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Effect of Nature of the Surface of the Condensate Film on Condensation Heat Transfer.

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EFFECT OF NATURE OF THE SURFACE OF THE CONDENSATE FILM ON CONDENSATION HEAT TRANSFER

Bу

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ABSTRACT- This paper is concerned with the investigation of the effect of the nature of the surface of the condenste film on heat transfer during laminar film condensation. An idealized rippled nature of the film surface is proposed. Local heat transfer coefficients are calculated for film condensation on a vertical plate in laminar case. Calculations are performed numerically. For the proposed rippled nature of the film surface, the average heat transfer coefficients are up to 20% higher than that obtained for smooth surface.

INTRODUCTION

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Design of total or partial condensers for single vapor or multicomponent mixture is one of the important problems in the field of thermal and chemical engineering.

Laminar film condensation has been described and analyzed by Nusselt [1,2] under several simplifying assumptions such as :

1- acceleration effects in the liquid film are ignored;

2- linear temperature distribution in the film is assumed ;

3- energy effect of liquid subcooling is not included.

Nusselt analysis has been later improved by many investigators to account for the above mentioned effects. Also, boundary layer analysis has been applied to film condensation. Boundary layer analysis improves the accurcy of the representation of the film condensation process by including convection terms in the liquid layer.

In many circumstances, actual transfer rates are substantially higher than predicted ones [2]. These discrepancies have been explained to arise mainly because the behaviour of the actual film differs from that assumed. Many actual films flow in a rippled manner [4,5]. These ripples often arise because of such disturbances as uneven, though small, vapor velocities or as a result of condensate drainage from higher surfaces. The effect of this rippled structure is to increase the heat transfer rate. Considering Fig. 1, The sensible heat flux q_g from the bulk M. 78 M.Mahgoub

of gas phase is given by :

$$q_{g} = h_{g} (t_{g} - t_{s}), \dots (1)$$

where h_g is the dry gas heat transfer coefficient, which is generally evaluated as if the gas phase were flowing alone [3]. The local overall heat transfer coefficient U, defined by

$$q_t = U(t_g - t_w) = h_f(t_s - t_w)$$
. ... (2)
ven by

is then given by

 $(1/U) = (1/h_f) + q_g/h_g q_t, \qquad ...(3)$

where q, is the total heat flux and h is the condensate film heat transfer coefficient.

To determine the dry gas heat transfer coefficient, there are many correlations which give acceptable values for laminar and tubulent flow of gas phase [1,2]. Such correlations apply to smooth surface. Wall roughness, which increases pressure loss by promoting momentum transfer, also increases heat transfer. Nunner, 1956 carried out extensive tests on air in tubes whose inside surfaces were artificially roughened [2]. It was found that the Nusselt number for the roughened wall is a function of the flow Reynolds number and of the ratio of the actual friction factor and the friction factor for smooth-wall flow at the same Reynolds number as shown in Fig. 2 and expressed by the following relation [4]:

where f_0 is the friction factor obtained from Blassius equation for smooth surface $f_0 = (100 \text{ Re})^{-0.25}$...(5)

Now, in the process of film condensation, the surface of the condensate film builds the tube wall, whose structure effects the heat transfer process. This effect may be compared with the effect of the surface roughness with two main differences :

I- The condensate has a velocity relative to the vapor phase; and

2- the ripple characteristics are not constant along the way of flow.

To determine the friction factor f (Eq.4) due to the roughness of the condensate film, Hempel developed the following correlation [4]:

 $f = f_0 [1 + 17.2 (b_f / d_i)^{0.9}]$

...(6)

where b_{f} is film thickness, di is the tube inside diameter, and f is the friction factor for smooth surface.

FILM HEAT TRANSFER WITH PARTIALLY ACTUAL FILM SURFACE

Consider a flat plate of length L whose exposed face is at uniform temperature t and which is inclined at an angle with the horizontal. Fig. 3 illusturates a proposed idealized actual film surface, which can be expressed in the following relation :

$$y_{py} = y_{y} (1.0 - f \sin(2\pi x / p)),$$

...(7)

where x is the distance along the plate in the direction of flow, f is a factor less than unity, and p_x is the peiod of the wave. In Eq. (7), y_x is the mean thickness

of the condensate film evaluated on the basis of Nusselt theory for laminar film condensation and is given by

$$y_{x} = \left[\frac{4 \text{ k } \mu \left(t_{v} - t_{w}\right)}{\beta \left(\beta - \beta_{v}\right) \text{ g } h_{fg}} \sin \phi \right]^{1/4} \left[x\right]^{1/4} \qquad \dots (3)$$

According to Nusselt theory, the local heat transfer coefficient h, is given by :

$$h_{x} = k/y_{x} = \left[\frac{g(g-f_{y})k^{3}g}{4\mu(t_{y}-t_{w})}\right]^{1/4} (1/x)^{1/4} \dots (9)$$

To calculate the actual heat transfer coefficient h structure one substitutes in Eq. (9) for y_{ax} instead of y_{x}^{ax} .

The average actual heat transfer coefficient h_a for the plate of length L is given by :

$$h_{a} = (1/L) \int (k/y_{ax}) dx = (k/L) \int \frac{dx}{y_{x}(1 - f \sin(2\pi x/p))}$$

Since y is function of $x^{1/4}$, the above integration can be performed only numerically. In the present work, numerical integration is performed using the trapezoidal rule. On the other hand, the integration can be performed analytically for $\xi = 0$ (smooth surface), the result is given by :

$$h = 0.943 \left[\frac{f(f - f_v) k^3 g h_{fg} \sin \varphi}{L \mu (t_v - t_v)} \right]^{1/4} = 3/4 h_L \qquad \dots (11)$$

To investigate the effect of the proposed actual surface structure described by Eq. (7), condensation over a 1 ft high vertical plate is considered, whose surface is maintained at 71 C. Vapor phase is steam at 0.52 bar and condenses in a filmwise manner. The following property information is used :

$$t_v = 82 \text{ C} , \quad t_w = 71 \text{ C} , \qquad k = 670 \times 10^{-3} \text{ W/m degree} \\ h_{fg} = 2303 \text{ Kj/kg} \qquad \qquad \mu = 3510 \times 10^{-7} \text{ kg/m sec.} \\ S = 970.5 \text{ kg/m}^3 \qquad \qquad g = 9.81 \text{ m/sec}^2 .$$

In this analysis, liquid properties are assumed to be independent on the temperature.

