## **Mansoura Engineering Journal**

Volume 8 | Issue 1

Article 3

6-1-2021

## Studies in Tidal Phenomena.

Abdel-Razik Zidan

Assistant Professor, Irrigation and Hydraulics Engineering Department, Faculty of Engineering, Mansoura University, Mansoura, Egypt., ahmedzidan@live.com

Follow this and additional works at: https://mej.researchcommons.org/home

## **Recommended Citation**

Zidan, Abdel-Razik (2021) "Studies in Tidal Phenomena.," *Mansoura Engineering Journal*: Vol. 8 : Iss. 1, Article 3.

Available at: https://doi.org/10.21608/bfemu.2021.180175

This Original Study is brought to you for free and open access by Mansoura Engineering Journal. It has been accepted for inclusion in Mansoura Engineering Journal by an authorized editor of Mansoura Engineering Journal. For more information, please contact mej@mans.edu.eg.

C.32. A.K.Zidan.

#### STUDIES IN TIDAL PHENOMENA

Zidan, Abdel Razik A."

## ABSTRACT

As a result of complexity of the tidel current and weter level prediction problem; before the computer time, reliance has mainly been placed on field measurements and tidel model studies to obtain a reliable picture of water levels and tidel currents in inlets, bays, and setuaries. The expense connected with either of these two methods has greetly restricted to emount of tidel current and tidel range informations.

At the present, due to the increasing capacity of high epeed digital computer end the different numerical techniques for solving the governing equations of motion, the use of mathematical models for tidal flow computation is quite well established. The main objective of this present study is to investigate the influence of boundary resistance on tidel wave propagating elong an estuary or inlat and also on the tidal currents. An increase of boundary resistance will decrease the tidel renge and the corresponding tidel current. Resonance could occur at low value of boundary resistance, which will influence both the characteristics of tidel wave and tidal current. The influence of freah water discharge in conjunction with boundary resistance on the tidal phenomena is also investigated.

## INTRODUCTION

The aim of studies of tidee could be classified into three main purposes: (i) scienfific interest; (ii) nevigation to predict water level end/or current for a given place; (iii) hydraulic engineering to predict the effect of changing the conditions by hydraulic structures or by

# Lecturer, Irrigetion and Hydraulice Dept., Mansoura Univ.

natural causes as an example is a prediction of tidel current in planned canal connecting two different tidal regimes such as Suez Canel and Panama Canal. The main objective of this work is to investigate the influence of boundary resistance and/or river flow on the tidal wave end tidel current. Analytical studies were used, before the computer time under simplified essumptions Ref.(4).

C.33

The mathematical model has been used since comprehenaive field measurements are expensive and time consuming, and the physical models suffer serious scale effects.

#### Tidel Constituente:

Orbits of earth eround the sun and of moon around earth are not circles but ellipses, that is distance sun-earth and earth-moon vary periodically so the gravitational force of attraction exhibits a maximum and a minimum value during each orbit. The orbitel plane of revolution of earth round tha sun is inclined to an angle to the sun axis. The axis of the moon is also inclined to the plane of its orbit round the sarth consequently the gravitational tide producing force at a given point on the earth varies in a complex, but a predictable manner. The largest component of this force is due to the moon for its proximity from the earth and has a period of about 12 h 25 min.

The lunar tidel force reaches its maximum value once in 28 days when the moon is nearest to the serth, when the moon is furthest, the lunar tidel force is about 2/3 its maximum value. The total force due to combined action of sun and moon is greatest when they ect together that is when the sun and moon are se nearly in line with the earth as possible. This happens twice a month, when the moon on the side of earth as the sun, i.e. during a full moon and a new moon. When this happens apring tides occur, having erange of movement bigger than the average. When sun and moon in quadraturc with the earth their effect gives rise

## C.34. A.R.Zidan.

to smaller range than the average when this happens neap tide occure which is also twice a month.

A list of components can be made from the harmonic analysis of the tide generating force Ref.(10). Bogran (1883) gave a list of 29 partial tides. A list in the Admiralty Mannual of Tide by Herrie Contains 23. The British Admiralty Manual of tide gave 20.Some of these partial tides half a period, up to half year, S ea component due to the declination of eun with the equator. The hydraulic engineer is not concerned directly with tide generating force, but with thair effects on rise and fall of water level. He is not usually interested with partial tide having long periode, as he wants to be informed about a very high or very low, high water level and low water level, or the maximum velocity of the current at a place where he is going to work For that reason it is not necessary to consider all the partial tides in tha hydraulic engineering, the following table gives the principal harmonic components which account for 83% of the total tide generating force Ref.(8).

