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# Numerical Simulation of Flows in an Engine Cylinder with an Eccentric Deep Bowl Combustion Chamber during Compression (1st Report, Formulation and Algorithm).

# M. El-Kady

Mechanical Power Engineering Department, Faculty of Engineering, Mansoura University, Mansoura, Egypt., mselkady@mum.mans.eun.eg

#### H. Mascheck

Professor of Institute of Fluid Mechanics, Technical University of Dresden, Germany (GDR).

# A. Hoche

Professor and head of the institute of I.C.E., Technical University of Dresden, Germany (GDR)

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NUMERICAL SIMULATION OF FLOWS IN AN ENGINE CYLINDER WITH AN ECCENTRIC DEEP BOWL COMBUSTION CHAMBER DURING COMPRESSION (1st Report, FORMULATION AND ALGORITHM)

محاكاه عددية للسربان داخل اسطوانة دات غرفة احتراق غبر مركزية في المكبس خلال شوط الانضفاط ( التقربر الاوْل : التكوين والصودج العــــددي ) <sup>‡</sup>

Ву

M.S. El Kady<sup>1</sup>, H.J. Mascheck<sup>2</sup> and A. Hoche<sup>3</sup>

الخلاصة \_ هذا البحث عصره خطوة أخرى في نفدهم نموذج عددى وطريقة عددية لاستنب اط حركة الفاز في اسطوانة محرك ترددى ، في المرجع ( ۱ ) تم دراسة حركة الفاز فيني غرفة احتراق مركزية مع محور الاسطوانة ، أما في هذا البحث فقد تم انحراف غرفية الاحتراق لتكون غير مركزية ووضعت المعادلات التي تميع حركة الغاز الفير مستقللي الاحتراق لتكون غير مركزية ووضعت المعادلات التي تميع حركة الغاز الفير مستقللات خلائي الاثباد خلال شوط الانفغاط ، وباستخدام طريقة الرسم المتوافق تم اختبار نظام احداثيات خاص تكون فيه الفتحة العير مركزية بها مركزية مع محور الاسطوانة وسعللي ذلك وباستخدام طريقة النرحاف ثم مفكوك فورس للمتغيرات تحولت المشكلة من ثلاثبية الأبعاد الى مجموعة من المتحركات العددية استخدمت طريق فيروق المحدودة واستخدم فيها نظام المشبكة المتحركات العددية استخدمت طريق الفير صريح وذلك لعملية تمحيح الففط بواسطة التكليدرار ، وقد ممم برنامج كوم وتر لمياغة حركة الغاز ثلاثية الأبعاد الغير مستكرة داحسل السطوانة ذات غرفة احبران عميقة غير مركزية خلال شوط الانفعاط ، وفي المرجع ( ١١ ) م استخدام هذا البرنامج في مشال عددي على احدى ماكينات الدين المفيرة وعبيدر في المتهادة وحراستها النتائج ودراستهادا .

#### ABSTRACT

This paper describes another step in the numerical simulation of the in-cylinder gas flow in the real reciprocating engine cylinder. The deep bowl combustion chamber in the piston which is axisymmetric in [1] is shifted here to be eccentric to the cylinder axis and the three dimensional unsteady air motion during the compression stroke is predicted. By the use of the conformal mapping a special coordinate system is chosen in order to make the eccentric bowl axisymmetric, then by the use of the perturbation method and Fourier expansion for the dependent variables the three dimensional problem is transferred to a group of two-dimensional problems which are bounded together. Predictions were carried out using a finite difference method to solve the

1. Mech. Power Dept., Faculty of Engineering, Mansoura University

Professor, Institute of Fluid Mechanics, Technical University of Dresden, Germany (GDR)

Professor and head of the institute of I.C.E., Technical University of Dresden, Germany (GDR)

governing differential equations for continuity and momentum. A movable grid system is employed and the alternating direction implicit method (ADI) was used for the pressure correction. A computer program system EBSTR was developed for this case. In the second report numerical computation is made for a typical case and the results are discussed briefly [11].

# 1. INTRODUCTION

The investigation of the gas flows in the cylinder of the internal combustion engine is one of the most important ways to realize low pollution and high combustion efficiency. Since the incylinder flows are in a very complicated three dimensional turbulent state, there are many barries to reveal the flow only by experimental study. Therefore, recently the method of flow analysis by a computer has been developed. So far, however, most of the flow analysis have been performed on the axisymmetric or two dimensional flows [1]-[7].

