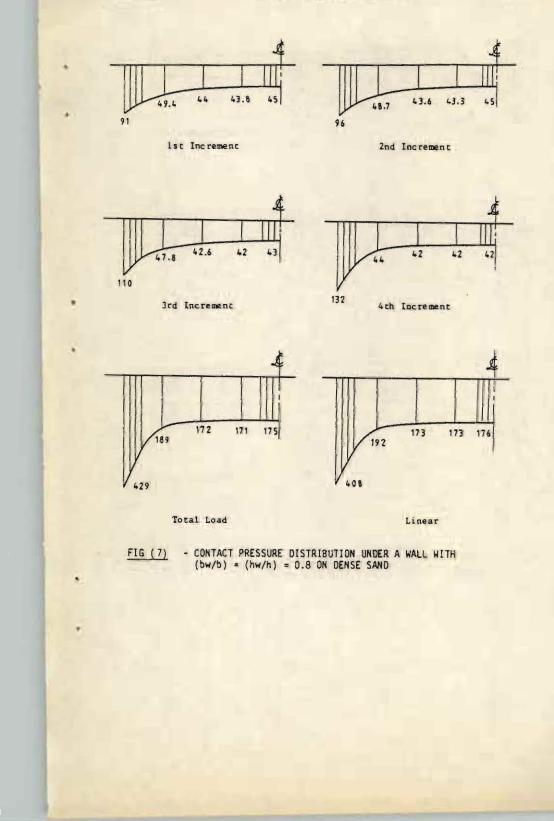
C.12, Sherief Abu-El-Magd.



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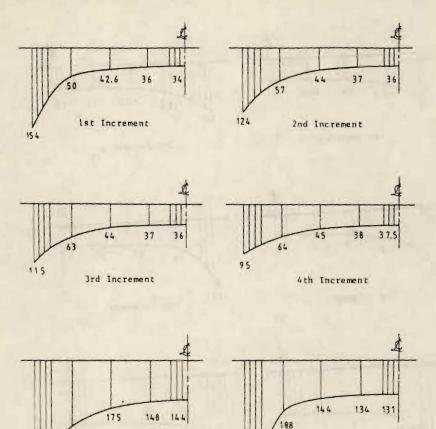






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FIG (8)

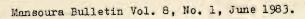
438

236

Total Load

- CONTACT PRESSURE DISTRIBUTION UNDER A WALL WITH (bw/b) = (hw/h) = 0.8 ON LEAN CLAY

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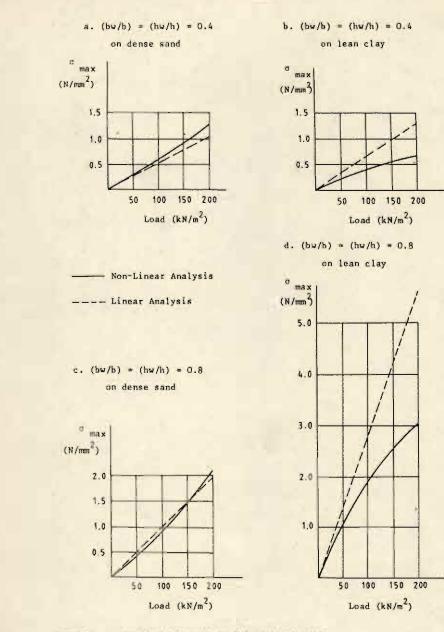


FIG (9) - MAXIMUM STRESSES IN THE ANALYSED WALLS

C.15