RESULTS AND DISCUSSION

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Analytical solution of the problem obtained according to N sselt theory for smooth surface (f = 0.0) give the results which are plotted in Fig. 4. The figure illusturates the behaviour of the local heat transfer coefficient h and the local condensate film thickness y along the plate. According to the figure, the minimum heat transfer coefficient occurs when x is maximum, that is when x = L. The minimum heat transfer coefficient is 5960 W/m² C. The average heat transfer coefficient for smooth film surface given by Eq. (11) is 7948 W/m² C.

On the other hand, Fig. 5 illusturates the effect of the actual film surface on the behaviour of the film thickness and heat transfer for certain surface parameters- f = 0.2 and p = 1/3 (the wave is repeated 3 times). It is clear that

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the local film thickness y object the function x $1/4 \sin (2\pi x/p)$, which means local thinning or thickening of the film. Local heat transfer coefficient ($h_{\alpha,x} = k/y_{\alpha,x}$) has also a wave character.

Most noticeable is the value of the actual average heat transfer coefficient h. The predicted value of h for f = 0.2 and p = 1/3 is 8220 W/m² C, which is 3.2% higher than that obtained for smooth surface (h = 7962 W/m² C) by the same numerical technique. For the same f (0.2) and if p = 1 (one wave over the length of the plate), the predicted value of h is 8282 W/m²C, which is 4% higher than that for smooth surface. This result is physically acceptable because as p increases the film surface becomes more flat (Fig. 6).

When p = 1 and $\xi = 0.5$, the predicted value of the actual average heat transfer coefficient h is 9582 W/m²C, which is approximatlly more than 20% higher than that obtained for smooth surface. It is concluded that the parameter is more effective than the parameter p. Predicted values of the actual average coefficients for different surface parameters are listed in the table below. In the extereme case, where $\xi = 0.9$, the average heat transfer rates approaches the value of 19465 W/m²C, which is in the order of heat transfer coefficients in case of dropwise condensation.

E	1/3	1/2	1
0.0	7962	7962	7962
0.1	8055	8061	8084
0.2	8220	8242	8282
0.5	9424	9480	9582
0.9	19040	19139	19465

Table : Average heat transfer coefficients for different actual surface parameters, W/m²C.

CONCLUSION

In filmwise condensation, actual heat transfer rates are substantially higher than predicted ones. One reason for this descrepancy is the actual surface of the condensate film. Actual films flow in a rippled manner, whose effect on the dry gas heat transfer is compared with the surface roughness. The effect of the actual surface on the film heat transfer is to increases the average coefficients up to 20% higher than coefficients for smooth film surface.

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NOMENCLATURE

ср	specific heat
r S h h fg	friction factor gravitational acceleration heat transfer coefficient latent heat
k ^δ L q t x y, δ _f	thermal conductivity of liquid phase plate length heat flux temperature distance along the plate thickness of the condensate film
ל,p אש Re Pr Nu	film surface parameters vescosity density angle of inclination Reynolds number Prandtle number Nusselt number

Subscripts

я

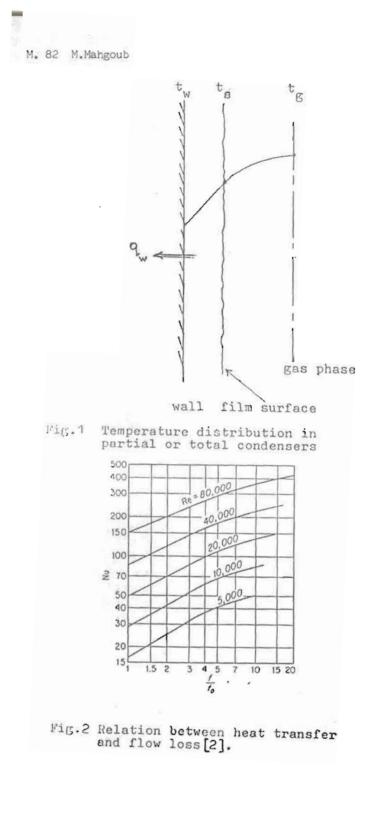
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a	actual
v,g	vapor
w	wall
f	film

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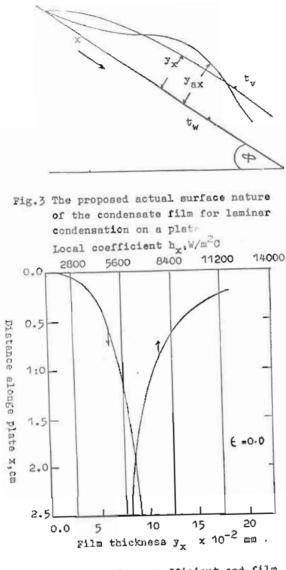
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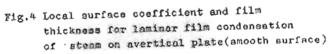


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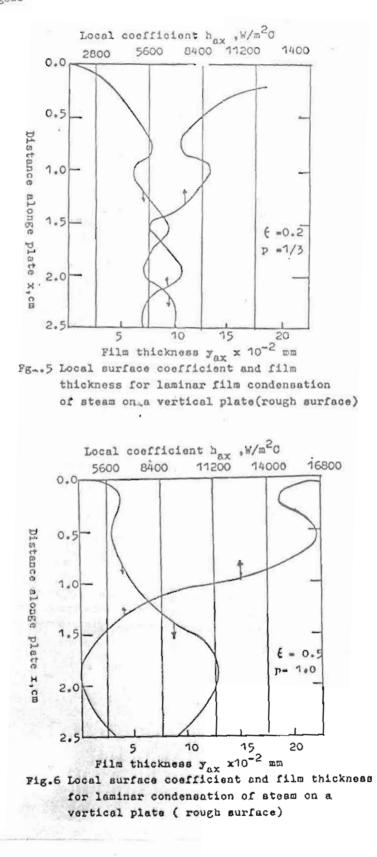
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COMPUTER ROLE FOR DETERMINATION OF FILM COOLING EFFECTIVENESS OF AN AEROFOIL MODEL