The aim of this study is to simulate numerically the three-dimensional flow of the eccentric deep bowl combustion chamber of the direct injection diesel engine during the compression stroke. This is another step in approach to the gas flow in the real-cylinder of the four stroke engines by making the deep bowl in piston which is axisymmetric in [1] eccentric to the cylinder axis. This part of the paper describes the formulation of the problem and the method of the numerical analysis, while the second part [11] gives the results of sample calculation for a typical small direct injection diesel engine.

#### 2. MATHEMATICAL MODEL

#### 2.1. Coordinate system

A special coordinate system  $(R,\theta,z)$  is chosen in which the eccentric deep bowl combustion chamber will be axisymmetric, this will make the boundary conditions easy to be handled and also the discretisation error will be very near to zero. The cylinder wall and also the bowl wall will have constant radial values  $R_{\rm c}$ =const. This will be done by the conformal mapping as shown in Fig. 1-3. The zero point of this coordinate system does not coincide with the center of the bowl or the center of the cylinder as shown in figures 2 and 3 but it lies at the symmetrical plane at  $x = -\frac{R}{2}$  where  $\frac{R}{2}$  is an eccentric parameter which is assumed to be small. As the eccentric parameter  $\frac{R}{2}$  tends to be zero the bowl axis tends to coincide with the cylinder axis and also with the  $\frac{R}{2}$ -axis of the coordinate system  $\frac{R}{2}$ , and when  $\frac{R}{2}$ =0 the coordinate system  $\frac{R}{2}$ ,  $\frac{R}{2}$  will coincide with the normal cylindrical system. To do this, we define first in the z plane the complex variables  $\frac{R}{2}$ , as follows

$$w = x + iy$$
 and  $\xi = \xi + i\eta$ 

where  $\zeta = (v+\varepsilon)/(\varepsilon v+1)$  and the reciprocal  $v=(\zeta-\varepsilon)/(1-\xi\varepsilon)$ . In these planes the circle  $|\zeta|=1$  and  $|\zeta|^2=R_b^2$  in the  $\zeta$ -plane represent as shown in figure 2 the circles  $|\mathbf{v}|=1$  and  $|\mathbf{v}(\xi)+a|^2=R_b^2=$  constant in the w-plane. For these relations the variables £,R and  $\theta$  can be expressed as a function of a,x,  $r_b$  and y.

# 2.2 Governing equations

The fluid density is assumed to be spatially uniform over the flow field but time dependent. The true flow field inside real internal combustion engines might be reasonably modeled via a large inviscid core plus a very small viscous boundary layer at the walls, as conventially done in aerodynamics. Thus the inviscid flow is investigated here.

The governing equations will be the continuity and Euler equations. For the cartesian coordinate X,Y,z which will be oriented at every point due to the direction of the coordinates R= constant and  $\theta=$ constant as shown in Fig. 4 the differential equations will take, like in any cartesian coordinates, the form:

$$\frac{\partial U}{\partial t} + U \frac{\partial U}{\partial x} + V \frac{\partial U}{\partial y} + W \frac{\partial U}{\partial z} + \frac{\partial P}{\partial x} = 0$$

$$\frac{\partial V}{\partial t} + U \frac{\partial V}{\partial x} + V \frac{\partial V}{\partial y} + W \frac{\partial V}{\partial z} + \frac{\partial P}{\partial y} = 0$$

$$\frac{\partial W}{\partial t} + U \frac{\partial W}{\partial x} + V \frac{\partial W}{\partial y} + W \frac{\partial W}{\partial z} + \frac{\partial P}{\partial z} = 0$$

$$\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial W}{\partial z} + \frac{1}{2} \frac{dQ}{dt} = 0$$
(2)

where P is the pressure divided by the density

If  $\beta$  is the angle between the coordinate axis R=const. and X=const. as shown in Fig.4, the relation between the velocity components u,v,w in the coordinate system R, $\theta$ ,z and U, $\nabla$ , $\Psi$  in the coordinate system X,Y,z will take the form:

$$U = u \cos \theta - v \sin \theta$$
  
 $V = u \sin \theta + v \cos \theta$  (3)

Using equation (3) and the relations between the two coordinate systems the governing equations (1) and (2) can be transformed and written in the coordinate system  $R,\theta,z$  as follows:

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial R} - u \cdot v \cdot \frac{\partial B}{\partial R} + v \cdot \frac{x}{R} \cdot \frac{\partial u}{\partial \theta} - v^2 \cdot \frac{x}{R} \frac{\partial B}{\partial \theta} + w \frac{\partial u}{\partial z} + x \frac{\partial P}{\partial R} = 0$$

$$\frac{\partial v}{\partial t} + u \cdot x \left[ u \frac{\partial B}{\partial R} + \frac{\partial v}{\partial R} \right] + v \cdot \frac{x}{R} \left[ \frac{\partial v}{\partial \theta} + u \frac{\partial B}{\partial \theta} \right] + w \frac{\partial v}{\partial z} + \frac{x}{R} \frac{\partial P}{\partial \theta} = 0 \quad (4)$$

$$\frac{\partial w}{\partial t} + u \cdot x \cdot \frac{\partial w}{\partial R} + v \cdot \frac{x}{R} \frac{\partial w}{\partial \theta} + w \cdot \frac{\partial w}{\partial z} + \frac{\partial P}{\partial z} = 0$$

$$\frac{\partial u}{\partial R} + \frac{\chi}{R} \frac{\partial v}{\partial \theta} + \frac{\partial w}{\partial z} - v \cdot \chi \cdot \frac{\partial B}{\partial R} + \frac{1}{Q} \frac{\partial Q}{\partial t} = 0$$
where  $\chi = \frac{1 - 2 \, \epsilon \, R \, \cos \theta}{1 - \epsilon^2} + \frac{\epsilon^2 \, R^2}{1 - \epsilon^2}$ 

# 2.3 Integration area

Figures 1 and 4 show the integration area with its boundaries which consists of the axis, cylinder head, cylinder wall, piston crown, bowl wall and bowl bottom.

During the motion of the piston in a fixed z coordinate the boundaries of the integration area will vary with the time. To avoid an incomplete coverage of the wall boundaries in the computational grid which will be discussed in 3.2. a movable coordinate z' is used in the axial direction to make the boundaries of the integration area time independent where

$$z' = \frac{z}{h} c_1$$
  $0 \le z' \le c_1$ ,  $0 \le z \le h$   
 $z' = z + c_1 - h$   $c_1 \le z' \le c_1 + b_1$ ,  $h \le z \le h + b_1$ 

The governing equations will be transformed to the time movable coordinate system in which every point has an axial velocity in the cylinder, that is the same velocity of the grid point was in Fig.4. The time derivative for the movable coordinate will take the following form:

$$\frac{\partial}{\partial t}\Big|_{mov} = \frac{\partial}{\partial t}\Big|_{fixed} + w_g \frac{\partial}{\partial z}$$
 (3)

where 
$$w_g = \frac{z}{h} w_p$$
 for  $0 \le z \le h$   
and  $w_g = w_p$  for  $h \le z \le h + b_1$ 

This will change the governing equation (4) by only an excess derivative term in the convection form in the axial direction.

# 2.4 Governing equations by small accentricity of the bowl

Equations (4) will be solved by the perturbation method. Taking the eccentricity as a small perturbation parameter and restricting the solution on the linear terms of £, the velocity components u,v, w and the pressurte P can be written in the following form:

 $F(R,\theta,z) = F_0(R,z) + \xi F_1(R,\theta,z) \tag{6}$  The first term  $F_0(R,\theta)$  represents the independent term of  $\theta$  for the velocities u, v, v and the pressure P. This term casts

the symmetrical flow (the main flow). The second term  $F_1(R,\theta,z)$  represents the additional term which expresses the deviation of the flow from the symmetrical case (the disturbance term).

The additional terms for the velocities and the pressure which depend on  $\theta$  will be developed in Fourier series and restricted on the first harmonles of the coordinate  $\theta$ 

$${\rm FF}_1(R,\theta,z) = {\rm FF}_{10}(R,z) + {\rm FF}_{11}(R,z) \cos \theta + {\rm FF}_{12}(R,z) \sin \theta$$
 (7)

In this sequence the three dimensional variables  $F(R,\theta,z)$  are transformed to a group of two dimensional variables  $F_0$ ,  $F_{10}$ ,  $F_{11}$ ,  $F_{12}$  which are coupled together.