Tabla (1) Principal Harmonic Component

Name of Component Principal lunar	Symbol M2	Period Bolar houre	Amplitude ratio	
			100	
Principal solar	S2	12.00	46.6	semi
Larger lunar elliptic	No	12.66	19.2	diurnal
Luni-solar semidiurnel	K2	11.97	12.7	or at the r
Luni-solar diurnal	ĸī	93.93	58.4	
Principal lunar diurnal	01	25.82	41.5	diurnal
Principal solar diurnal	P1	24.07	19.4	

It is seen that the larger part of the tidal variation is due to moon and the principal effects are due to variation of phase of moon, distance and declination. The diurnal tide could be found on the Coast of China, Alaska, and the gulf of Mexico. The semi diurnal tide on the shore of Atlantic ocean and the mixed tide on the pacific Coast of the North America.

### NUMERICAL MODEL

Mathematical models of tidel flow computations are based on the equations of motion, the continuity and dynamic equations;

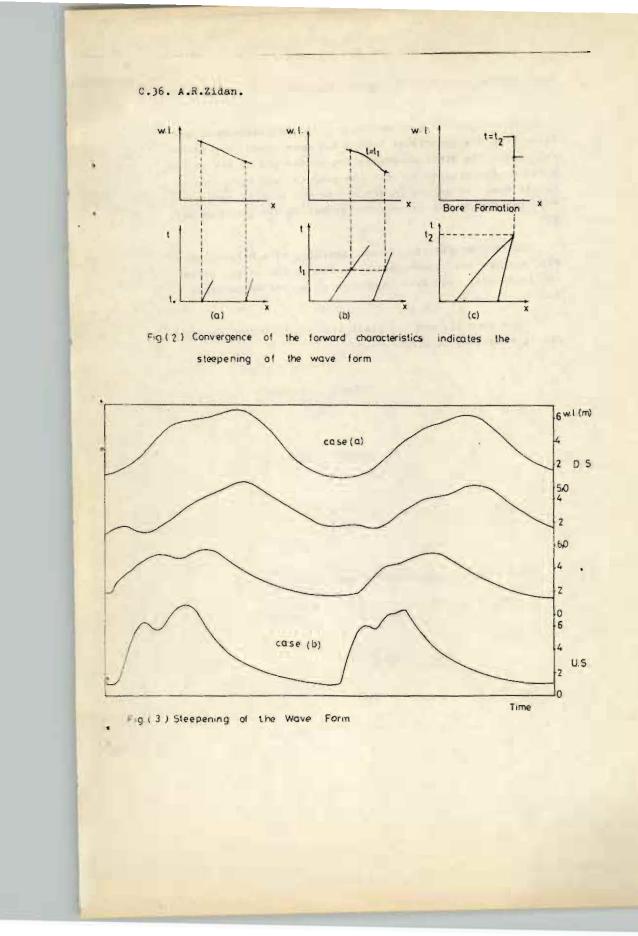
$$\frac{\partial Q}{\partial x} + b \frac{\partial h}{\partial t} = 0 \qquad \dots (1)$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial t} = S_0^{-}S_f \qquad \dots (2)$$

in which;

Q = water dischargs; b = instantaneous surface breadth; u = water velocity; h = water surface alsoation; S<sub>0</sub> = bed elops; and S<sub>f</sub> = friction elops.

The numerical techniques for the solution of these two governing equations of motion are based on three main approaches: (1) method of characteristice; (11) finite difference method; (11) finite element method. The characteristic method has the advantages of transformation of tidel wave as it proceed along the estuary. Convergance of forward characteristics indicates the steapening of the wave. Their intersection indicates the formation of e bore Fig.(2). Figure (3) demonstrates the steepening of

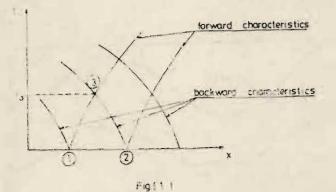


flood tide when the wave propagates in the upstream direction. The characteristic method has been found more accurate among the other numerical techniques and it has proved a faster convergence between the computed and actual water levels even for errors in estimating the initial conditions. More details of the characteristic method are given in Ref. (1).

C.37

Section proparties, echematization, of a natural estuary, such as mean depth depth, watted perimeter and cross sectional area have been incorporated in the mathematical model.

