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HORIZONTAL TRANSITIONS IN SUBCRITICAL FLOW.

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الانتقالات الافتية في السريان تحت الحرج

خـــلاصـــة:

_ تستخدم الانتقالات عندما سنغير حجم أو شكل الغطاع المائي وهده البغيــــرات غالدا ما تكون في المجارى المائية الطبيعة أو المناعدة عند المنشأت المائية وذلـــك لفرص اقتصادى أو لفرض عملي ، والانتقالات اما أن تكون رأسة كالتغير في منبوب فــاع المجرى المائي فحائيا أو تدريجيا أو أفغة كحالة اتباع أو تقلم عرى القطاع المائـــي، وهذا التقليم أو الاتتاع أما أن يكون فجائدا أو تدريجيا ، لذلك فان هذه الانتفـــالات معتمد أسادا على الخمائي الهندية للفطاع المائي ، النصرف وكذلك حالة الحريان في المحرى المائي سواء كان حريان تحت حرج أو فوق حرج وننيجة المعودة هذه المشاكل التاجعة مـــــــ المائي والتغيرات فقد أحريت درامة نظرية لاستنداج أهم المعادلات الرياضية إلتي يحكم خـــواي الحريان ظلال هذه الانتفالات الأنفية والحاد حل نظري لحصيع الحالات التي يمكن حدوثها كمــا عثمل هذا البحث درامة معطية لتحقيق تلك النتائج النظرية .

ADSTRACT

The present research deals with open channel transitions (sudden contraction and limited constriction) in subcritical flow. The flow pattern is usually complicated to be analytically solved, so practical solution is possible through systematic experimental investigations.

Interrelationships between parameters in dimensionless forms, which govern the flow characteristics are presented. Effects of contraction ratio, flared entrance and friction on the flow pattern, especially the oblique waves and chocking phenomenon are given.

INTRODUCTION

Transitions are provided whonever the size or shape of cross section of an open channel changes. Such changes are often required in natural or artificial channels at irrigation atructures for economic as well as practical reasons.

The problem of horizontal transition may be solved by writting the specific energy equation before and after the transition sections.

The axiating method for solving the problem of open channel transitlons involves a trial and error solution of higher degree squstion. There are two possible suswers for the depth in transition. The correct enswer can be determined only by knowing in advance the state of flow which will be either subcritical or supercritical condition.

The phenomenon is usually complicated that the resulting flow pattern is not readily subject to any analytical solution, so a practical solution is possible through systematic experimental investigation. The present research deals with horizontal transitions in the case of subcritical flow. Such transitions can be solved more confidently with the use of the specific energy squation than the momentum concept.(7).

the main objective of this research is to develop a graphical solution for horizontal contraction and limited constriction for practical purposes i.e. to establish interrelationahips between hydraulic paramaters which affect the phenomenon in the form of dimensionless terms.

THEORETICAL ANALYSIS

From the concept of specific energy equation:

$$F_{c} = Y + \propto (Q^2/2y \Lambda^2)$$
(1)

in Which;

E = specific energy;
Y' = depth of flow;

≃ energy coefficient;

Q = Water discharge;

A = cross sectional area of flow; and

y = acceleration due to gravity.

For rectongular meetion A = b.Y

Where: b = brendth of section.

$$q^2/2g b^2 \epsilon^3 = (Y/\epsilon)^2 (1 - Y/\epsilon)$$

 $Q_* = Y_*^2 (1 - Y_*)$ (2)

o r

<u>,</u>

in which;

Q. = dimensionless discharge

$$= \sqrt{q^2/2g b^2 E^3}$$

Y_{*} = dimensionless depth = Y/E

Equation (4) can be written in the fullowing form:

$$E = Y(1 + F^2/2)$$

 $Y_* = 1/(1 + F^2/2)$ (3)

From equations (2) and (3)

$$U_{*} = (f/\sqrt{2})(1+f^{2}/2)^{3/2}$$
(4)

The specific energy equation for section upstream and downstream the transition can be written as:

$$E_1 = E_2 + \Delta E$$

i.e.
$$Y_1 + \frac{q^2}{2g b_1^2 Y_1^2} = Y_2 + \frac{q^2}{2g b_2^2 Y_2^2} + \Delta E$$
(5)