Making use of equations (5)-(7) in equation (4) and collecting only the coefficients of the zeroth and first order terms of and the coefficients of the first harmonies  $\cos \theta$  and  $\sin \theta$ , we get three groups of equations. Expressing the variables which have the form  $F_{11}$ ,  $F_{12}$  by the form  $F_{1}$  and  $F_{2}$  and to make the handling of these equations does not need very long discretising forms and many special forms in the numerical solution these three groups of equations will be expressed by using a number of operators for the special terms as follows:

$$\frac{\partial \vec{u}_{o}}{\partial t} = N_{o}(\vec{v}_{o}, m_{g}) - G_{o}P_{o}$$

$$\frac{\partial \vec{v}_{1}}{\partial t} = N_{1}(\vec{v}_{1}, \vec{v}_{o}, m_{g}) + M_{1}(\vec{v}_{2}, \vec{v}_{o}, P_{o}) - G_{o}P_{1} - G_{1}P_{2}$$

$$\frac{\partial \vec{v}_{2}}{\partial t} = N_{1}(\vec{v}_{2}, \vec{v}_{o}, m_{g}) + M_{2}(\vec{v}_{1}, \vec{v}_{o}) - G_{o}P_{2} + G_{1}P_{1}$$
(8)

and the continuity equations as follows:

The definitions of the convection operators N<sub>0</sub>, N<sub>1</sub>, M<sub>1</sub>, M<sub>2</sub>, the gradient operators G<sub>0</sub>, G<sub>1</sub> and the divergent operators D<sub>0</sub>, D<sub>1</sub> can be expressed by using  $\overline{\bf a}$ ,  $\overline{\bf u}$ , g, f for the vector and scalar quantities as follows:

$$N_{0}(\vec{u},g) = -u \frac{\partial \vec{u}}{\partial R} + (g-w) \frac{\partial \vec{u}}{\partial z} + \begin{bmatrix} v^{2}/R \\ -uv/R \\ 0 \end{bmatrix}$$
(10)

$$N_{1}(\vec{a}, \vec{u}, g) = -u \frac{\partial \vec{a}}{\partial R} + (g-w) \frac{\partial \vec{a}}{\partial z} - u \frac{\partial \vec{u}}{\partial R} - c \frac{\partial \vec{u}}{\partial z} + \begin{bmatrix} 2v.b/R \\ -(u.b+v.s)/R \end{bmatrix} (11)$$

$$M_{1}(\vec{a}, \vec{u}, f) = 2R u \frac{\partial \vec{u}}{\partial R} - \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} .2R. \frac{\partial f}{\partial R} - \frac{1}{R} v.\vec{a}$$
(12)

$$M_{2}(\vec{a}, \vec{u}) = \frac{1}{R} \cdot \vec{a} + 2 \begin{bmatrix} u \cdot v \\ -u^{2} \end{bmatrix}$$
(13)

$$O_0 \tilde{b} = \frac{1}{R} \frac{\partial (a.R)}{\partial R} + \frac{\partial (c.R)}{\partial z} \quad \text{and} \quad O_1 \tilde{b} = \frac{b}{R}$$
 (14)

$$G_{0}f = \begin{bmatrix} \frac{\partial f}{\partial R} \\ 0 \\ \frac{\partial f}{\partial z} \end{bmatrix}$$
 and  $G_{1}f = \begin{bmatrix} 0 \\ \frac{f}{R} \\ 0 \end{bmatrix}$  (15)

where 
$$\vec{a} = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$
 and  $\vec{u} = \begin{bmatrix} u \\ v \\ w \end{bmatrix}$ 

# 2.5 The Boundary and initial conditions

The boundary conditions express the global features of the in-cylinder flow, only special condition occurs at the axis. The velocities  $u_1$  and  $v_2$  and also  $u_2$  and  $v_1$  are coupled together in such a way to make the velocity contours smoothly flow along the axis. These boundary conditions are summarized as follows:

 $u_0=v_0=0$ ,  $u_1+v_2=0$ ,  $u_2+v_1=0$ ,  $w_1=v_2=0$ ,  $\partial w_0/\partial R=0$  at the axis  $u_0=u_1=u_2$  at the cylinder and bowl walls  $w_0=v_1=v_2$  at the cylinder top  $w_0=w_p$ ,  $w_1=v_2=0$  at the piston crown and bowl bottom  $\partial p_0/\partial n=0$  at all boundaries,  $p_1=p_2=0$  at the axis while  $\partial p_1/\partial n=\partial p_2/\partial n=0$  at all other boundaries, where n is the normal coordinate to the boundary.

