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MATHEMATICAL MODEL OF SYNCHRONOUS COMPENSATOR OPERATING IN CONJUNCTION WITH A RIGIDLY IMPULSED INVERTER

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## ABSTRACT

A synchronous compensator is recently used in conjunction with a rigidly impulsed inverter to supply an isolated AC load. In this case the inverter frequency is adjusted to be equal to the load frequency. In order to hold it constant, the feed-back control between the rotor speed and inverter frequency must be investigated. The system consumes its requirements of active power from the inverter through a DC-link which may be connected to an unconventional source of electrical power. Reactive power requirements will be supplied from compensator. In such a system, and after synchronizing the inverter with the DC-link, it is expected to have an oscilating behaviour which may force either the compensator to go out of stability or the inverter to have a failure.

The paper is concerned with the formulation of the quasi-steady behaviour of the foregoing through an adequate mathematical model. It will be based on the time varying effective value. The proposed model gives three approaches during formulation process of the problem. The computer results show the necessity of the system to be integrated with any conventional type of control.

LIST OF SYMBOLS

V	:= Voltage across the inverter AC side, load and compensator, r.m.s.
Е	:= Voltage behind the compensator stator leakage reactance, r.m.s.
	:= Excitation voltage, time-varying effective value.
E vf	:= Voltage across the inverter DC-side, time-varying effective value
	· · · · ·
V <sub>D</sub>	:= Voltage across the DC-link behind the smoothing reactor, time-
Þ	varying effective value.
I	:= Current in the DC-link, time-varying effective value.
I.	:= The inverter current, time-varying effective value.
I I N I S I L N	:= The compensator current, time-varying effective value.
-TS	:= The load current, time-varying effective value.
L.	
	:= Constant of the inverter current = $\sqrt{6}/\pi$
н <sub>S</sub>	:= Compensator resistance, in Ohms.
XS	:= Synchronous reactance, in Ohms.
XD	:= Compensator leakage-reactance, in Ohms.
R XS XP a <sup>P</sup>	:= p / ( J <b>. ლ</b> ე)
p X_S X_E	:= Number of pole pairs.
X.	:= Compensator subtransient reactance, in Ohms.
x <sup>S</sup>	:= Subtransient reactance of transformer may be connected with
ΞE	compensator, in Ohms.
7	
Z Z,S	:= Compensator synchronous impedance, in Ohms
Ζ,	:= Load-impedance, in Ohms.

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:= Inertia coefficient of compensator rotor, kg-m<sup>2</sup>.
J
<sup>P</sup>f+₩
      := Friction and windage loss of compensator, watts
      := Nominal rotor speed, which corresponds to the rigid inverter-
៷
         frequency, in electrical rad./second.
W_r/W_o := Relative speed of E_f
W_v/W_o := Relative speed of V.
:= Arctan (R_g / X_g)
β
      := Advanced angle of the inverter, elec. rads.
้อร
      := Load angle of the compensator, elec. rads.
      := Commutator angle, elec. rads.
T<sub>D</sub>
      := Time interval, in sec.
```

#### 1.0 INTRODUCTION

Synchronous compensators are usually applied today across the AC side of inverter type convertors, which are used to permit the electrical energy to flow from a DC-link to an isolated AC load. So, the synchronous machine is suggested mainly to generate the AC voltage across the corresponding side of the inverter. This voltage is necessary to ensure voltage type commutation for the inverter. It is a simple method of commutation to be used. In addition to this job, the synchronous machine has to deliver the reactive power needed by the inverter and the load.

