# [Mansoura Engineering Journal](https://mej.researchcommons.org/home)

[Volume 15](https://mej.researchcommons.org/home/vol15) | [Issue 1](https://mej.researchcommons.org/home/vol15/iss1) Article 2

6-1-2021

# Horizontal Transitions in Subcritical Flow.

A. Zidan

Associate Professor of Irrigation and Hydraulic Engineering Department, Faculty of Engineering, Mansoura University, Mansoura, Egypt.

T. Owais Dean and Heed of Water Engineering, Faculty of Engineering, Zagazig University, Zagazig, Egypt.

I. Reehwen Heel Corporation, Saudi Arabia.

Follow this and additional works at: [https://mej.researchcommons.org/home](https://mej.researchcommons.org/home?utm_source=mej.researchcommons.org%2Fhome%2Fvol15%2Fiss1%2F2&utm_medium=PDF&utm_campaign=PDFCoverPages)

# Recommended Citation

Zidan, A.; Owais, T.; and Reehwen, I. (2021) "Horizontal Transitions in Subcritical Flow.," Mansoura Engineering Journal: Vol. 15 : Iss. 1 , Article 2. Available at:<https://doi.org/10.21608/bfemu.1990.170532>

This Original Study is brought to you for free and open access by Mansoura Engineering Journal. It has been accepted for inclusion in Mansoura Engineering Journal by an authorized editor of Mansoura Engineering Journal. For more information, please contact [mej@mans.edu.eg](mailto:mej@mans.edu.eg).

## HORIZONTAL TRANSITIONS IN SUBCRITICAL FLOW.

Zidan, A.R.A<sup>\*</sup>; Owais, T.M.<sup>\*\*</sup> and Reshwan, I.M.<sup>\*\*\*</sup><br>\* Aasoc. Prof. Irrigstion and Hydr. Dept., Mansoura University.<br>\*\* Dean and Head of Water Engry, Fac. of Engry, Zagazig Univ. \*\*\* Hael Corporation, Saudi Arabia.

الانتقبالات الافقية في السريان تحت الحرج

خــلاصــة :

ــ تصفقهم الانتقالات محتمدا منفير حدم أو خلال الفطاع المدائى وهذه العفيــــــر<br>تحاليا ما تكون في المجاري المائجة الطبيعية أو المناعية عند المحتشات المدائية وذلـــــ<br>لكرس اقتصادي أو لكرش مملي الما والانتقالات اما أن تكون ر ــر ات المه — اع لخرص اقتصادى او لخرض معلى الما والانتقالات اما ان تكون راسمة كالتغيير فى منصوبا فـــــــــــــــــــــــــــــ<br>المجرى المائى فحائبا أو تدريجيا أو أفغنة كحالة النباع أو تقليم عرض القطاع المائـــــــــــــــــــــــــــــــ

#### **ADSTRACT**

The present research deals with open channel transitiona (sudden contraction and limited constriction) in subcritical flow. The flow pattern is usually complicated to be analytically solved, so practical solution is possible through systematic experimental investigations.

Interrelationships between parameters in dimensionless forms, which govern the flow characteristics are presented. Effects of contraction ratio, flared entrance and friction on the flow pattern, especially the oblique waves and chocking phenomenon are given.

#### **INTRODUCTION**

Transitions are provided whenever the size or shape of cross section of an open channel changes. Such changes are often regoired in natoral or artificial channels at irrigation atructures for economic as well as practical reasons.

The problem of horizontal transition may be solved by writting the specific energy equation before and after the transition sections. The axiating method for solving the problem of open channel transitlons involves a trial and error solution of higher degree aquation.<br>There are two possible answers for the depth in traneition. The correct answer can be determined only by knowing in advanca the state of flow which will be either subcritical or supercritical condition.

The phenomenon is usually complicated that the resulting flow<br>pattern is nut rendily subject to any analytical solution, so a practical sululion is possible through systematic experimental investigation. The present research deals with horizontal transitional in the case of subcritics! Flow. Such transitions can be solved<br>more confidently with the use of the specific energy squation than the momentum concept.(7).

the main objective of this research is to develop a graphical solution for horizontal contraction and limited constriction for practical purposes i.e. to establish interrelationahips between hydraulic paramaters which affect the phenomenon in the form of dimensionless terms.

```
THEORETICAL ANALYSIS
```

```
From the concept of specific energy equation:
                   F = Y + \alpha C \frac{q^2}{2u} \Lambda^2......(1)
in Which:
              E = specific energy;<br>Y = depth of flow;
              x = energy coefficient;
              Q = Water discharge;
              A = cross sectional area of flow; and
              y = acceleration due to gravity.
       For rectonaular nection A = b \cdot YWhere: b = brendth of section.
       Considering \alpha = 1.0 equalion (1) becomes
           q^2/2q b^2 \t E^3 = (Y/E)^2 (1 - Y/E)<br>Q_+ = Y_+^2 (1 - Y_+^2)o e
                                                                        ......(2)in which;
             Q. = dimensionless discharge
                \frac{1}{2} \sqrt{a^2/2a-b^2} \sqrt{c^3}and
            Y_+ = dimensionless depth = Y/EEquation (1) can be written in the fullowing form:
                   E = Y(1 + F<sup>2</sup>/2)Y_+ = 1/(1 + F^2/2)ť.
       \overline{\mathbf{0}} \overline{\mathbf{r}}\ldots \ldots (3)From equations (2) and (3)
                  q_{\perp} = (f / \sqrt{2})(1 + f^2 / 2)^{3/2}\ldots \ldots (4)
```
The specific energy equation for section upstream and downst-<br>ream the transition can be written as:  $E_1 = E_2 + \Delta E$ 