BY

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دور الحاسب الآلى في ايجـاد معامل التبريد الغشـائى لنموزج ايروفويـل خلاصه: يقدم هذا البحث برنامج حاسب آلى لايجـاد معامل التبريد الغشـائى لنموزج "ايروفويـل" وطريقة التبريد المتبعة في هذه الحـالة هى بحقن المبرد منخلال صفوف انابيب عند مقدمة حافة نموزج ايروفويل وتتم في وجود وعدم وجود تدرج ضغطى • وقد اجريت الدراسـة لحالتى الحقن العمود ى والماسى للسطح وكذلك لظروف زاوية هبوب موجبة وسـالبه وزاوية صفـر • بواسطة هـفذا البرنامج يمكن حساب معامل للتبريد التبريد الغشـائى في زمن اقل منعشر ثوان • والنتائج التى حصل عليها من الحاسب بينت توافقا مرضيا مع النتائج التى حصل عليها من التجارب المعطيه في البحوث السابقة النشر لمعامل النبريـد الغشـائى للحالات السابقة الذكر •

ABSTRACT - This work presents a FORTRAN computer program for the analysis of film cooling effectiveness of an aerofoil model. The procedure of cooling is by injecting the coolant through a row of tubes at the leading edge of the aerofoil model. The study is carried out for two cases of normal and tangential injection and for zero, positive, and negative attack angle.

The data analysis carried shows satisfactory agreement with experimental results on film cooling effectiveness obtained in previous studies.

NOMENCLATURE

Cf	skin friction coefficient without injection	
CDC	specific heat at constant pressure,	J/(kg.K)
^c f ^c pc ^c P C D	specific heat at constant pressure for main air stream.	J/(kg.K)
C D	surface pressure coefficient; (p-p_)/0.5.9.u2	
D	diameter of injection holes.	mm
F.C.F.C. h	full coverage film cooling heat transfer coefficient,	w/m ² .K
	= (k/x) S _D .Re _x . $(c_{1}/2)^{0.5}$	
k	thermal conductivity,	W/m.K
L	chord length of the aerofoil model,	N/m ²
Ps	static pressure,	2
р М	surface pressure,	N/m.2
M	blowing ratio or blowing parameter; pc.uc/o.u	
m	mass flow rate.	kg/s
Nu	Nusselt number; $(h.x/k) = \operatorname{Re}_{x} (c_{1}/2)^{0.5}$.Sp	0
Pr	Prandtl number;	

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Rex	Reynolds number (ug.x/ダ)
St	Stanton number; (N_u/Re_x) .Pr)
t	temperature,
taw	adiabatic wall temperature,
u	local velocity,
х	distance in streamwise direction,
х	dimensionless distance = x/L
GREEK	LETTERS
2	film cooling effectiveness; $(t_w - t_{ac}) / (t_c - t_w)$

			abi-lanaa.	
boundary	layer	displacement	thickness;	$=\int_{\Omega} (1 - \frac{u}{u}) dy,$
			boundary layer thickness, boundary layer displacement	boundary layer thickness, boundary layer displacement thickness;

τ shear stress.

density, g

dynamic viscosity, μ v kinematic viscosity,

SUBSCRIPTS AND INDICES

с injectant total t wall w

main stream œ

1- INTRODUCTION

Film cooling technique is widely used in many systems to protect solid surfaces exposed to high temperature gas streams. The coolant injected in the boundary layer acts as a heat sink, reducing the gas temperature near the surface. Applications are numerous, particularly in gas turbine systems [1:6] where combustion chamber flame tubes, turbine blades, and other hot parts of the engine used air, usually taken from the exit of engine compressor, for film coolant.

°C °č m/s mm

mm mm N/m^2

kg/m³

N.s/m² m²/s

In the leading edge region of a turbine blade there is often a very high surface heat transfer. In this region, film cooling has found widespread use in maintaining suitable skin temperatures.

With film cooling, a coolant is injected locally through the wall in such a way that it creates a film along the surface, thereby protecting the wall from exposure to a hot gas stream. The study is carried out for two cases of normal and tangential injection and for zero, positive and negative attack angle [19, 20].

The major part of the present work is to simplify the determination of film cooling effectiveness using a computer program specially designed for this purpose in the light of several analytical studies [7:14].

The program output agreed well with the present experimental results for an aerofoil model.

The experimental study [21] has been conducted in low-speed, open circuit wind tunnel. A detailed description of the wind tunnel, air injection system is given elsewhere [19:21]. Table 1 shows the range of test conditions as given in [21].

Table 1 EXPERIMENTAL RANGE AS GIVEN IN [21]

a set and the set of the	Construction of the Carl Street Carl	the second se
MAIN STREAM VELOCITY,	υ _æ	20 m.s
MAIN STREAM TEMPERATURE ADJACENT TO THE LEADING EDGE,	T _{eo}	330 K
TEMPERATURE OF INJECTANT AIR,	Т _с	300 K
BLOWING RATE,	M	0.2
	and the second se	Co. N. BURLAUT

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2- AU, ROXIMATE ANALYSIS OF FILM COOLING EFFECTIVENESS

Several authors [2, 9, 10] derived expressions for the temperatures distributions in the boundary layer and for the cooling effectiveness of the hot surfaces. In [2, 10:12] experimental data have been correlated with equations similar to the analytical expressions derived in [2]. In [9,10] the influence of specific heat of both the media has been taken into consideration and assuming a fully developed turbulent boundary layer, the following equation has been drived

$$\gamma = \frac{1.9 \text{ Pr}^{2/3}}{1.0 + 0.329 \text{ B}^{0.8} \frac{c_{\text{pm}}}{c_{\text{pc}}}} \cdot \beta$$

where

$$3 = (\frac{\mu_{\rm C}}{\mu_{\rm m}} \cdot {\rm Re}_{\rm C})^{-0.25} \cdot \frac{{\rm X}}{[{\rm m}.{\rm B}]}$$

 β takes into consideration the influence of blowing angle.