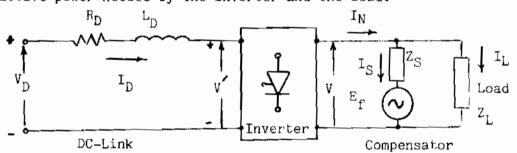


Figure 1 : Schematic Diagram of the Investigated System

Frgure 1 shows the schematic diagram of the investigated system. It consists of a DC-link, a rigid impulsed inverter, a synchronous compensator and an isolated load. The inverter is suggested to be rigidly impulsed in order to hold the load frequency constant. Therefore, feed-back control between the compensator rotor speed and the impulse-frequency is not required. The input power to the DC-link may be supplied from a HVDC transmission line or from a renewable source of electrical power. The system can also be suggested to work in conjunction with the shaft alternators (4) .The synchronzation problem of the inverter with the DC-link had been discussed in reference (5).

In this paper, a mathematical model of the above described system will be derived to represent its quasi-steady behaviour after synchronzation. Natural oscillations in the compensator speed, due to the absence of adapting the rotor speed with the triggering frequency, will be expected. They may force the synchronous machine to go out of stability or may lead to an inverter failure. The interaction between the synchronous, as the only source of voltage and reactive power, and the inverter, as the only source for current and active power plays a great role in the overall system stability. Accordingly, the system may be assisted by any type of conventional controls in order to ensure more stable operation. For example this will be achived by applying continous control to the compensator excitation or by controlling continously the DC level behind the DC link.

The proposed mathematical model describes the system through three approaches having the following features:

- 1- The first approach does not consider any of the above mentioned controls
- 2- The second approach considers only the excitation control in order to maintain constant terminal voltage.
- 3- The third approach adds to the excitation control the control of the voltage behind the DC-link.

The additional type of control suggested in the latter approach aims mainly to hold the advance angle  $\beta$  of the inverter constant at a proper value and away from its two extreme limits. The commutation angle  $\boldsymbol{\mathcal{T}}$  is taken to be the lower limit. The advance angle  $\beta$  must be greater than the commutation angle. As a maximum limit, the angle  $\beta$  is not allowed to be equal or greater than  $\pi/2$ , else the power flow will be reversed. The foregoing both limits lead to inverter failure (6).

# 2.0 MATHEMATICAL MODEL

As the synchronous compensator is supplied from the inverter, the speed of the rotating field established by the stator currents will be proportional to the triggering frequency of the inverter impulses. The rotor speed will be in turn equal to that of the rotating field. Under steady state , the balance of the power supplied to the system must be exist such as :

1-The active power supplied by the inverter must be equal to the active power cons-

umed by both compensator and load. 2- The reactive power supplied by the compensator must be equal to the reactive power

consumed by the inverter and the load. The proposed mathematical model is based on small perturbations in the rotor speed,w. They are due to lacks of the proper damping and control. Theses small perturbations in the rotor speed are caused by the attempt of both power source in the system to get the power balance. Therefore, the rotor speed will oscillate in air-gap around its nominal value w and the relative rotor speed (w\_/w\_) can be taken as a measure of the expected oscillations. Accordingly, the phase shift ( $\beta + \delta$ ) as shown in figure 2, between

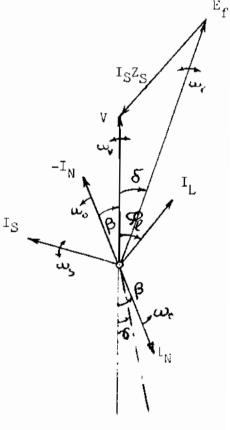


Fig. 2: Ouasi-Steady Complexor Phasor Diagram.

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the rigid frequency inverter current  $I_N$  and the oscillating excitation voltage  $E_f$ . This variation is due to both variations in  $\beta$  and  $\delta$ . The variation in  $\delta$  is naturally caused by the rotor oscillation while the variation in  $\beta$  is caused by the variations in the DC link conditions : V,  $I_D$ ,  $V_D$ . As the rotor oscillation are assumed to be small, the system can be considered to be operating under quasi-steady state conditions. Therefore, the system of differential equations describing this mode of operation can be written in term of the ' time varying effective value' of the concerned variables. Accordingly, the initial conditions for these equations at each time interval can be obtained with the help of the complexor phasor diagram of Figure 2 taking into considration the variaions gained in both  $\beta$  and  $\delta$  from the corresponding differential equation.