Equations (1) and (2) yield the two following cheracteristic equations Fig.(1);



The forward characteristic equation:  $u_{3} + 2c_{3} = u_{1} + 2c_{1} - \int_{0}^{t_{3}} \left[ g \frac{\partial z}{\partial x} + g \frac{u |u|}{c^{2} \cdot R} + \frac{u \cdot c}{b} \frac{\partial b}{\partial x} \right] dt \qquad \dots (3)$ 

### C.38. A.R.Zidan.

The backward characteristic equation:

$$u_{3} - 2c_{3} = u_{2} - 2c_{2} - \int_{0}^{t_{3}} \left[ g \frac{\partial z}{\partial x} + g \frac{u_{1} k_{1}}{C^{2} R} - \frac{u_{1}c}{b} \frac{\partial b}{\partial x} \right] dt \qquad \dots (4)$$

The two equations confirms the effect of estuary shape on wave speed and water current. This is small if

 $\frac{\partial \ln(b)}{\partial x}$  is less than  $\frac{g u | u |}{c^2 \cdot d}$ .

Some eqtuaries have appreciable value of bad elope with respect to section elope such as the Thames of England and the Houghly of India other esturies have very flat bed alope  $\left(\frac{dz}{2x} = 0\right)$  such as the Deleware estuary of the United State, where the friction term is three to four times the slope term. This flat bed slope could help in the analytical solution based on the incident and reflected wave.

It seems desirable to develop characteristic models which have the ability to choose the most efficient and stable computation for a given set of conditions of time increment, space increment, water velocity and calerity of the vave at a particular time and place Ref.(4).

## Boundary Resistance

Friction parameters for use in a numerical model can be obtained in esveral ways. The final choice may be modified during the process of calibration and will depend on the feature of the channel, they are used as a compensating factors for the lack of interpolation technique and represention of the cross sectional properties along the estuary in the mathemetical model. The roughness coefficients computed by Manning's equation  $n = \frac{AR2/3 \gamma S}{Q}$  or Chezy coefficient  $C = \frac{Q}{A \cdot \sqrt{RS}}$ , or any similar equation are not real roughness, but numerical coefficient, which relate to the section properties such as hydraulic redius, and cross sectional area, to the discharge and energy slope. In lined prismatic channels, these roughness values can be considered to represent physical roughness. In a composite natural section contains zones of different bed roughness and/or over bank flow areas, these coefficients are numerical values, any procedure which sttempt to use these values es a true roughness is absolutely wrong Ref.(3).

The numerical Manning's coefficients 0.01, 0.022, and 0.05 have been used in the model.

#### Boundary Conditions

Estuaries are controlled by the tidal action at ese end and by the river flow. They are two main independent variables. Some estuaries have negligible fresh water flow, and othershave lost all contact with river that formed them, all estuaries were formed by the combined action of tide and river flow.

All numerical models require boundary conditions et the landward end the seaward end. At the landward end, from river flow. When tide propagates along an estuary of finite length and nagligible river flow, assuming e complete reflection at the setuary head, the flow is zero and this could be applied in the case of e gulf.

Two values of river flow have been incorported into the mathematical model for hypothetical estueries under investigation, normal river flow (50  $m^3$ /Sec) and flood water flow (1000  $m^3$ /Sec.). At the seeward end tidal gauge recorde have been used.

## C.40. A.R.Zidan.

## ANALYTICAL STUDY

The governing equations of motion, (1) and (2), reduce to the classical wave equation, for estuaries of constant depth and crose sactional shape, and negligible friction sffect.

$$\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2} \qquad \dots \dots (5)$$

$$\frac{\partial^2 \ell}{\partial t^2} = c^2 \frac{\partial^2 \ell}{\partial t^2} \qquad \dots \dots (6)$$

in which:

u = tidal current; c = wave celerity;

 $\chi$  = water surface elevation elative to the mean depth.

The two foregoing equations could be satisfied by a single harmonic function

$$\frac{1}{2} = \frac{2}{\max \cos (ft - kx)} ....(7)$$

$$u = \frac{2 \tan c}{d} \cos (ft - kx) ....(8)$$

in which:

.

f = tidal wave frequency = 277/T;
k = wave number = 277/L;
L = wave length;
T = wave period;
2 m = maximum amplitude;
d = mean weter dapth.