Tribus and Klein [12], acting upon a sugges ion of Eckert, considered the secondary fluid as a line heat source at the wall. The magnitude of the source depended on the mass flow, temperature, specific heat, etc., of the injectant fluid. They use Duhamet's theorem to predict the film cooling effectiveness to be:

$$\gamma = \frac{5.77 \text{ Pr}^{2/3}}{(\text{cp}_{o}/\text{cp}_{c}) \cdot (\mu_{o}/\mu_{c})^{0.2}} \cdot x^{0.8}$$
(2)

where

$$X = \frac{x}{M.h} \cdot Re_{h}^{-0.25} = \frac{x}{M.h} \cdot (\frac{U_{C,h}}{\nu_{c}})^{-0.25}$$
 with h slot height, and

 $\gamma = (T_w - T_w) / (T_c - T_w)$

Later prediction by Librizzi [14] and Kutateladze [13] also considered the secondary fluid as a heat source, they assumed the mainstream and coolant fluid in the boundary layer to be completely mixed. In both of these analysis the actual mass of secondary fluid is assumed to be added to the boundary layer which then grows as a normal turbulent layer on a flat plate. They suggested a heat balance to get the mean boundary layer temperature.

$$\underset{w}{\mathsf{m}} \overset{c}{\mathsf{r}}_{p_{ap}} \overset{T}{\underset{\infty}{\mathsf{m}}} \overset{c}{\mathsf{r}}_{p_{ap}} \overset{c}{\underset{\alpha}{\mathsf{m}}} \overset{r}{\underset{\alpha}{\mathsf{m}}} \overset{m}{\underset{\alpha}{\mathsf{r}}} \overset{c}{\underset{\alpha}{\mathsf{r}}} \overset{r}{\underset{\alpha}{\mathsf{m}}} \overset{m}{\underset{\alpha}{\mathsf{c}}} \overset{c}{\underset{pc}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{\alpha}{\mathsf{c}}} \overset{c}{\underset{pc}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{\alpha}{\mathsf{c}}} \overset{c}{\underset{pc}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{\alpha}{\mathsf{c}}} \overset{r}{\underset{pc}{\mathsf{r}}} \overset{m}{\underset{w}{\mathsf{m}}} \overset{r}{\underset{w}{\mathsf{c}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{m}{\underset{w}{\mathsf{m}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{m}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{r}{\underset{w}{\mathsf{r}}} \overset{m}{\underset{w}{\mathsf{r}}} \overset{m}{\underset{w}{}} \overset{m}{} \overset{m}{\underset{w}{}} \overset{m}{\underset{w}{}} \overset{m}{\underset{w}{}} \overset{m}{} \overset{m}}{} \overset{m}{} \overset{m}{} \overset{m}{} \overset{m}{} \overset{m}{}$$

or

Since m_c is measured and c_{pos} and c_{pc} are known, the problem reduces to a prediction of the mass flow in the boundary layer which comes from the mainstream, m_c

In view of **Goldstein** and **Haji-Sheikh** [15,16], the mass flowing within the boundary layer is considered to be composed of two different fluids from two different spreams. One is the mass injected per unit time which is completely contained within the boundary layer, mo The other is the mass which enters the boundary layer from the mains tream per unit time, m. The total mass per unit time in the boundary layer that passes any position is thus

$$m = m_{\omega} + m_{c} \tag{5}$$

Consider \hat{T} as the bulk temperature of the fluid contained within the boundary layer, \hat{T}_{co} as the temperature of the free stream and T_{C} is the temperature of the coolant at the point of injection a heat balance [14] yields the relation

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(1)

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$$(\tilde{\mathbf{T}} - \mathbf{T}_{\mathbf{\omega}}) / (\mathbf{T}_{\mathbf{c}} - \mathbf{T}_{\mathbf{\omega}}) = (\mathbf{m}_{\mathbf{c}} \cdot \mathbf{c}_{\mathbf{pc}}) / (\mathbf{m}_{\mathbf{c}} \cdot \mathbf{c}_{\mathbf{pc}} + \mathbf{m}_{\mathbf{\omega}} \cdot \mathbf{c}_{\mathbf{p}\omega})$$
(6)

Librizzi [14] assumed T to be the wall temperature and m_{∞} to be the mass contained in the boundary layer in the absence of mass injection. According to the definition of \vec{T} , one can write

$$(\bar{T} - T_{\omega}) = \frac{\int_{0}^{\infty} \rho \cdot c_{p} \cdot u \cdot (T - T_{\omega}) dy}{\int_{0}^{\infty} \rho \cdot c_{p} \cdot u \cdot dy}$$
(7)

In order to obtain the bulk temperature, both a temperature profile and a velocity profile must be considered. Downstream from the point of injection, one may assume that the velocity profile is governed by the power law

 $\left(\frac{u}{u_{\infty}}\right) = \left(\frac{y}{\delta}\right)^{n}$, with $n = \frac{1}{n}$

Assume the temperature profile to be similar, one can write

$$(\mathbf{T} - \mathbf{T}_{\omega}) = (\mathbf{T}_{w} - \mathbf{T}_{\omega}) \mathbf{G}(-\frac{\mathbf{y}}{\mathbf{\delta}_{T}})$$
(8)

where

$$S_{T} = \int_{0}^{\infty} \frac{T - T_{co}}{T_{w} - T_{co}} dy$$
(9)

Assuming that the product $oc_p = oc_p$ does not vary greatly in the y direction, one obtains;

$$\overline{\mathbf{r}} - T_{\alpha \alpha} = \frac{0}{\int_{0}^{\infty} c_{p} \cdot c_{p} \cdot u (\mathbf{T} - T_{\alpha}) dy}{\int_{0}^{\infty} c_{p} \cdot \rho \cdot u \cdot dy}$$

Divide both sides by (T - T):

$$\frac{\overline{T} - T_{\infty}}{T_{w} - T_{\infty}} = \frac{1}{(T_{w} - T_{\infty})} \cdot \frac{9 \cdot c_{p_{0}} \int^{\infty} u \cdot (T - \underline{T}) dy}{9 \cdot c_{p_{0}} \int^{\infty} u \cdot dy}$$

$$= \frac{0^{\int_{0}^{\infty} (y/\delta)^{n}} G(y/\delta T) dy}{\int_{0}^{\delta} \frac{(y)^{n}}{(\delta)^{n}} G(y/\delta T) dy}$$

$$= \frac{0^{\int_{0}^{\delta} \frac{(y)^{n}}{(\delta)^{n}} G(y/\delta)^{n}} G(y/\delta)^{n} G(y/\delta)^{n}}{\int_{0}^{\delta} \frac{(y/\delta)^{n}}{(\delta)^{n}} G(y/\delta)^{n}} \frac{(y/\delta)^{n}}{(\delta)^{n}} G(y/\delta)^{n} G(y/\delta)^{n}}$$

.