# 2.1 DERIVATION OF THE BASIC EQUATIONS

TS =

In addition to the above mentioned assumption, the following assumptions are also considered to develop the differential equations:

- 1- Saturation is neglected in the synchronous compensator. Thus the machine is assumed to operate in the linear part of the magnetisation curve, In this case, the excitation voltage control is proportional to the field control.
- 2- Higher harmonics are neglected. The first harmonic is only taken into consideration. This assumption is valid for both the compensator and the inverter.
- 3- The electrical load is assumed to be passive and balanced load. This assumption enables to represent the system by its phase equivalent circuit.
- 4- Damper-winding parameters are referred to the stator-side. Induction in the field-circuit as well as the saliency-effect are neglected.
- 5- The inverter-thyristor units are assumed to possess ideal resistances in both forward and reverse directions. Also, it is assumed that there is no effect of the commutation on the rectangular shape of the inverter current.
- 6- The smoothing-reactor is assumed to be a proper one and is enough to eliminate the ripples in both the DC voltage and current.

The above assumptions are practically reasonable as the system is operating under quasi-steady conditions.

So, the differentional equations representing the system can be given now:

$$d(w_{\rm p} / w_{\rm o}) / dt = a (TS + TAS - TD)$$
(1)

$$d(\mathbf{\beta} + \mathbf{\delta})/dt = w_0(1 - w_0/w_0) \tag{2}$$

$$d(I_D)/dt = V_D/L_D - I_D R_D/L_D - (3.N/L_D) V.cos \beta$$
 (3)

The first equation is derived mainly with the help of the dynamic equation of the synchronous compensator which relates the electric developed synchronous torque, TS, to all other torques exerted inside the machine;

$$TS = TI + TD - TAS$$
(4)

$$(V. E_{f}.sin (\mathbf{5}+c)/Z_{S}-(E_{f}/Z_{S})^{2}.R_{S}).(p/w_{o})$$
 (4-a)

$$TI = J \cdot d(w_{n})/dt = (d(w_{n}/w_{n}) / dt) / a$$
 (4-b)

$$TD = TD_{o} \cdot (w_{o}/w_{o}) \tag{4-c}$$

TAS= 
$$(E.X_{S}/(X_{E}+X_{S}))^{2}/R_{K}.(p/w_{o}).(1-w_{p}/w_{o})$$
 (4-d)

Where  $R_K$  is damper resistance referred to stator side The synchronous torque,TS, depends mainly on the excitation voltage  $E_r$  and the load angle  $\delta$  which could be positive or negative under oscillating conditions. The inertia torque, TI, is a function, in the first derivative of  $(w_r/w_o)$ . The damping torque corresponds to the friction and windage losses inside the machine. It depends on the rotor relative speed where TD is the damping torque measured at synchronous speed w. The asynchronous torque TAS is exerted by the damper winding and depends on the air-gap voltage. It will be, accelerating torque for  $(w_r/w_o) < 1$ , positive slip, and it will be, retarding torque for  $(w_r/w_o) > 1$ , negative slip. It is also evident that under steady state for  $w_r=w_o$ , TS =TD as it is well known for compensator mode of synchronous machine operation. The second equation, eqn. 2, is derived by relating the variation  $\Delta(B + \delta)$  with the time, to both frequencies  $w_o$  and  $w_r$ . Equation 3 is developed from the DC-link mesh where  $V_D$  is given by

$$V_{\rm D} = I_{\rm D} \cdot R_{\rm D} + L_{\rm D} \cdot d(I_{\rm D})/dt + V'$$
 (5)

Where

$$= 3 . N . V . \cos B$$
 (6)

V is the inverter DC voltage

Equation 5 makes the necessary coupling between the compensator terminal voltage, which also the load terminal voltage and the DC-link variables, including the advance angle  $\beta$  of the inverter. Equation 3 forms a non-linear system. It can't be written in the form of a state equation. Therefore, the initial conditions for each time interval, while solving the system numerically by a fourth order Runge-Kutta's method, will be essential to continue the solution.