In short frictionless eetuary the tidal wave will be reflected at the head of the eatuary. For a complete, reflection the reflected wave is given by

$$2 = \frac{2}{\max} \cos (ft + kx)$$
 .....(9)

and the corresponding current is given by

superposition of the incident and reflected wave gives

The corresponding current is

$$u = \frac{22 \max c}{d}$$
 Sin (ft) Sin (kx) .....(12)

which represents a case of standing oscillation maximum velocities occur at time of mean water level that is at half tide.

The tidal elevation and tidal currents in real systems can be considered to be a combination of large number of incident and reflected tidal constituents, each have its own amplitude, wave length and frequency.

The reflection occurs at the head of the astuarg is not a complete reflection, mainly due to the presence of freeh water discharge and boundary resistance. The incident wave will suffer frictional dissipation end convergence of the estuary cross section, while the reflected wave suffers divergence of the channel cross section and frictional dissipation of energy as well. For these ressone the value of maximum tidal current may not occur exactly at half tides Fig.(13), and the ebb period will be larger than the corresponding flood period.

#### C.42. A.R.Zidan.

## RESULTS AND ANALYSES

The total energy, which consists of kinetic energy and potential energy, of a wave could be given by, Ref.(6)

$$E = \frac{1}{8} \cdot \chi \cdot H^2 L \qquad \dots \dots (13)$$

in which; E is the total energy, H = wave height, and L is the wave length.

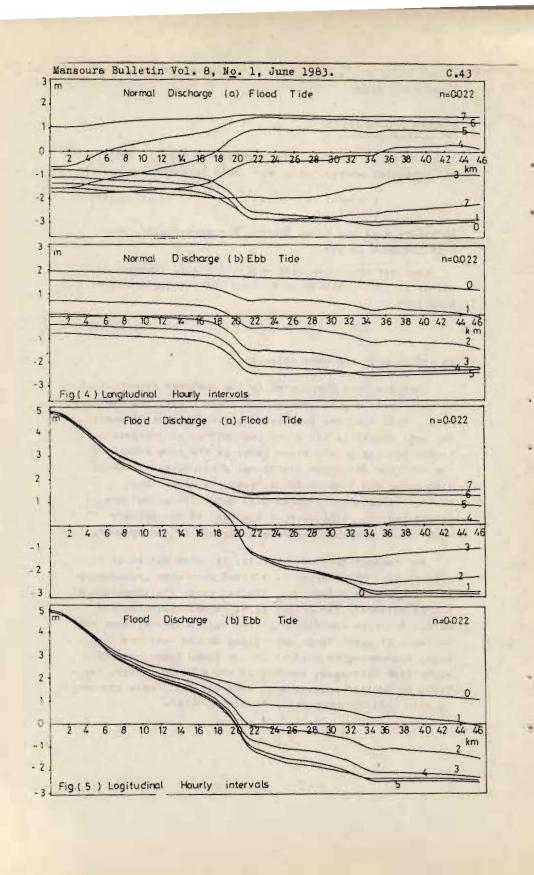
Wave not only possesses energy but also transmit this energy in the direction of motion. This is given by the equation:

$$\frac{dE}{dt} = \frac{1}{8} \forall . H^2.c \qquad \dots \dots (14)$$

in which; c is the wave celerity.

When the wave propagetes in the upstream direction of an estuary or e gulf, refraction could occur, end the wave height will increase because of e fixed amount of energy per unit length is being confined within an increasing nerrow passage.On the other hand, as the wave travels in the upstream direction frictional discipation of energy will occur and this could decrease the tidal range. Another complicated problem will exist for an estuary of finite length, reflection at the head of the estuary which could increase the wave amplitude in the upriver.

For reasons mantioned before, it eseme difficult to predict what will happen to a tidal wave when propagating in the upstream direction. Fig.(4) gives the longitudinal hourly intervals for apring tida, normal discharge and normal friction coefficient. The figure demonstrates the decrease of tidal range when going in the upstream direction, eteapening is noticed in the flood tide. As the river flow increases, damping of the wave increases, resulting in smaller amplitude of wave Fig.(5). More distortion is eleo noticed especially in the upriver.