Equation (3) can be arranged to give

$$F_1^2 = \frac{2((Y_2/Y_1^{-1}) + \Delta E/Y_1)}{(1 - 1/(\frac{b_2 Y_2}{b_1 Y_1})^2} \dots (6)$$

$$\sigma r = \frac{2((Y_s - 1) + h_2/Y_1)}{(1 - \frac{1}{Y_s^2} (1 - \frac{\Delta b}{b_1})^2}$$

Where: Y_s = Y₂/Y₁

Again equation (5) can be written as:

$$E = Y_1(1 + F_1^2/2) - Y_2(1 + F_2^2/2)$$

10

$$\frac{1 + F_2^2}{1 + F_1^2/2} = \frac{1}{Y_2/Y_1} \left(1 - \frac{\Delta E/Y_1}{1 + F_1^2/2}\right) \dots (7)$$

From the continuity equation:

Q = constant = A₁ V₁ = A₂ V₂ = b₁ Y₁ V₁ = b₂ Y₂ V₂

or:
$$\frac{b_1^2 y_1^3 y_1^2}{g y_1} = \frac{b_2^2 y_2^3 y_2^2}{g y_2} \dots (B)$$

$$F_1^2 = (\frac{b_2}{b_1})^2 (\frac{Y_2}{Y_1})^3 F_2^2 \dots (9)$$

From equation (4)

$$(q_{+2}/q_{+1}) = (F_2/F_1)^2 \left(\frac{1 + F_1^2/2}{1 + F_2^2/2}\right)^3 \dots (10)$$

The relationships between $Q_{*,7}$ and F_1 with the parameter b_2/b_1 are derived from equations (9) and (10) the following equation:

$$Q_{*2} = F_1^2/2 (b_2/b_1)(1 + F_1^2/2 - \Delta E/Y_1)^3$$
(11)
Again equation (5) can be written as follows:

$$\Delta E/Y_{1} = (1 + F_{1}^{2}/2) - (Y_{2}/Y_{1} + F_{1}^{2}/2 (b_{2}/b_{1})^{2} (y_{2}/y_{1})^{2})$$
or
$$\Delta E/E_{1} = Y_{1}/E_{1}(1 + F_{1}^{2}/2) - (Y_{2}/Y_{1} + F_{1}^{2}/2 (b_{2}/b_{1})^{2} (Y_{2}/Y_{1})^{2})$$

$$= \frac{1}{(1 + F_{1}^{2}/2)} (1 + F_{1}^{2}/2) - (Y_{2}/Y_{1} + F_{1}^{2}/2 (b_{2}/b_{1})(Y_{2}/Y_{1})^{2})$$

The above equation represents the relationship between the efficiency (E_2/E_1 = 1.- $\Delta E/E_1$) and F_1 with (b_2/b_1) and (Y_2/Y_1) as parameters.

EXPERIMENTAL WORK

Experiments were conducted in flow visulization tank. The general arrangement of this equipment is shown in Fig.(1). The channel has two steel parallel walls and cross section of 61 cm breadth and 20 cm depth, along its two metres length. For the purpose of the present study, in order to have more accurate results, an extended part of other two metres having the same cross section was fabricated.

The channel is firmly supported on two steel tanks inlet tank (1) and outlet tank (1) the two steel water tanks are predisposed for closed circuit. The inlet tank was provided with grading gravel rest on horizontal screen to minimise the energy of the coming flow. A suitable pump (4) was provided to the apparatue to supply weter in a closed circuit, suction pipe (3) and delivery pipe (5) from the outlet tank to the inlet tank. An inferential mechanical meter (2) which measure the flow rate into the channel is placed on the suction pipe. Because of high head loss this type of meter is not often used for measuring flow rate above 0.3 m/sec. Valve (6), control the flowrate, is placed on the delivery pipe. The outlet water from the channel falls freely over steel spillway (11) back to the outlet tank for recirculation. The water depth is controlled by screw wheel (10) which is used to adjust the spillway inclination. The water depth was measured by a hook gauge mounted on carriage (9) which could slide across the breadth of the channel. Also it could slide along two rails above the horizontal surface of the channel.

The velocity through the channel was measured by using the current meter. Some readings of the current meter were checked by using the pitot tube.

Apair of steel side wells were erected in both sides of the channel providing an equal distance to the centre line giving a transition part for the purpose of study. They were 2.0 m in

length and 0.2 m height (sudden contraction), plate (1). Another pair of steel walls were used with 0.5 m long and 0.2 m height (limited constriction), plate (2), four shapes of transitions are shown in Fig. (2).