# 2.2 INITIAL CONDITIONS

<u>1-At the starting point, t =0</u>, we have the following initial conditions:

- $(\underline{i})$ Load : the load power (KVA), load power factor  $\cos \varphi_{\ell}$  and its type whether lagging or leading, and the rated terminal voltage, V, of the compensator or the inverter.
- (ii) Inverter: the impulse frequency which determines the load or compensator frequency. This frequency remains constant. In addition, the initial value of the advance angle  $\beta$  of the inverter must be known. This angle must be greater than the expected commutation angle and too far less than  $\pi/2$ .
- (iii)Compensator: the rated mechanical losses are measured at the synchronous speed, w<sub>o</sub>, which determines the rated damping torque TD. In addition, the ratio of the total active power to the apperent power (kw/kva) at rated excitation must be known.

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Accordingly to the mentioned principle of power balance, and the complexor phasor diagram shown in Fig. 2, the following equations can be written:

$$I_{\rm S} \cdot \sin \varphi_{\rm S} = I_{\rm N} \cdot \sin \beta - I_{\rm L} \cdot \sin \varphi_{\ell}$$
 (7-a)

$$I_{S} \cdot \cos \varphi_{s} = I_{N} \cdot \cos \beta - I_{L} \cdot \cos \varphi_{\ell}$$
 (7-b)

$$E_{f} \cdot \cos \mathbf{\delta} = V - I_{S} \cdot Z_{S} \cdot \cos (\mathbf{\varphi}_{S} + \Theta_{S})$$
(8-a)

$$E_{f} \cdot \sin \boldsymbol{S} = I_{S} \cdot Z_{S} \cdot \sin (\boldsymbol{\varphi}_{S} + \boldsymbol{\theta}_{S})$$
 (8-b)

The manipulation with the above conditions and the equations 7 and 8 give the initial values of all AC voltages and currents and the corresponding phase shifts referred to the terminal voltage V. The voltage E can be obtained with equations similar to that written for  $E_f$ . On the DC side, the currentI<sub>D</sub>can be determined by

$$I_{D} = I_{N} / N \tag{9}$$

The steady-state form of equation 5 yields the initial value of the voltage behind the DC link. Now with the help of the equation 4 and for an initial value of (w /w ), equation 3 is ready to start the solution. <u>2- Initial conditions for any instant t > 0</u>

The determination of these conditions depends on the results gained at the previous interval :  $(\beta + \delta)_{n-1}$ ,  $(w_r/w_o)_{n-1}$ , and  $(I_D)_{n-1}$ ;

where n is the interval order. To get the rest of the initial conditions included in the differential equations, the separation between  $\beta$  and  $\boldsymbol{5}$  must be processed taking into considration the relation :

 $(I_N)_{n-1} = N \cdot (I_D)_{n-1}$  (10) This separation is directed by the applied approach and depends in turn on its variables.