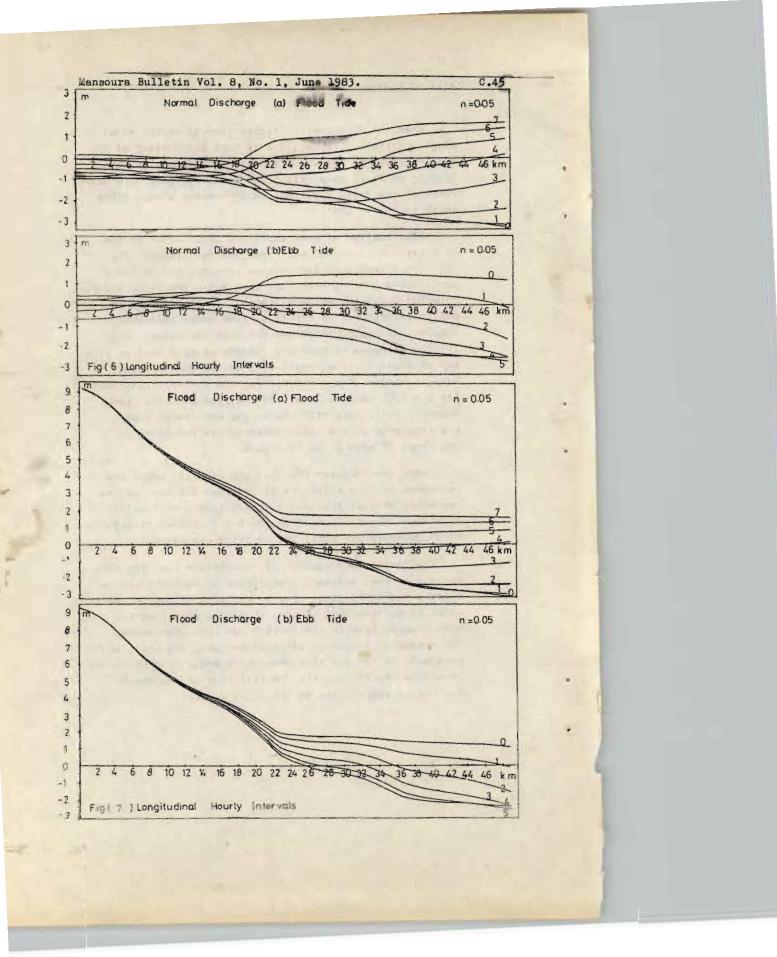
# C.44. A.R.Zidan.

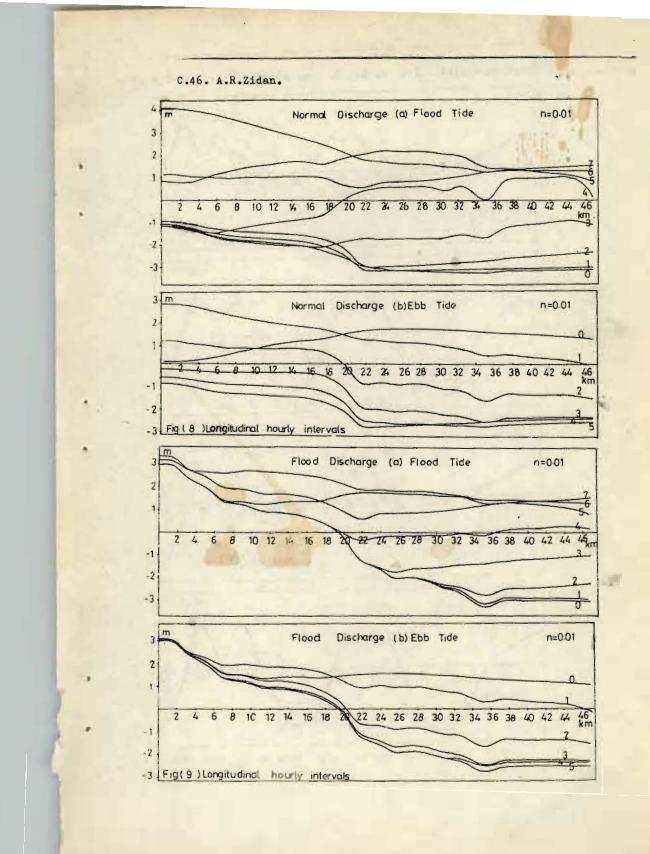
When the friction coefficient increases the tidal renge decreases, Fig.(6), due to more dissipation of the wave energy. In the condition of flood discharge more demping of tidal wave will occur resulting in a more decrease of the tidal emplitude which reaches a negligible value in the upriver.