A

$$=\frac{1}{6} \begin{pmatrix} 0 \\ n + 1 \end{pmatrix} (\begin{pmatrix} 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 2 \\ 2 \end{pmatrix})$$

Making use with $\delta_{\rm T}$ to perform ${\rm I}_1$ and ${\rm I}_2$ to have the following form :

$$\mathbf{I}_{1} = \delta_{T} \left(\delta_{T} / \delta \right)^{\hat{n}} \cdot \int_{(y/\delta_{T})}^{(\frac{y}{\delta_{T}}) = \left(\delta / \delta_{T} \right)} (y/\delta_{T})^{\hat{n}} \cdot \mathbf{G}(y/\delta_{T}) \cdot \mathbf{d}(y/\delta_{T})$$

ж

'n

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Also,

$$(y/\delta_{T}) = \infty$$

$$I_{2} = \delta_{T} \int_{(y/\delta_{T})} G(\delta/\delta_{T}), d(y/\delta_{T})$$

$$(y/\delta_{T}) = (\frac{\delta}{\delta_{T}})$$

$$\begin{split} &\tilde{\mathbf{T}} - \mathbf{T}_{\infty} \\ &\tilde{\mathbf{T}}_{w}^{-} \tilde{\mathbf{T}}_{\infty}^{-} = (\mathring{\mathbf{n}} + 1) \frac{1}{\delta} \left[\left(\begin{array}{c} \delta_{\mathrm{T}} & \mathring{\mathbf{n}} + 1 \\ -\delta_{\mathrm{C}} \end{array} \right)^{-1} \int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \cdot \mathbf{d}(\frac{y}{\delta_{\mathrm{T}}}) + \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \cdot \mathbf{d}(\frac{y}{\delta_{\mathrm{T}}}) + \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \cdot \mathbf{d}(\frac{y}{\delta_{\mathrm{T}}}) + \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \cdot \mathbf{d}(\frac{y}{\delta_{\mathrm{T}}}) + \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}{c} \frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^{-1} \cdot \mathbf{G}(\frac{y}{\delta_{\mathrm{T}}}) \\ &\int_{0}^{\langle \delta_{\mathrm{T}}} \left(\begin{array}(\frac{y}{\delta_{\mathrm{T}}} \end{array} \right)^$$

Finally, substitution of $(\bar{T} - T_{\infty})$ in equation (6) yields:

$$\frac{T_{w} - T_{\infty}}{T_{c} - T_{\infty}} = \frac{1/\lambda}{1 + \frac{p_{\infty}}{c_{pc}} \cdot m_{c}}$$
(11)

The turbulent boundary layer on a flat plate has a velocity distribution:

$$\left(\frac{u}{u_{\infty}}\right) = (y/\delta)^{1/n}$$
 (12)

As reported by Schlichting [17], the turbulent shear stress is given by:

$$\frac{\tau_{\rm w}}{\rho u^2} = 0.0225 \left[\frac{y}{u_{\infty} \cdot \delta} \right]^{0.25}$$
(13)

and the momentum equation:

$$\frac{\tau_{w}}{\rho \cdot u_{\infty}^{2}} = \frac{d}{dx} \int_{0}^{0} \frac{u}{u_{\infty}} \left(1 - \frac{u}{u_{\infty}}\right) dy$$
(14)

Substituting equations (12), (13) into equation (14) leads to:

$$\frac{\delta}{x} = \left[\frac{0.0225}{K}\right]^{0.8} (Re_x)^{-0.2}$$
(15)

where

$$K = -(17n)^{-1} + -(27n)^{-1} + -1$$

$$m_{ec} = \int_{0}^{0} 0 \cdot u \cdot dy ; m_{c} = 0 \cdot u_{c} \cdot \bar{h}$$

and

In the light of Weighardt [10] analysis, $G(y/\delta_T)$ may be taken as

EXP -C2 (y/6 T) 2+n

where

$$C_2 = [\Gamma[\frac{n+3}{n+2}]]^{n+2}$$

Reffering back to equations (10), (11)

$$\lambda = (\mathbf{\hat{n}}+1) \left[(\delta_{T} / \delta)^{\mathbf{\hat{n}}+1} \int_{0}^{\delta/\delta_{T}} (y/\delta_{T})^{\mathbf{\hat{n}}} \cdot G(y/\delta_{T}) \cdot d(y/\delta_{T}) + (\delta_{T}/\delta) \int_{\delta'/\delta_{T}}^{\infty} G(y/\delta_{T}) \cdot d(y/\delta_{T}) \right]$$

6)

The next item describes a computer program for marching all calculations of film cooling effectiveness.

3- FORTRAN PROGRAM FOR CALCULATING FILM COOLING EFFECTIVENESS

A FORTRAN computer program called 'MTØ' has been developed that calculates the film cooling effectiveness during a short running time (less than ten seconds).

STRUCTURE OF THE PROGRAM

Program 'MTØ' consists of a driver program and three subroutine:

I- SUBROUTINE SIM 2- SUBROUTINE BMW 3- SUBROUTINE FUN

The driver program sets all the boundary conditions and the input data; streamwise distance, mainstream velocity and temperature, injectant fluid velocity and temperature, injection hole geometery, physical properties of the fluids App. A.