#### 2.3 SOLUTION ALGORITHM

It follows now the salient directions and manipulation required for the separation process. It will be noticed that  $\varphi_{\ell}$  is assumed to be constant in all three approaches :

#### 2.3.1 First Approach

This approach doesn't consider the application of any control concepts.This result in :

 $V_D$  = constant and  $(E_f)_{n-1} = E_{fo} \cdot (w_n / w_0)_{n-1}$ 

Although the excitation isn't controlled, its voltage  $(E_f)_{n-1}$  differs from that calculated at t =0,  $E_{fo}$ , by the rotor relative speed So, substituting

 $(\boldsymbol{\delta})_{n-1} = (\boldsymbol{\beta} + \boldsymbol{\delta})_{n-1} - (\boldsymbol{\beta})_{n-1},$ The following variables can be declared as knowns while manipulating with equations 7 and 8 :  $(V_D, I_N, \boldsymbol{\varphi}, \boldsymbol{\epsilon}_f, \boldsymbol{\delta})_{n-1}$ The manipulation yields the following results. Mansoura Bulletin Vol. 10, No.1, June 1985

$$\boldsymbol{\beta} = \operatorname{Arc} \operatorname{Tan} \left( \left( \frac{K_1}{K_2} \right) \right)$$

Where

$$\begin{aligned} \mathbf{K}_{1} = \sin (\mathbf{\beta} + \mathbf{\delta}) - A\mathbf{K}_{2} \cdot \mathbf{I}_{D} - A\mathbf{K}_{3} \cdot \cos (\mathbf{B} + \mathbf{\delta}) - A\mathbf{K}_{1} \cdot A\mathbf{K}_{3} \cdot \mathbf{I}_{D} \\ \mathbf{K}_{2} = \cos (\mathbf{\beta} + \mathbf{\delta}) + A\mathbf{K}_{1} \cdot \mathbf{I}_{D} + A\mathbf{K}_{3} \cdot \sin (\mathbf{\beta} + \mathbf{\delta}) - A\mathbf{K}_{2} \cdot A\mathbf{K}_{3} \cdot \mathbf{I}_{D} \\ A\mathbf{K}_{1} = \mathbf{N} \cdot \mathbf{R}_{S} / \mathbf{E}_{f} \\ A\mathbf{K}_{2} = \mathbf{N} \cdot \mathbf{X}_{S} / \mathbf{E}_{f} \\ A\mathbf{K}_{3} = -A\mathbf{K}_{4} / A\mathbf{K}_{5} \\ A\mathbf{K}_{4} = (\mathbf{R}_{S} \cdot \sin \mathbf{g}_{2} + \mathbf{X}_{S} \cdot \cos \mathbf{g}_{2}) / \mathbf{Z}_{L} \\ A\mathbf{K}_{5} = 1 + (\mathbf{R}_{S} \cdot \cos \mathbf{g}_{2} - \mathbf{X}_{S} \cdot \sin \mathbf{g}_{2}) / \mathbf{Z}_{L} \\ Having \mathbf{\beta} \text{ and } \mathbf{\delta} \text{, the terminal voltage can be determined as:} \end{aligned}$$

$$V = (E_{f} \cdot \cos \boldsymbol{\delta} + K_{3} \cdot I_{D}) / K_{4}$$
(12)  
Where  
$$K_{3} = (R_{S} \cdot \cos \boldsymbol{\beta} - X_{S} \cdot \sin \boldsymbol{\beta}) \cdot N$$
  
$$K_{4} = AK_{5}$$

2.3.2 Second Approach

An excitation control is applied, here, to hold the constraint of having the terminal voltage V to be constant. The manipulation with eqns. 7 and 8 in this case implies that

 $\boldsymbol{\beta}_{n-1} = (\boldsymbol{\beta} + \boldsymbol{\delta})_{n-1} - \boldsymbol{\delta}_{n-1}$ 

So, the following variables can be declared as knowns :

$$\begin{array}{c} (v_D, \ \mathrm{I}_N, \ v_o, \ \mathrm{I}_L \ , \beta, \ \varphi_\ell \ )_{n-1} \\ \text{Accordingly , the $\boldmathcal{S}$ relation can be derived as} \end{array}$$

a. 