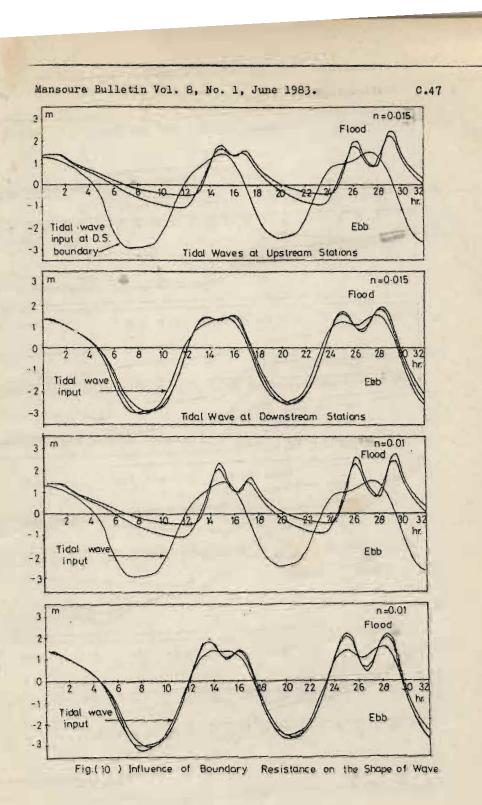
Amflification of wave amplitude could occur in the up river for lower value of friction coefficient, Fig. (8). This amplification becomes infinite if the tedal period of any tidal component approaches the value  $4l/\sqrt{gd}$ . in which; ( is the eatuary length. The phenomenon is called resonance. As the river flow water increases damping will occur which prevent such resonance. Fig. (9).The decrease of boundary resistance will have an effect of ehape of tide, Fig.(10) show the size of tidal hump is bigger. for n = 0.01 then the corresponding size for n = 0.01 especially at the upstream stations. Low boundary resistence will change the amplitude, phase, and frequency of the tidal consitudents resulting in the shape of wave given in figure.

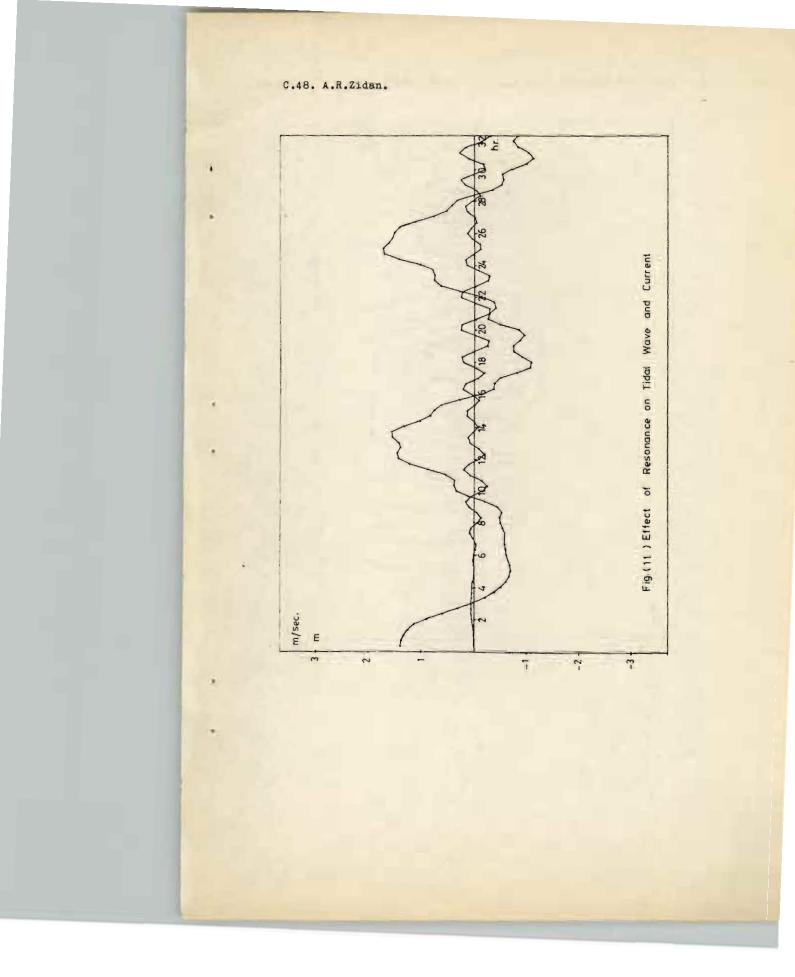
Comparison between Fig.(11) and Fig.(12) shows the resonance is more effective at upstream station, as the reflected wave at the head of the estuary, will suffer frictional dissipation of energy and a channel divergence which decrease its amplitude in going downstream.