The widths used for transition section having contraction ratio $\Delta b/b = 0.1$, 0.2, 0.3, 0.4, 0.5 and 0.6.

The transition section, under test was Fixed at the channel by using water tight material. The water depth at the upstream of transition was fixed to the required depth at a steady Flow condition.

RESULTS AND ANALYSES

The analysis of transition is based on the assumptions, the flow is considered one dimensional flow, both the energy coefficient and momentum coefficient are unity, the pressure is hydrostatically distributed and the channel is considered in horizontal position.

The following figures, from Fig.(1) to Fig.(28) show the relationships between these parameters:

$$F_1 = V_1 / \sqrt{gY_1}, \quad F_2 = V_2 / \sqrt{gY_2}, \quad Y_{*2} = Y_2 / E_1,$$

$$Q_{*2} = \sqrt{Q^2 / 2g b_2^2 E_2^3}, \quad Y_s = Y_2 / Y_1, \quad \theta_{*2} = b_2 / E_2$$

 $Y_{*1} = Y_1/E_1$, $Q_{*1} = \sqrt{Q^2/2g\,b_1^2\,E_1^3}$, $B_{*1} = b_1/E_1$ and E_2/E_1 for contraction ratio $\triangle b/b = 0.1$, 0.2, 0.3, 0.4, 0.5 and 0.6.

The relationships between the following parameters are the same for both the sudden contraction and limited constriction cases:

The relation between upstream froude number F_1 and the submergence Y_2 , dimensionless upstream depth Y_{+1} and Y_2 , and the upstream dimensionless breadth B_{+1} and Y_1 have shown bigger values in the case of limited constriction. A limited constriction exhibited bigger value of the downstream dimensionless discharge Q_{+2} than the corresponding one in a sudden contraction case for the same contraction ratio and F_1 the limited constriction has bigger downstream froude number F_2 , Q_{+2} , Y_{+2} and Y_5 than the corresponding audden contraction for the same value of B_{+1} and A_5/b . Slightly bigger values of downstream dimensionless breadth B_{+2} are given by limited constriction than sudden contraction for Froude number less than 0.25 and for contraction ratio $A_5/b = 0.4$, 0.5 and 0.6.

Values of Q_{*2} are bigger in the case of limited constriction then the case of Sudden contraction for the same value of Y_{*1} and

contraction ratio. On the contrary the valua of Y_{*2} is bigger in the sudden contraction for $\triangle b/b = 0.4$, 0.5 and 0.6.

A limited constriction has bigger value of Q_{*2} and smaller value of Y_{*2} for the same value of Q_{*1} under the same contraction ratio $_{\bullet}b/b^2=0.4,\ 0.5$ or 0.6.

The value of efficiency $\rm E_2/E_1$ increases with the decreasing value of contraction ratio under the same value of both the upstream froude number $\rm F_1$, depth $\rm Y_{*1}$ and discharge $\rm Q_{*1}$. Also with the same value of contraction ratio, the value of efficiency $\rm E_2/E_1$ increases with the decreasing value of both the upstream froude number and $\rm Q_{*1}$ and with the increasing value of $\rm Y_{*1}$.

The sudden contraction case exhibited higger values of efficiency $\rm E_2/E_1$ than the limited constriction mainly due to less energy losses.

Velocity Distribution

Change in shape and values of velocity contours (isovels) was observed by changing the contraction ratio Figs. (29 a and 29 b) or the channel bed from plain to gravel bed Figs. (30 s and 30 b).

Calculation of energy coefficient \propto varies with the contraction ratio, bed roughness and position of section.

The momentum coefficient ${\cal B}$ is slightly affected by both contraction ratio and bed roughness.

Effect of Flared Entrance

An improvement of flow through constriction has emergged due to increasing the degree of flaring at entrance from 1:1 sudden, 1:2, 1:3 and 1:4. It is noticed from Fig. (31a) that increasing the degree of flaring decreases the value of $\Delta E_{\perp}/E_{\perp}$ as the flow in the flaied entrance will deflect gradually to pass downstream than the case of sudden entrance plate (3). Fig. (31b) gives the relationship between degree of flaring and the downstream Froude number for different values of water depths.

Chaking Phenomenon

Yarious profiles of water surface occur in horizontal transition problems. These different profiles are dependent on the state of approach of flow and horizontal transition conditions.