The initial conditions are given to the quantities at the time of inlet valve closing as a forced vortex having a swirl ratio  $\omega_D$  which is assumed to be constant in the axial direction.

#### 3. SOLUTION ALGORITHM

#### 3.1 Method of solution

For the numerical time integration there are many methods, but to make the required computer capacity not very big the simplest explicit one direction forward method will be used and the value of the velocity vector  $\vec{u}_0$ ,  $\vec{u}_1$  and  $\vec{u}_2$  at the time t+8t is calculated from the velocity vectors  $\vec{u}_0$ ',  $\vec{u}_1$ ' and  $\vec{u}_2$ ' at the time t

$$\vec{u}_1 = \vec{u}_1' + \text{st} \ \partial \vec{u}_1 / \partial t$$
 (16)

 $\partial \tilde{u}_1/\partial t$  can be calculated only when the pressure is known. Beause the pressure is not known at first, the following algorithm will be used.

From the fact that the new  $\vec{u}_1$  at the time t+ $\delta$ t must satisfy the continuity equations (9), then by substituting  $\vec{u}_1$  in these equations it will take the following form

$$\begin{split} &D_{o}\vec{u}_{o} + \frac{1}{\varrho} \frac{d\varrho}{dt} = D_{o}(\vec{u}_{o}^{\prime} + \delta t \frac{\partial \vec{u}_{o}^{\prime}}{\partial t}) + \frac{1}{\varrho} \frac{d\varrho}{dt} = 0 \\ &D_{o}\vec{u}_{1} + D_{1}\vec{u}_{2} - 2R \frac{\partial u_{o}}{\partial R} = D_{o}[\vec{u}_{1}^{\prime} + \delta t \frac{\partial \vec{u}_{1}^{\prime}}{\partial t}] + D_{1}[\vec{u}_{2}^{\prime} + \delta t \frac{\partial \vec{u}_{2}^{\prime}}{\partial t}] - 2R \frac{\partial u_{o}^{\prime}}{\partial R} = 0 \\ &D_{o}\vec{u}_{2} - D_{1}\vec{u}_{1} - 2V_{o} = D_{o}[\vec{u}_{2}^{\prime} + \delta t \frac{\partial \vec{u}_{2}^{\prime}}{\partial t}] - D_{1}[\vec{u}_{1}^{\prime} + \delta t \frac{\partial \vec{u}_{1}^{\prime}}{\partial t}] - 2V_{o}^{\prime} = 0 \end{split}$$

Taking into consideration equation (16) and with the use of the relations

$$\vec{q}_{0} = \vec{u}_{0}' + \delta t N_{0}(\vec{u}_{0}', w_{g}')$$

$$\vec{q}_{1} = \vec{u}_{1}' + \delta t \left[N_{1}(\vec{u}_{1}', \vec{u}_{0}', w_{g}') + M_{1}(\vec{u}_{2}', \vec{u}_{0}', P_{0}')\right]$$

$$\vec{q}_{2} = \vec{u}_{2}' + \delta t \left[N_{1}(\vec{u}_{2}', \vec{u}_{0}', w_{g}') + M_{2}(\vec{u}_{1}', \vec{u}_{0}')\right]$$
(18)

for the convection term and also

$$po = st.Po$$
 ,  $pl = st.Pl$  and  $p2 = st.P2$  (19)

equation (17) will give for the pressure the following relations

$$D_{o}G_{o}P_{o} = D_{o}\overline{q}_{o} + \frac{1}{\varrho} \frac{d\varrho}{dt}$$

$$(D_{o}G_{o} - D_{1}G_{1}) P_{1} = D_{o}\overline{q}_{1} + D_{1}\overline{q}_{2} - 2R \frac{\partial \overline{u}_{o}}{\partial R}$$

$$(D_{o}G_{o} - D_{1}G_{1}) P_{2} = D_{o}\overline{q}_{2} - D_{1}\overline{q} - 2V_{o}$$
(20)

Equation (20) is an elliptic equation from Poisson's type and is used to calculate p by the known right hand side . This equation will be solved by iteration by using the ADI method [8]. By the calculated value of p the velocity  $\overline{\mathbf{u}}_i$  can be calculated by the equation (21).

$$\vec{u}_{0} = \vec{q}_{0} - G_{0}\rho_{0}$$

$$\vec{u}_{1} = \vec{q}_{1} - G_{0}\rho_{1} - G_{1}\rho_{2}$$

$$\vec{u}_{2} = \vec{q}_{2} - G_{0}\rho_{2} + G_{1}\rho_{1}$$
(21)