The driver program and the subroutines has been diagramed and listed in App.B&C. PROGRAM DESCRIPTION:

The first part of the driver program (statement 5 : statement 19) sets up the input data.

Statement 20: statement 38, Gama function estimation according to Stirling's expansion [18] which leads to:

$$\Gamma(z) = e^{-z} z^{z-0.5} \sqrt{2\pi} \left[1 + \frac{1}{12z} + \frac{1}{288z^2} - \frac{139}{51840z^3} + \frac{571}{2488320z^4} + (z^{-5}) \right]$$

Statement 49 : statement 56, estimating of integration 'Ii' .

Statement 57 : statement 66, estimating of integration 42° . Statement 67 : end of the driver programm, contains the final results of the film colling parameter and the film colling effectiveness. Mansoura Engineering Journal (MEJ) Vol. 12, No. 1, June 1987

PROGRAM OUTPUT: Sample of the results is shown in App.D.			
DESCRIPTION OF	PARAMETERS		
DH CP UMF UMC RF RC UF (II) UC REX DELTA EETA EETA EM (JI) X (II) AN (I)	injection hole diameter specific heat mainstream viscosity coolant viscosity mainstream density coolant density mainstream velocity coolant velocity coolant velocity Reynolds number boundary layer thickness film cooling effectiveness blowing ratio streamwise distance (= EN) = $n = 1/n$ film cooling parameter, (λ) n = 1/n Gama function, (λ) G (y/ δ) C ₂ - (ln G(y/ δ)) /C ₂ y/ δ_T l ₁ l ₂		

4- CONCLUDING REMARKS

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Comparison between theoretically obtained results, in the form of film cooling effectiveness, and the experimental results for the aerofoil model are shown in figures l(a,b,c) and 2.

For zero pressure gradient, tangential injection gives higher values of film cooling effectiveness than normal injection for x/L < 0.3 in both experimental and present program results. For x/L higher than 0.3, experimental film cooling effectiveness increases for the normal injection than tangential injection as shown in figure 1a. These results agree with the visualization photographs which indicate the effective region of the cooling film delayed a distance nearly 3-diameters downstream the injection hole [22].

For negative pressure gradient both normal and tangential injection give lower values for the film cooling effectiveness than the case of zero pressure gradient due to the deceleration of the flow and the separation effects (Fig. 1b). Comparison between experimental results and present program results for tangential injection indicate similar slope curves but lower values of film cooling effectiveness in the region of x/L = 0.45 in the case of present program results.

In the case of positive pressure gradient the film cooling effectiveness increases at the leading edge than for the case of zero pressure gradient for experimental and theoretical results in the case of tangential injection, than gradually decreases downstream x/L = 0.3(Fig. 1c).

Also, the present program gives more accurate results than uses the flat plate model as shown in figure 2. This is due to taking into consideration the change in mainstream velocity across the chordwise direction.

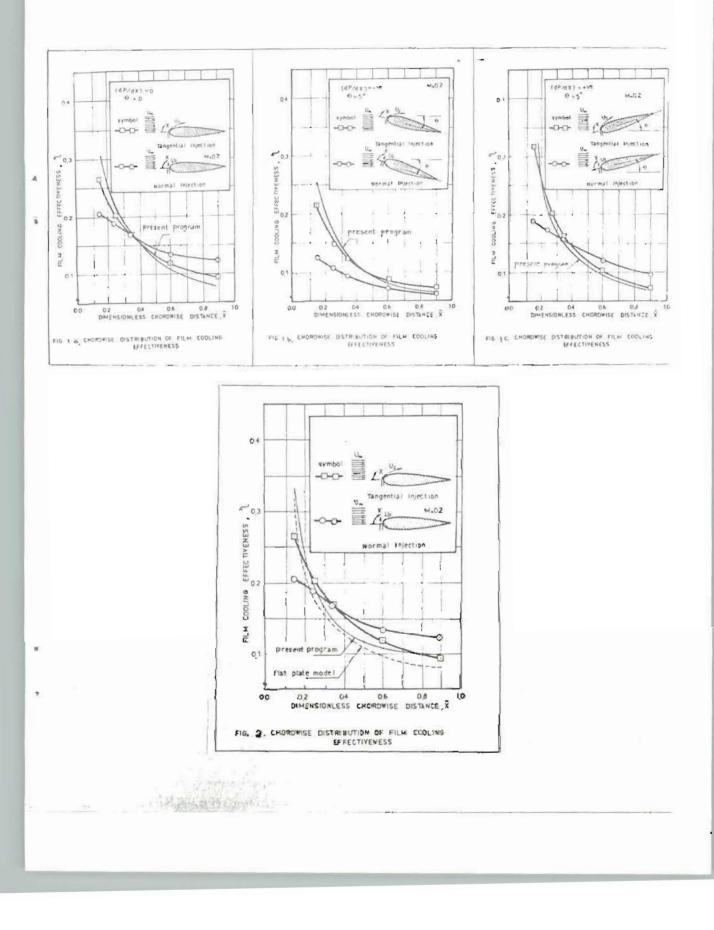
M. 91

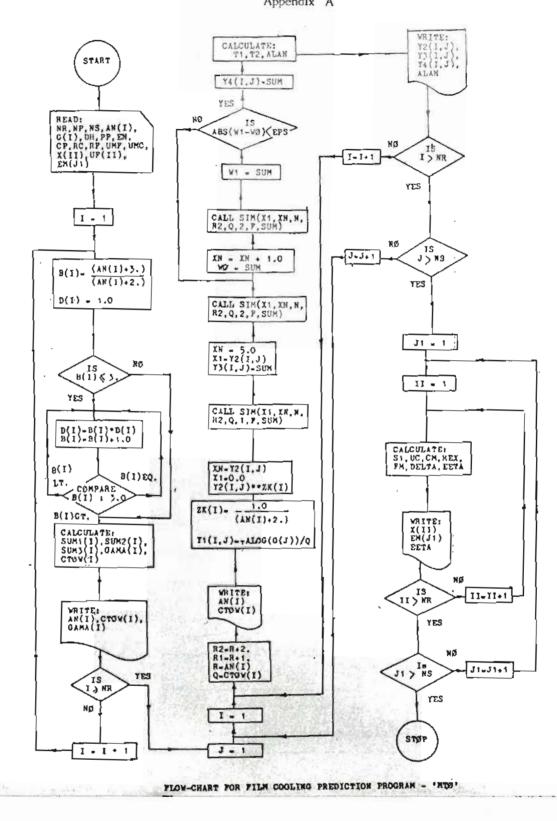
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Appendix A