If the contraction becomes critical at the downstream section, the flow will be in a critical condition and the characteriatics of the upstream flow, depth and velocity will not be affected at this stage. When the contracted width is less than the critical breadth, chocking phanomenon will occur i.e. the breadth of the channel will not be able to pass the energy per unit width of the channel and the upstream flow condition will be influenced.

The contraction ratios $\triangle b/b = 0.2$, 0.3, 0.4, 0.5 and 0.6 were used to cause backwater the transition section. Oblique standing waves (shock waves) within the transition were observed. The relationship between unstream frouds number F. and contraction ratio

tionship between upstream Froude number F₁ and contraction ratio b/b are given in Fig. (32). It is observed from the figure that the theoretical values of contraction ratio are bigger than the corresponding practical values which causes the chocking phenomenon mainly due to energy losses covering the transition in practical cases.

The pattern of standing waves was found approximately at centre line of the channel for contraction ratio more than the critical contraction ratio which causes the choking. It moves to the upstream position with an increasing value of contraction ratio b/b, Fig. (33). Also the deflection angles of oblique standing waves are abown between 30 and 35°, Fig. (33).

Bed roughness (gravel bed), plate (4) causes the junction to move in the upstream position, Fig. (34) and decreases the negative disturbances at the downstream in comparison with the same contraction ratio for plain bed and it was observed that the deflection angle increases with $\Delta b/b = 0.6$.

Figure (35) shows the flered entrance decreases the water depths upstream section (2), Fig. (2). Water depths increases with flared entrance from 12.5 cm downstream section (2) to about 37.5 cm at the constriction and downstream the transition, as the energy per unit width in case the flared entrance will have more chance to pass the downstream. The same behaviour, as before, can be obtained for flared entrance of gravel bed Fig. (36). This could mean that the flared entrance is more effective in the chocking than the bed roughness.

CONCLUSIONS

A set of graphical relationships has been deduced which could be used for design purposes to provide an accurate solution to the theoretical one.

Experimental value for the critical width of a channel is bigger than the corresponding theoretical value given by the equation:

$$(b_c/b)^2 = F_1^2 - (1.5/(1 + F_1^2/2)^3$$

and the difference between the Lwo values increases with the increasing value of the upstream froude number.

It is hoped that this paper will be of value in the solution of problems involving horizontal transitions especially chocking phenomenon and cross wavee (coblique standing waves). However the successful design of transition depend on the designer ability to predict the deflection angle with reasonable degree of accuracy.

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NOTATION

```
The following symbols are used in this paper:
     = croas sectional area;
ь
     = breadth of section;
ь
8 с
     = critical contraction breadth;
     = dimensionless breadth;
E
     = specific energy;
     = Frouda's number;
F
     = acceleration due to gravity;
g
     = water discherge;
u.
     = dimensionless discharge;
     = water mean velocity;
     = water depth;
     = dimensionless depth;
     = Y_2/Y_1.
```

= energy coefficient;
β = momentum coefficient;

b '= contraction in breadth;

SE = energy loss; and

9 = angle of flared entrance.

<u>Subscripts</u>

1 = upstream; end 2 = downstreem.

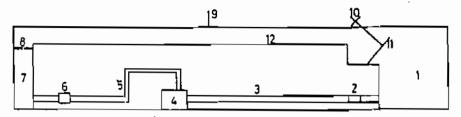
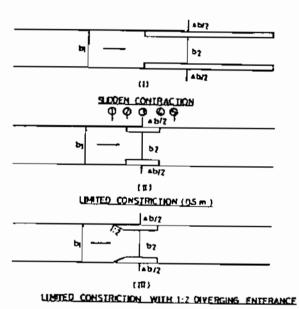


FIG.(1) EXPERIMENTAL APPARATUS.

1) OUTLET TANK 7) (NLET TANK
2) SPARLING 8) SCREAN
3) SUCTION PIPE 9) HOOK GAUGE
4) PUMP 10) SCREW WHEEL
5) DELIVERY PIPE 11) STEEL SPILWAY
6) VALVE 12) STEEL CHANNEL



(141)