# 3.2 Diskretisation of the differential equations

For the discretisation of the governing equations two different two dimensional staggard grids in the way discussed by Stephens et al [9] are used for the vector and scalar variables as shown in Fig. 5. The crosses (+) represent the points of the grid  $\Omega_G$  for the vector field and the points (.) represent the point of the grid  $\widehat{\Omega}_G$  for the scalar field. The calculation of the convection terms and the pressure gradient will be at the points of the grid  $\widehat{\Omega}_G$  and the satisfaction of the continuity equation will be at the points of the grid  $\widehat{\Omega}_G$ . Variable axial spacing is used to allow for the change of the distance between the cylinder head and the piston crown, while a fixed grid system is used for the space in the piston bowl. The number of the axial nodes is varied during compression to avoid the exremely small spacing between it [1].

To express the discrete operation which are used in equations (17)-(21) without making many special forms, the following definitions will be taken into consideration

The convective operators  $N_0,\ N_1,\ M_1$  and  $M_2$  will take the following discrete forms

(27)

$$\left[ N_{0}(\vec{u}, w_{g}) \right]_{1,k} = \frac{1}{d_{R}} \left[ (u_{1,k})^{+}, (\vec{u}_{1-1,k} - \vec{u}_{1,k}) + (-u_{1,k})^{+}, (\vec{u}_{1+1,k} - \vec{u}_{1,k}) \right]$$

$$+ \frac{1}{d_{k-1}} \left( w_{1,k} - w_{gk} \right)^{+}, (\vec{u}_{1,k-1} - \vec{u}_{1,k}) + \frac{1}{R_{1}} \left[ v_{1,k}^{2} - v_{1,k}^{2} - v_{1,k}^{2} \right]$$

$$+ \frac{1}{d_{k}} \left( w_{gk} - w_{1,k} \right)^{+}, (\vec{u}_{1,k+1} - \vec{u}_{1,k}) + \frac{1}{R_{1}} \left[ v_{1,k}^{2} - v_{1,k}^{2} - v_{1,k}^{2} \right]$$

$$\left[ N_{1}(\vec{a}, \vec{u}, w_{g}) \right]_{1,k} = \frac{1}{d_{R}} \left[ (u_{1,k})^{+}, (\vec{a}_{1-1,k} - \vec{a}_{1,k}) + (-u_{1,k})^{+}, (\vec{a}_{1+1,k} - \vec{a}_{1,k}) \right]$$

$$+ \frac{1}{d_{k-1}} \left( w_{1,k} - w_{gk} \right)^{+}, (\vec{a}_{1,k-1} - \vec{a}_{1,k}) + \frac{1}{d_{k}} \left( w_{gk} - w_{1,k} \right)^{+}$$

$$\left( \vec{a}_{1,k+1} - \vec{a}_{1,k} \right) + \frac{a_{1,k}}{2 \cdot d_{R}} \left( \vec{u}_{1,k-1} - \vec{a}_{1,k} - \vec{u}_{1+1,k} \right) \right)$$

$$+ \frac{c_{1,k}}{d_{k-1} + d_{k}} \left( \vec{u}_{1,k-1} - \vec{u}_{1,k+1} \right) + \frac{1}{R_{1}} \left[ - u_{1,k} \cdot b_{1,k} - v_{1,k} \cdot a_{1,k} \right]$$

$$- \frac{v_{1,k} \cdot \vec{a}_{1,k}}{R_{1}} - \frac{2R_{1}}{d_{k+1} + d_{k}} \left[ 0 \right] \left[ d_{k} (f_{1,k-1} - f_{1-1,k-1}) + d_{k-1} (f_{1,k} - f_{1-1,k}) \right]$$

$$- \frac{v_{1,k} \cdot \vec{a}_{1,k}}{R_{1}} - \frac{2R_{1}}{d_{k+1} + d_{k}} \left[ 0 \right] \left[ d_{k} (f_{1,k-1} - f_{1-1,k-1}) + d_{k-1} (f_{1,k} - f_{1-1,k}) \right]$$

$$\left[ M_{2}(a,u) \right]_{1,k} = \frac{1}{R_{1}} \cdot v_{1,k} \cdot \vec{a}_{1,k} + 2 \left[ u_{1,k} \cdot v_{1,k} \right]_{0}$$