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Appendix	B
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1		SUBROUTINE SIN(X1, XN, N, R2, Q, M, P, SUN)	•
2		DIMENSION 7(400)	
3		N1-R+1	
4		H-(IN-I)/H	
5		DO 3 K-1, N1	
6		I1-X-1	SUBROUTINE SIN(11.1N. H. R2.
7		1-11+11=8	Q, H, 7, SUX)
8		IF(K.EQ.1)60 TO 10	\
9		CALL BHY(X, 82, 0, 1, 7)	1
10		CO TO 3	N)=S+)
11	10	CALL FUR(X, R2, Q, X, P)	B-(XX-X1)/8
12	,	CONTINUE	x-1
13		SUMO=0.0	 ,
14		SUKE-0.0	1 3 - X - 1
15		DO 4 K=2,8,2	X=X1+ 11=H
16	4	SUHO-SUHO+P(K)	1
17		86-8-1	KO IS TES
18		DO 5 K-3, N6, 2	× [*] , > ⁺ [*]
19	5	SUME-SUME-P(X)	
20		SUH_H*(P(1)+P(N1)+4	
21		*SUMP+2. *SDNE)/3.	BAW PUN
22		RETURN	
23		D אנז	15 YES
			<x 23="" <="" [i-x-1]-<="" n1="" td=""></x>
			NO
			SUMD-0.0
			SUME-0.0
			X-3

SUME-SUME-P(K) SUM-R*(P(1)+P(N1)+4.* SUMD+2.SUME)/). 15 K & N6 N0 YES K.K+2 RETURN

FLOWCHART FOR SUBROUTINE 'SIM(X1, 1N, N, R2, Q, K, 7, SUN)'.

.

1	SUBROUTINE FUN(X,R2,Q,X,F)
2	DINENSION F(400)
3	Y(X)-0.0
4	SS-EXP(-Q*(I**R2))
5	F(K)_(X**(#2-2))*SS
6	RETURN
7	EN D

SUBROUTINE BAY(K,R2,Q,X,7)

DIMENSION F(400)

7(1)-EXP(-Q*(1**82))

F(T)-0.0

RETURN

EN D

1 2

3 4

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Appendix C

¢		FILM COOLING PREDICTION PROCRAM - 'HTO'	51		ZX(I)=1./(AM(I)+2.)
1		DINENSION AN(10), B(10), SUM1(10), SUM2(10), SUM3(10),	52		Y2(1,J)**2X(I)
2		*D(10), GAMA(10), CTOY(10), G(10), C(10), Y1(10, 10),	53	,	11-0.0
3		*ZK(10), 72(10,10), 73(10,10), 7(400), 74(10,10), UP(10),			IN- 72(I, J)
¢		* 2x(10), 1(20)	55		CALL SIM(X1, IN, N. RZ, Q, 1, F, SUM)
5		N = 200	56		T3(1,J)=SUM
6		EPS = 0.000001	57		I1-12(I.J)
7		PI = 3.141592653	58		IN-5.0
8		PA = SQRT(2.=PI)	59		CALL SIM(X1, XN, N, R2, 0, 2, F, SUM)
9		VRITE(2,200)	60	101	WO.SUR.
10		VRITE(2,201)	61		XN=XN+1.0
11		VRITE(2,200)	62		CALL SIM(X1, XM, N, R2, 0, 2, P, SUM)
12		READ(1,4) HR, NP, NS	63		VI-SUM
13		READ(1,8)(AN(1),I=1,WR)	64		IF (ABS (W1-W3), LE, EPS) GB 10 100
		READ(1,9)(G(I), I=1, WR)	65		GO TO 101
14			66		14(1,J)=SUM
15		READ(1,5)DH, PP, EN, CP, RC	67	100	
16		READ(1,6)RF, UMF, UMC			$T_1=R_1*((1, /Y_2(I, J))*R_1)*Y_3(I, J)$
17		READ(1,7)(X(II), II=1, NS)	68		T2=R1=(1./T2(I,J))=Y4(I,J)
18		READ(1,7)(UP(II), II=1, NS)	69		ALAN=11+72
19		READ(1,30)(EM(J1),J1=1,NP)	70		WRITE(2,205)Y2(1,J),Y3(1,J),Y4(1,J), ALAN
50		DO 10 I.I., WR	71	16	CONTINUE
21		B(I)=(AW(I)+3.)/(AW(I)+2.)	72	10.00	WRITE(2,200)
22		D(I)=1.0	73	15	CONTINUE
23		IF(B(I).GT.3.)GP TO 11	74		D3 106 J1=1, NS
24	12	D(I)=B(I)=D(I)	75		DO 105 II-1,NR
25		B(1) = B(1) + 1.0	76		S1=0.2242*DH
56		IP(B(I)-3.)12,12,11	77		UC-EN(J1)*(RF*UF(I1))/RC
27	11	SUN1(I)=1.+1./(12.*B(I)+1./(288.*B(I)*	78		CM_RC*S1*UC
28		•B(I))-139./(51840.*(B(I)**3.))-571./	79		REX_RF*UF(II)*X(II)/UKF
29		*(2488320.*(B(1)**4.))	80		DELTA-X(II)=0.37/REX=*0.2
30		SUM2(1)=1./EIP(B(I))	81.		FM_RF=UP(II)=DELTA/(EN+1.)
31		C(I)=B(I)-0.5	82		EETA-CH*CP/(0.56*PM)
32		SUN3(I)=B(I)=*C(I)	83		WRITE(2,36)1(11), EN(J1), EETA
33		GAMA(I)=(SUM2(I)*SUM3(I)*PI*	84		CONTINUE
34		<pre>sum1(1))/D(1)</pre>	85	106	
35		ANN=AN(I)+2. CTSY(I)=CAMA(I)**ANN	86	4	
36			87		FORMAT(5(77.4,1X)) FORMAT(P4.2,2X,2(F9.7,2X))
37		WRITE(2,202)AN(I), CTGV(I), CAMA(I)	89		PORMAT(5(P6.3,21))
38	10	CONTINUE	90		PORMAT(6(P4.2,2X))
39		VRITE(2,200)	91		PORMAT(6(P5.3,2X))
40		DO 15 I-1, WR	92	· · ·	PORMAT(3(PB.4,2X))
41		Q-CT3V(1)	93		PORMAT(5(75.3,2X))
42		R=AX(I)	94		PORMAT(BO(1H=))
43		R1=R+1.0	05		PORMAT(21, "N", 71, 'C2', 81, 'GAMA')
44		R2=R+2.0	30	202	PORMAT(P5.3,2(1X,P10.5))
45		VRITE(2,203)AN(1),CTOW(1)	97	203	PORMAT(2X, "N", P5.3, 2X, 'C2. ', P10.5)
46		VRITE(2,200)	97	204	PORMAT(1%, 'Y/DELTA', 2%, 'INTEGRAL 1', 2%,
47		VRITE(2,204)	99	204	"INTEGRAL 2', 5X, 'LANDA')
48	1.1	VRITE(2,200)	100	205	PORMAT(4(F10.5.2X))
49		DO 16 J.1. WR Y1(1,J)ALOC(G(J))/Q	101	203	STOP
50		11(1,0)=-ALGO(0(0))/0	102		DND
		manual a Cartan a lan and a langung and a sub-	102		