FIG. 2 DIFFERENT TRANSITIONAL SHAPES

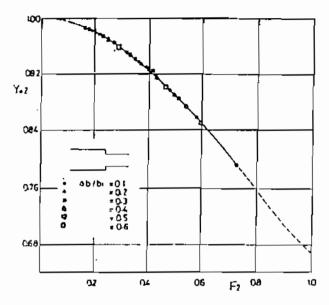
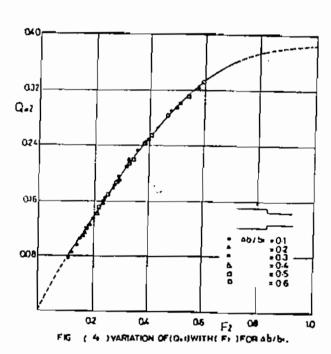
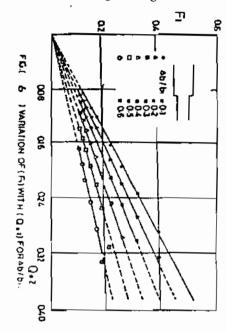
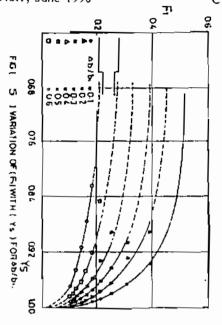
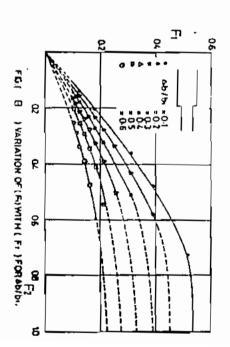


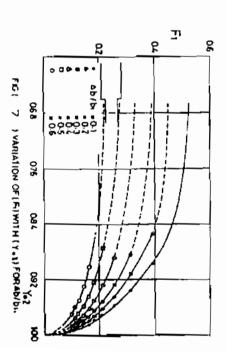
FIG (3) VARIATION OF IT-INVIEW (F)) FOR A DIVIN