$$\left[ (25) \right]_{1,k}$$

and the discrete forms for the gradient fields  ${\tt G}_{0}{\tt f}$  and  ${\tt G}_{1}{\tt f}$  will be

$$[G_0f]_{1,k} = \frac{1}{d_R(d_{k-1}+d_k)} \begin{bmatrix} d_{k-1}(f_{1,k}-f_{1-1,k})+d_k(f_{1,k-1}-f_{1-1,k-1}) & 0 \\ d_R(f_{1,k}+f_{1-1,k}-f_{1,k-1}-f_{1-1,k-1}) \end{bmatrix}$$

$$[G_1f]_{1,k} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \frac{d_{k-1}(f_{1,k}+f_{1-1,k})+d_k(f_{1,k-1}+f_{1-1,k-1})}{2R_1(d_{k-1}+d_k)}$$

$$(26)$$

Fig. 6 shows the values of the function f which is used in equations (26) and (27) to calculate the gradient fields  $G_0f$  and  $G_1f$  at the point  $P_1$  is  $G_0f$ .

Gif at the point  $P_{i,k} \in \mathfrak{I}_G$ Fig. 7 shows the velocity components which are used to calculate the discrete forms of the diverging operators  $D_0 \hat{u}$  and  $D_1 \hat{a}$  at the point  $p_{i,k} \in \widetilde{\mathfrak{I}}_G$  according to the definition of equation (14) as follows

$$\left[ D_{0}\vec{u} \right]_{i,k} = \frac{1}{2R_{i}} \left\{ \frac{R_{i+1}}{d_{R}} (u_{i+1,k}^{+u_{i+1,k+1}}) - \frac{R_{i}}{d_{R}} (u_{i,k}^{+u_{i,k+1}}) \right] \\
+ \frac{R_{i+1}}{d_{k}} (w_{i+1,k+2}^{-w_{i+1,k}}) + \frac{R_{i}}{d_{k}} (w_{i,k+1}^{-w_{i,k}}) \\
\left[ D_{1}\vec{a} \right]_{i,k} = \frac{1}{4R_{i}} (b_{i+1,k+1}^{+b_{i+1,k}} + b_{i,k+1}^{+b_{i,k+1}} + b_{i,k})$$
(28)

A computer program system EBSTR is written in FORTRAN for the numerical simulation of the in-cylinder flow during compression. The complete details and discussion for this system can be found in ref. [10].

#### 4. CONCLUSIONS

This paper shows and describes a numerical method to simulate and predict the turbulent unsteady swirling flow in an eccentric deep bowl combustion chamber of an engine cylinder during compression stroke. The three dimensional problem could be transformed to a number of two dimensional problems by the perturbation method to adopt the present computer capacity. The numerical simulation is performed by using the finite difference method. This method has been applied to simulate the two dimensional flow in a symmetrical deep bowl combustion chamber [1] and the three dimensional flow in an eccentric deep bowl combustion chamber of a direct injection diesel engine in the second part of this paper [11].

#### 5. NOMENCLATURE

a	Eccentricity of the bowl axis
bl	Bowl height (depth)
cl	Total cylinder length = h at BDC
do,dc	Grid spacing in z direction in the bowl and cylinder
₫Ŗ	Grid spacing in R direction
Do, D <sub>1</sub>	Divergent operators
f	Scalar field
F	Dependent variable
$G_0$ , $G_1$	Gradient operators
Go, G <sub>1</sub>	Piston posiction from the cylinder top
L1L4	Number of grid points in R and z direction
м <sub>1</sub> , м <sub>2</sub>	Convection operators
$N_0$ , $N_1$	Convection operators
P, ,	Pressure per unit density

R Radial coordinate in the R plane t Velocity components in the R, O and z coordinates Velocity components in the X, Y and z coordinates Complex variable in the plane z=constant u,v,w U,V,W wg, wp Grid points and piston velocities x, yCartesian coordinates X,Y,z Oriented cartesian coordinates 2,2' Fixed and movable coordinates ß Angle between the coordinates R=const and X=const.  $\epsilon$ Eccentricity parameter ζ Complex variable in the plane z=const. ( $f = F + i\eta$ ) Θ Tangential coordinate 6 Density Swirl ratio, the ratio of swirl angular velocity of Wa that of the engine shaft