$$\sin^2 \boldsymbol{\delta} + b$$
.  $\sin \boldsymbol{\delta} + c = 0$  (13)

Its solution yields

$$\begin{aligned}
Sin &= (-b \stackrel{+}{=} \sqrt{b^2 - 4.a.c}) / 2a & (14) \\
a &= (-R_S, I_L, Sin \mathcal{G} - X_S, I_L, Cos \mathcal{G})^2 \\
&+ (V_o - X_S, I_L, Sin, \mathcal{G}) + R_S, I_L, Cos \mathcal{G} )^2
\end{aligned}$$

Where

$$b = -2.N.I_{D}.(R_{S}.Sin(\beta+\delta) + X_{S}.Cos(\beta+\delta))$$

$$\cdot (V_{o} - X_{S}.I_{L}.Sinq_{\ell} + R_{S}.I_{L}.Cosq_{\ell})$$

$$c = (N.I_{D})^{2}.(R_{S}.Sin(\beta+\delta) + X_{S}.Cos(\beta+\delta)^{2})$$

$$-(-R_{S}.I_{L}.Sinq_{\ell} - X_{S}.I_{L}.Cosq_{\ell})^{2}$$

Equation 14 gives two values for  $\sin \delta$ . Accordingly, two values in turn for the angle will be obtained . The acceptable value of  $\delta$  is to have the smallest value.

# 2.3.3. Third Approach

Here, the control of  $V_D$  is applied as well as the excitation control to hold the advance angle of the inverter and the terminal voltage, respectively be constant at their initial values at t = 0 (i.e.  $\beta_0$  and V ). Therefore, the load angle  $\delta_{n-1}$  can be directly determined where  $\rho_{n-1} = B_0$ 

$$\mathbf{5}_{n-1} = (\mathbf{B} + \mathbf{5})_{n-1} - \mathbf{B}_{n-1}$$

And eqns. variables ( $V_0$ ,  $I_L$ , , B, )<sub>n-1</sub> can be stated as knowns

Applying eqns. 7 and 8 ,a relation of the inverter current can be obtained  $\sim$ 

$$(1_N)_{n-1} = C_1 \cdot V_0 / (C_2 + C_3 \cdot \tan \delta)$$
 (15)

Where

$$C_{1} = A/Z_{L} + (1 + \beta/Z_{L}) \cdot \tan \delta$$

$$C_{2} = R_{S} \cdot \sin \beta + X_{S} \cdot \cos \beta$$

$$C_{3} = R_{S} \cdot \cos \beta - X_{S} \cdot \sin \beta$$

$$A = R_{S} \cdot \sin \varphi_{\ell} + X_{S} \cdot \cos \varphi_{\ell}$$

 $B = R_{S} \cos \varphi_{\ell} - X_{S} \sin \varphi_{\ell}$ 

Having  ${\rm I}_{\rm N},$  the current in the DC-link can be given by:

$$(I_D)_{n-1} = (I_N)_{n-1} / N$$

And the controlled voltage can be deduced by :

$$(V_D)_{n-1} = 3$$
, N.V<sub>o</sub> cos  $\beta$  +  $R_D I_D$  +  $[(I_D)_{n-1} - (I_D)_{n-2}] L_D / T_D$  (16)

So, accordingly to the approach applied the rest of the initial conditions required per solution progress can be decided.

# 3. PROGRAM ORGANIZATION

The proposed mathematical model had been written in the form of FORTRAN program for the mini-computer installed in the Electrical Engineering Department of EL-Mansoura University. The criteria being applied to the results of each time interval will be discussed in the following section. Most of these criteria are suggested to stop the calculations when the system shows tendency to one of the following kinds of instability:

(a) Load Angle  $\delta \gg \pi/2$ 

This criterion indicates that the synchronous compensator is going out of stability.

(b) <u>Negative-current in the DC-link</u>

This condition occurs when  $V > V_D$  in the first approach .Negative current in the DC-link can't actually be happened because of the nature of the inverter as long as  $\beta < \pi/2$ . In this case  $I_D$  will stop to flow and the calculations will be continued by  $I_D = 0$ 

- (c) <u>Advanced Angle βλ π/2</u> It will be indicated ,here, the advance angle β is going above its upper limit. This means that the inverter has to reverse the power flow. Naturally, this can't be happened, where the DC-link is the only source for active power.