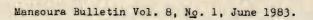
The resonance frequency is equidistant i.e. the difference between adjacent frequencies is constant and is about 2 hours Fig.(12). In the ebacence of damping factor, which is difficult to obtain, it may be said that the semi diurnal tide is responsible for this phenomenan. The resonance frequency of tidal current, Fig.(12), is then same as for the tide wave, which could mean the corresponding current for that partial tide is responsible for the irregularities of the tidal current.

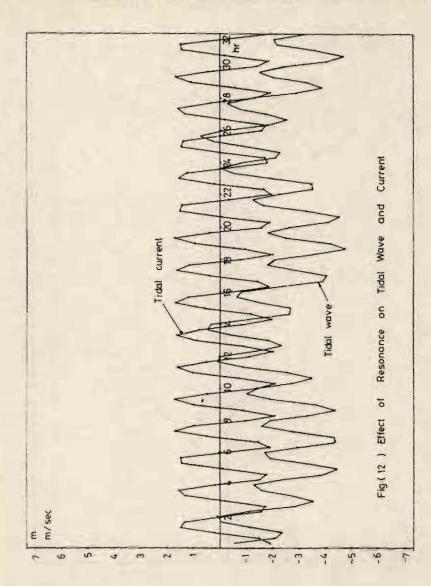












C.49

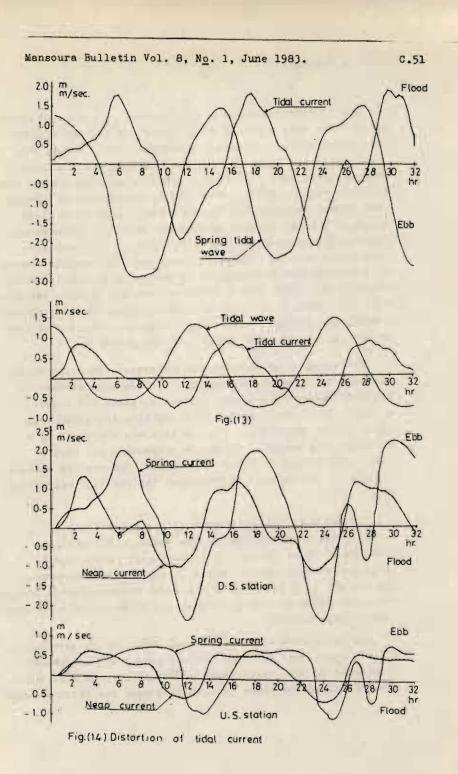
C.50. A.R.Zidan.

Due to coonplexity of tidal current, no theory of tidal current has been advanced which has found general acceptance by the hydraulic engineers. Stevanson (1872) stated tha tidal wave and tidal current are two separate phenomena, he considered that the tidal current is entirely due to the slope of water surface. West (1973) introduced an approximate lineer relationship between tidal current and tidel range in the Tay estuary of Scotland Ref.(2). Considering the strength of the ebb and flood currente, the ebb flow will drain off flate tende to concetrate in the main channel as a consequence generally to be faster as in the Tay astuary Ref.(7). This method could be reversed in some estuaries i.e. the strength of flood will be stronger than the correaponding ebb current, due to the topographic feature of the estuary as in the river Houghly of Indie Ref.(8).

Deepening of an eetuery could increase the fload duration and decrease the ebb period. In the Lune eetuery of England, deepening the main channel by about 1.0 m over a length 7Km. The duration of flood tide increased from 3h 20 min to 3h 45 min. The ebb tide was shortened by a curresponding amount. Extensive deepending can have e measurable effect on tidal propagation, reduces the maximum flood tide velocities and increases the ebb tide velocities Ref.(8).

The hydraulic investigation of the river Forth of Scotland has revealed that at the mouth of the estuary strength of tidal current is proportional to the tidal renge and when the wave travels in the upstream direction, the current is a function of the cross sectional area, frictional dissipation of energy, reflection of the tidal wave and type of tide Ref.(11).

The tidel wave has a sinueoidal shape in the deep weter, for L/d  $\leq$  2. When the wave propagate in a shollow water distortion for both tidal wave and tidal current will occur. Fig.(13) gives the shape of both tide wave and tidal current



### C.52. A.R.Zidan.

for epring end neap tidee, the profiles of both tide wave and tide current are more or less einusoidal but as the wave propagate in the upstream direction distortion will occur for both tidal wave and tidal current Fig.(14).