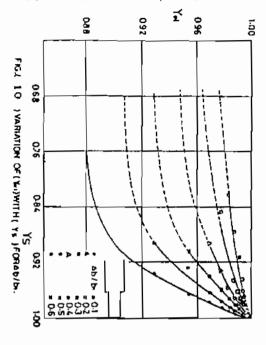


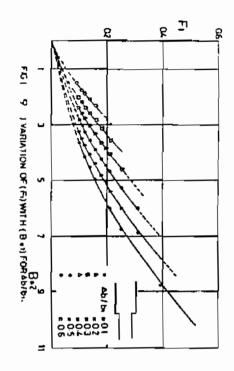


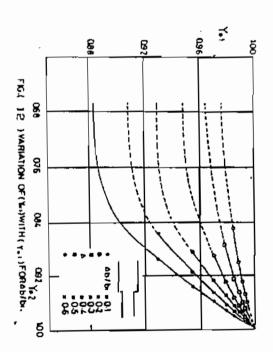


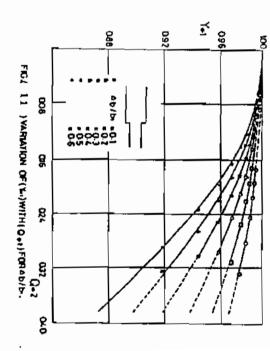


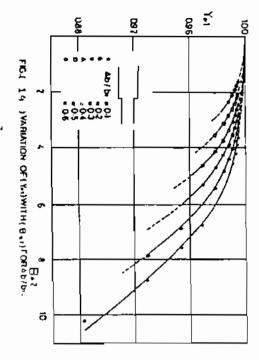


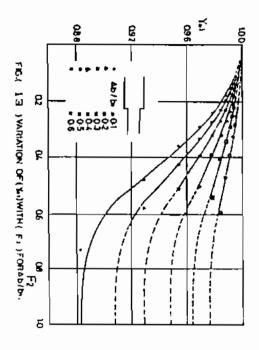


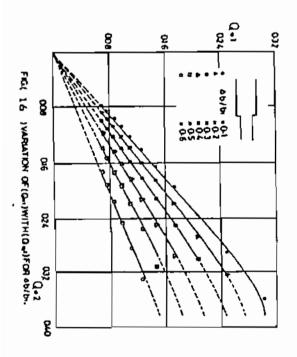


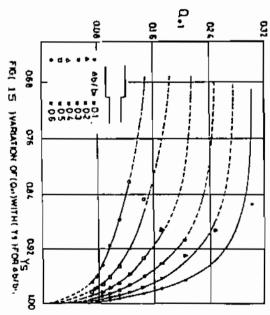


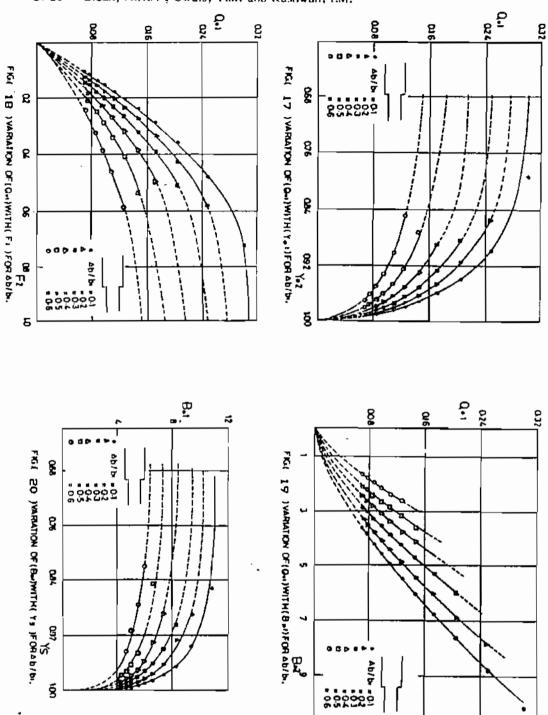


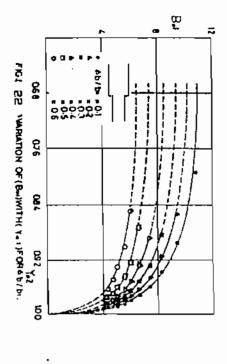


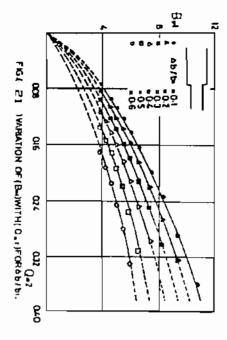


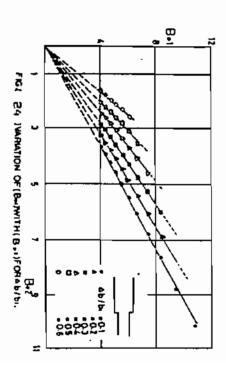


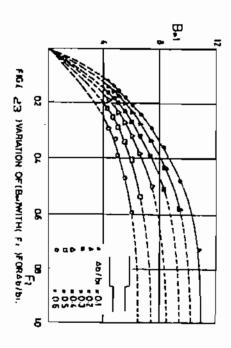


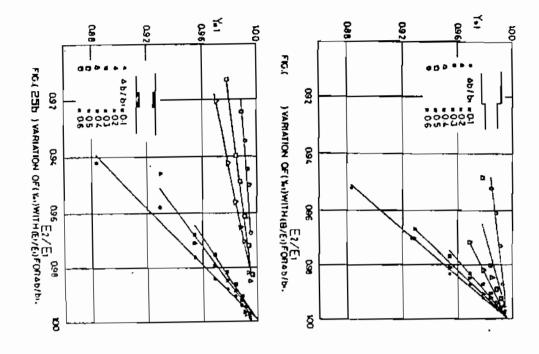


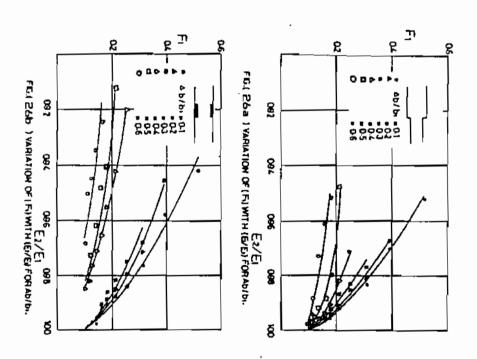


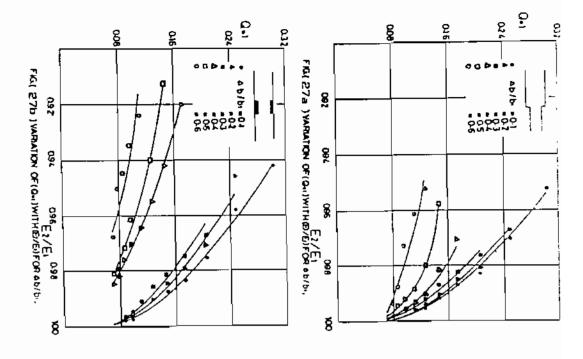