#### 6. REFERENCES

- 1. £1 Kady, M.S., Mascheck, H.J., and HOCHE, A., "Numerical simulation of the flow in a symmetrical deep bowl combustion chamber of a diesel engine cylinder during the compression stroke. MEJ, Vol. 12, No. 2, Dec. 1987, pp M20-M30
  2. Gosman, A.D. and John, R.J.R., SAE paper No. 800091
- (1980).
- Ramos, J.I., Humphera, J.A.C. and Sirignano, N.A., SAE paper No. 790356 (1979).
- 4. Griffin, M.D., Anderson, J.D., Diwaker, R., "Navier-Stokes solution of flow field in an I.C.E." AIAA Journal, Vol 14 Dec. 1976 pp 1665-1666.
- 5. Diwakar, R., Anderson, J.D., Griffin, M.D., "Inviscid solutions of the flow field in an I.C.E." AIAA Journal, Vol 14 Dec. 1979 pp 1667-1668
- 6. Seppen, J.J., "A study of flow field phenomena in I.C.E." Ph.D. thesis, TH Delft, October 1982.
- 7. El Kady, M.S., "Serechnung symmetrischer und unsymmetricher Zylinder-Brennraum-Stroemungen in Dieselmotoren beim Verdichtungshub" Dissertation, TU Dresden March 1985
- 8. Peaceman, D.W., Rachford, H.H., "The numerical solution of parabolic and elliptic differential equations", J.Soc. Indust. Appl. Math. 3, 28-41, 1955.
- 9. Stephens, A.S., Bell, J.B., Solomon, J.M., "A finite difference formulation for the incompressible Navier-Stokes equation" J. of
- computational physics, vol. 5 (1984) op 152-172. 10. El Kady, M.S., "Anleitung zur Nutzung der Programme die Berechnung der Zylinder-Brennraum-Stroemungen in Dieselmotoren beim Verdichtungshub." Bericht No. 656. TU Dresden Sektlon 12, WB Stroemungstechnik.
- El Kady, M.S., Mascheck, H.J. and Hoche, A., "Numerical simulation of flows in an engine cylinder with an eccentric deep bowl combustion chamber during compression " (2nd Report: numerical example) MEJ, Vol. 16, No. 2 Dec 1989

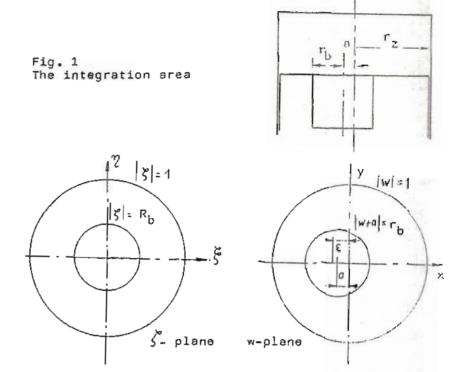


Fig. 2 conformal mapping for the z-plane

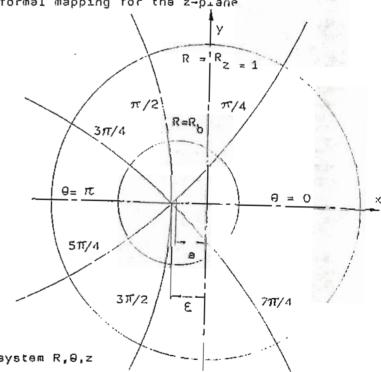


Fig. 3 The coordinate system R.O.z

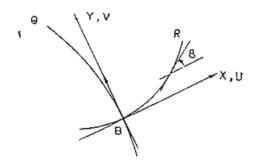


Fig. 4
The oriented cartesian coordinate X,Y,z

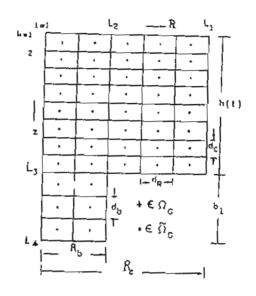


Fig. 5 The computational arrangement

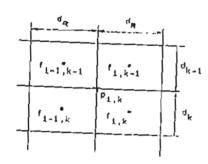


Fig.6 The values of the function f which is used to calculate the gradient fields  $G_0$  f and  $G_1$  f

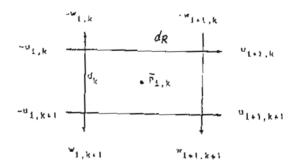


Fig. 7 The velocity components which is used to calculate the discrete values  $\mathbf{D_0}^{\mathrm{u}}$  and  $\mathbf{D_1}^{\mathrm{u}}$