## CONCLUSION

Tidal motion in any estuary is a turbulent unsteady non uniform flow which is mainly governed by the boundary resistance, river flow and downstream tide wave. Difficulties lie in predicting the water surface elevation or tidal current in any analytical way. The eccuracy of mathematical tidal flow model is as good, if not better than the tradiditional physical model, provided care is teken to minimise numerical echematization error and the friction parameters are determined from field results.

Bed elope, friction effect end change in channel geometry have a direct effect on both the tidal current and tidal wavs. A configuration between setuery mean depth, boundery resistance and setuary length may leed to the phenomenon of resonance. This will effect both the tidal current and tidal wave. An increase of freeh water discharge end/or boundery resistance will dempen the tidal emplitude and prevent the phenomenon to occur. The tidal current hes been found more sensitive to this resonance then the tidal wave.

Dredging of an estuary or any tidel water wey will decrease the boundary resistance according to the formula  $g = \frac{u|u|}{C^2 R}$  or  $\frac{g u|u|}{C^2 d}$  for wide channel. This increases the tidel range, increases the flood duration, decreases the ebb period, and the tidel wave will be less distorted. Further and extensive despening could lead to a resonance.

The increase of boundary resistence and/or river flow will distort the shape of tidal wave, further increase of

one of these two paremeters could result in changing the character of the wave from being oscillatory to a progressive type.

Propagation of the tide wave along the river could result in steepening of the flood tide. Once a steep fronted wave is formed vertical accelerations become large and may lead to the formation of highly turbulent travelling surge or a bore. The dynamic equation satisfies quite well the conditions upstream and downstream the bore, but it is not applicable in the bore itaelf. The equation has to be modified to cops with such situation.

C.53

#### C.54. A.R.Zidan.

## APPENDIX (I) REFERENCES

- Abbott, M.B., "Computational Hydraulics" Elements of Theory of Free surface Flow, Pitmen Advanced Publishing Program, London, 1980.
- (2) Charlton at al., "Tidal and Fresh Water Induced Circulation in the Tay Estuary" Proceeding of the Royal Society of Edinburgh (B), 75, 2, 1974/1975.
- (3) Cunge J.A., et al., "Practical Aspect of Computational Hydraulice", pitman Advanced publishing program, London, 1980.
- (4) Einstein and Fuche, "Computation of Tides and Tidal Currente", United State Practice, Proc. A.S.C.E. Journal of the Hyd. Div., June 1955.
- (5) Ellia, J., "Unsteady Open Channel Flow" Annual Meeting of Hydraulic Specialista, Portemouth Polytechnic, September 1979.
- (6) Hendereon, F.M., "Open Chennel Flow", Macmillan Co. Ltd, London, 1966.
- (7) Huthance, J.M., "Tidal Currant Asymmetric over the Norfolk Sendbenke", Estuerina and Coastal Marina Sciance, 1973, 1, pp. 89-99.
- (8) MacDowall, D.M., and O'Conner, B.A. "Hydreulice Behaviour of Eatuaries" Macmillen Prese Ltd, London, 1980.
- (9) Proudman, J., "The Effect of Friction on e Progressive Weve of Tide and Surge in an Estuary" Proc. Roy. Soc., London, A., 233, 407.
- (10) Thijieea, J.T.H., "International Course in Hydraulic Engineering" Oelft, Netherland, 1965.
- (11) Ziden, A.R., "A Hydraulic Investigation of the River Forth", Ph.O. Thesis, Strethclyde University, Scotland.

#### APPENDIX (II) NOTATION -----

The following symbols are used in this paper

A 😕	wat	er	ar	68
-----	-----	----	----	----

- = instantaneous top width; b
- C . Chazy coefficient;
- c wave celerity;
- d mean water depth;
- E = wava energy;
- f = wave frequency =  $\frac{2\pi}{T}$ ;
- = acceleration due to gravity; 9
- H - wave amplitude;
- = water surface elevation; h
- k. = wave number;
- L = wave length;
- = wave length; = estuery length; 1
- n Manning'e coefficient,
- R = hydraulic radiue; S<sub>0</sub> = bed elope; S<sub>f</sub> = friction elope; T

- T = wave period;
- u = weter velocity;
- W.L. = weter level;
- 5 x = space increment;
- St =time increment;
- 2 = water eurface elevation relative to mean depth, and
- 2 max = maximum amplitude of wave.

14