- (d) Advance Angle B≤T To achive this criterion , the commutation angle T must be firstly determined, (6):

$$\mathbf{\tilde{0}}$$
 = Arc cos (1-2.  $X'_{S}$ .  $I_{D} / (\sqrt{6} V)$ ) (17)

The physical concepts of the inverter show that the advance angle  $\beta$  must be greater than  $\mathcal{T}$ . If  $\beta \leq \mathcal{T}$ , an inverter failure will give alarm.

The model had been tested using the following data : (a) <u>Load</u>

KVA = 4, V = 220 Volt , f = 50 Hz, P.F. = 0.8 lag.

(b) Synchronous Compensator

KVA = 5.23 P.F = 0.15 leading P<sub>f+w</sub> = 600 Watt, R<sub>S</sub> = 0.33 , X<sub>P</sub> = 0.66 X<sub>S</sub> = 5.3 , X<sub>S</sub> = 0.55 Ohm, R<sub>K</sub> = 0.15 , and X<sub>E</sub> = 0.0 Ohm and J = 0.308 Kg.m<sup>2</sup>.

(c) <u>Inverter and DC -link</u>  $\beta_0 = 36^\circ$ ,  $R_D = 0.25$  Ohm and  $L_D = 200$  mh.

# 4. RESULTS

Fig. 3 indicates the behaviour of the DC current  $I_D$  resulting on applying the three approaches. The behaviour of a group of other variables such as  $\beta$ ,  $\gamma$ , ( $\varphi_s + \delta$ ), V,  $I_S$ , ( $w_r/w_r$ ), ( $w_r/w_r$ ), and ( $w_s/w_r$ ), of the first approach only are given in Fig. 4. The first approach, which does not apply any type of control, show unstable

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operation. The DC-link current increases in an oscillatory manner with diverging envelope to give an inverter failure at advance angle  $\beta$  less than the commutation angle. The angle  $(\mathcal{P}_{3} + \mathbf{5})$ , Fig. 4 indicates the mode of operation of the synchronous machine while it is oscillating around w<sub>0</sub>. At moments, at which  $(\mathcal{P}_{3} + \mathbf{5}) = \pi/2$ , the machine will act as ideal compensator and doesn't exert the synchronous torque. For  $(\mathcal{F}_{3} + \mathbf{5})$  less or greater than  $\pi/2$ , the machine will act as a motor or generator, respectively. In this case, TS will be positive or negative, consequently. It is evident that V and I<sub>S</sub> are also oscillating with ascending exponential envelop. The relative speeds  $(w_{1}/w_{2})$ ,  $(w_{2}/w_{2})$  and  $(w_{2}/w_{2})$  show the variation in speed of the corresponding variables : E<sup>6</sup>, V and I<sub>S</sub>, respectively. Either of them is pulsating with a different speed and manner with respect to the rigid reference w<sub>2</sub>. In accordance with the results of the second and third approache Fig 4 shows the behaviour of I<sub>D</sub> which is also oscillating with converging envelope to reach its steady value in few milli-seconds. It is a also evident that I<sub>D</sub> resulting from the third approach reaches its steady value sooner than that resulting from the second approach. Changes in other variables aren't remarkable.

#### 5. CONCLUSION

Quasi-steady behaviour of a system consisting of a synchronous compensator in conjunction with a rigidly impulsed inverter supplying an isolated load had been formulated through an adequate mathematical model The model gives three approaches for solving such problem. The first approach doesn't consider any control concepts ,the second approach considers the excitation control, while the third one considers the excitation and DC voltage behind the DC link controls . Application of the mathematical model to a system having a conventional compensator shows the necessity of continous excitation control , else the system will go out of stability or has an inverter failure. The application of continuous control of both excitation voltage and the voltage behind the DC-. link results in quick stable operation. The mathematical model gives the opportunity to have an optimum dimensioning of each element in the system.

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