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10.00 Table

Appendix D

SAMPLE OF THE OUT PUT RESULTS OF'MTØ'.

¥	C2	DAMA	
0,120	0.77302	0.88565	
0.140	0.77109	0.88562	
0.150	0.77014	0.88561	
0,160	0.76919	0.88560	
0.180	0.76733	0.88561	
0.200	0.76550	0,88562	
	A CONTRACTOR OF		
I-0.12	0 C2=0.7	7302	
		***************	******
T/DELTA	INTEGRAL 1	INTEGRAL 2	LAN DA
2.32055	0.90373		0.39532
2.08998	and the second second		0.44454
1.89455	0.89219	5.53 C.5.55	0.49623
1,76894	0.88394		0.53583
1.67339	0,87514		0.57015
1.59483	0,86586	0.03796	0,60160
	AN TOTAL CONTRACTOR OF A	******************	
N=0.14			
********		***************	
Y/DELTA	and the second se		LANDA
2.30506		A COLUMN	0.39286
2.,07806	Charles and an and an and an		0.44220
1.88547	DATAMENTY - ALLENAN DA	and the second second	0.49405
1.76160	0.87068	0.02053	0.53380
1.66730			0.56826
1.58975	0.85264		0.59905
¥-0.16			
Y/DELTA	INTEGRAL 1		LANDA
and the second se	and the second second second	*******	
2.20992	0.87769		0.39047
		0.00579	0.43991
2.06639			
1.87657	0.86609	0,01268	0.49192
1.87657	0.86609	0,01268	0.49192 0.53181
1.87657	0.86609 0.85786 0.84910	0,01268 0,02023 0,02833	0.49192 0.53181 0.56641
1.87657 1.75438 1.66132 1.58474	0.86609 0.85786 0.84910 0.83986	0,01268 0,02023 0,02833 0,03692	0.49192 0.53181
1.87657 1.75438 1.66132	0.86609 0.85786 0.84910 0.83986	0,01268 0,02023 0,02833 0,03692	0.49192 0.53181 0.56641
1.87657 1.75438 1.66132 1.58474	0.86609 0.85786 0.84910 0.83986	0,01268 0,02023 0,02833 0,03692	0.49192 0.53181 0.56641
1.87657 1.75438 1.66132 1.58474	0.86609 0.85786 0.84910 0.83986	0,01268 0,02023 0,02833 0,03692	0.49192 0.53181 0.56641
1.87657 1.75438 1.66132 1.58474 M=0.18 T/DELTA	0.86609 0.85786 0.84510 0.83986 0 C2-0.7 IN2ECRAL	0,01268 0,02023 0,02833 0,03692 6733	0.49192 0.53181 0.56641 0.59813 LANDA
1.87657 1.75438 1.66132 1.58474 N=0.18 T/DELTA 2.27510	0.86609 0.85786 0.84510 0.83986 0 C2-0.7 UN2EGRAL	0,01268 0,02023 0,02833 0,03692 6733 1 INTEGRAL 2 0,00206	0.49192 0.53181 0.56641 0.59813 LANDA 0.38815
1.87657 1.75438 1.66132 1.58474 N=0.18 T/DELTA 2.27510 2.05496	0.86609 0.85786 0.84510 0.83986 0 C2-0.7 UN2ECRAL 0.96529 0.86124	0,01268 0,02023 0,02833 0,03692 6733 1 INTEGRAL 2 0,00206 0,00570	0.49192 0.53181 0.56641 0.59813 LANDA 0.38813 0.43768
1.87657 1.75438 1.66132 1.58474 N=0.18 Y/DELTA 2.27510 2.05496 1.86784	0.86609 0.85786 0.84910 0.83986 0 C2-0.7 INTEGRAL 0.86529 0.86124 0.85368	0,01268 0,02023 0.02833 0.03692 6733 1 INTEGRAL 2 0.00206 0,00570 0,01249	0.49192 0.53181 0.56641 0.59813 LANDA 0.38813 0.43768 0.48984
1.87657 1.75438 1.66132 1.58474 M-0.18 T/DELTA 2.27510 2.05496	0.86609 0.85786 0.84510 0.83986 0 C2-0.7 UN2ECRAL 0.96529 0.86124	0,01268 0,02023 0.02833 0.03692 6733 1 INTEGRAL 2 0.00206 0,00570 0,01249	0.49192 0.53181 0.56641 0.59813 LANDA 0.38813 0.43768

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