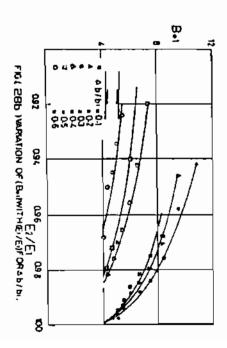


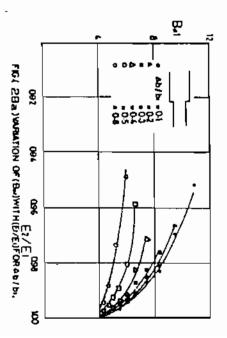












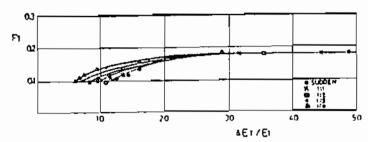
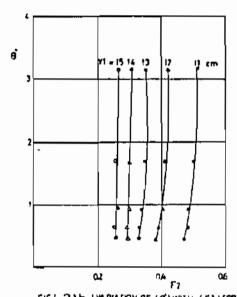
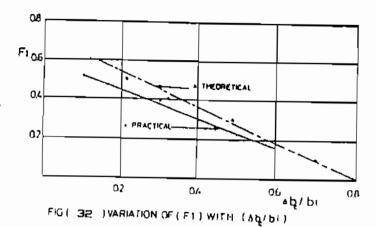
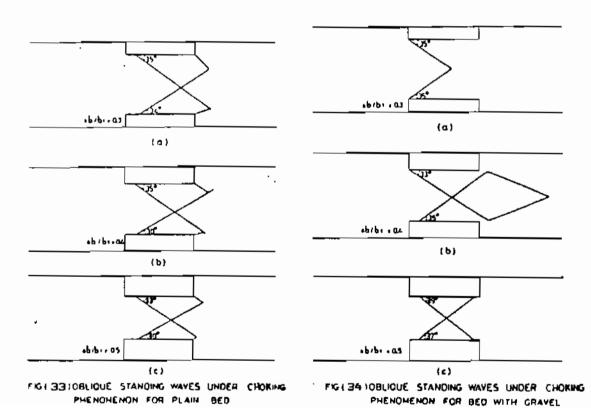


FIG. (31a) VARIATION OF (FI) WITH (AET/EI) FOR(8)



FIGE 315 IMPRATION OF (d) WITH (FE) FOR YE





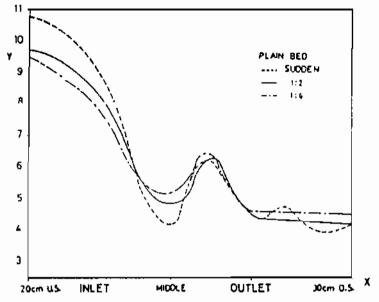
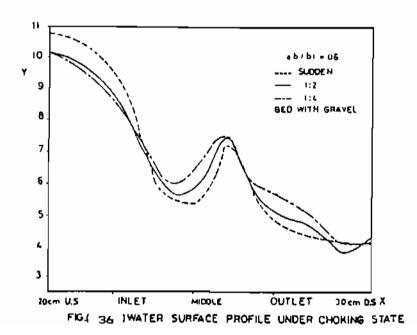


FIG.(35) WATER SURFACE PROFILE UNDER CHOKING STATE



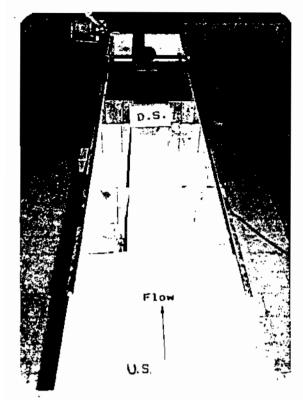


Plate (1) Sudden contraction



Plate (2) Limited constriction

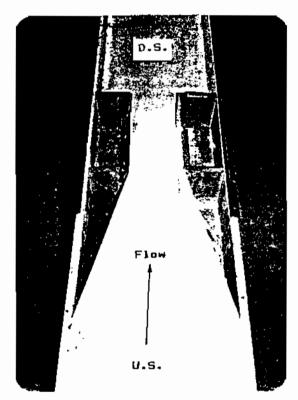


Plate (3) Flared entrance



Plate (4) Gravel bed