i.e. 
$$
Y_1 + \frac{q^2}{2q b_1^2 y_1^2} = Y_2 + \frac{q^2}{2q b_2^2 y_2^2} + \Delta E
$$
 .........(5)

Equation (3) can be arranged to give

$$
F_1^2 = \frac{2((Y_2/Y_1 - 1) + \Delta E/Y_1)}{(1 - 1/(\frac{b_2 Y_2}{b_1 Y_1})^2)}
$$
 (6)

or 
$$
F_1^2 = \frac{2((Y_9 - 1) + h_2/Y_1)}{(1 - \frac{1}{Y_8^2} (1 - \frac{\Delta b}{b_1})^2)}
$$

Where:  $Y_g = Y_2/Y_1$ 

Again equation (5) can be written aa :

$$
E = Y_1(1 + F_1^2/2) - Y_2(1 + F_2^2/2)
$$

 $0<sub>l</sub>$ 

L

 $\bullet$ 

$$
\frac{1 + F_2^2}{1 + F_1^2/2} = \frac{1}{\gamma_2/\gamma_1} (1 - \frac{\Delta E/Y_1}{1 + F_1^2/2}) \qquad \qquad \dots \dots (7)
$$

From the continuity equation:

 $Q = constant = A_1 V_1 = A_2 V_2 = b_1 Y_1 V_1 = b_2 Y_2 V_2$ 

$$
\frac{b_1^2 \gamma_1^3 \gamma_1^2}{g \gamma_1} = \frac{b_2^2 \gamma_2^3 \gamma_2^2}{g \gamma_2}
$$
 (8)

$$
F_1^2 = \left(-\frac{b_2}{b_1}\right)^2 \left(-\frac{v_2}{v_1}\right)^3 \ F_2^2 \qquad \qquad \ldots \ldots \tag{9}
$$

From equation (4)

$$
(u_{*2}/u_{*1}) = (F_2/F_1)^2 \left(\frac{1 + F_1^2/2}{1 + F_2^2/2}\right)^3 \qquad \qquad (10)
$$

The relationships between  $0_{+7}$  and  $F_1$  with the psrameter  $b_2/b_1$ <br>are derived from equations (9) and (10) the following equation.

Again equation (5) can be written as follows:

$$
\Delta E/Y_1 = (1 + F_1^2/2) - (Y_2/Y_1 + F_1^2/2 (b_2/b_1)^2 (y_2/y_1)^2)
$$
  
or 
$$
\Delta E/E_1 = Y_1/E_1(1 + F_1^2/2) - (Y_2/Y_1 + F_1^2/2 (b_2/b_1)^2 (Y_2/Y_1)^2)
$$

$$
= \frac{1}{(1 + F_1^2/2)} (1 + F_1^2/2) - (Y_2/Y_1 + F_1^2/2 (b_2/b_1)(Y_2/Y_1)^2
$$
........(12)

The above equation represents the relationship between the efficiency  $(E_2/E_1 = 1 - \Delta E/E_1)$  and  $F_1$  with  $(b_2/b_1)$  and  $(Y_2/Y_1)$ as parameters:

#### **EXPERIMENTAL WORK**

Experiments were conducted in flow visulization tank. The general arrangement of this equipment is shown in Fig. (1). **The** channel has two ateel parallel walls and cross section of 61 cm breadth and 20 cm depth, along its two metree length. For the purpose of the present etudy, in order to have more accurate results,<br>an extended part of other two metres having the same croes section was fabricated.

The channel is firmly supported on two steel tanks inlet tank  $(7)$  and outlet tank  $(1)$  the two ateel water tanks are predisposed For closed circuit. The inlet tank was provided with grading gravel rest on horizontal screen to minimise the energy of the coming flow. A suitable pump (4) was provided to the apparatue to supply weter in a closed circuit, suction pipe (3) and delivery pipe (5) from the outlet tank to the inlet tank. An inferential mechanical meter (2) which measure the flow rate into the channel is placed on the suction pipe. Because of high head loss this type of meter is<br>not often used for measuring flow rate above 0.3 m'/sec. Valve (6), control the flowrate, is placed on the delivery pipe. The outlet water from the channel falls freely over steel spillway (11) back to the outlet tank for recirculation. The water depth is controlled by screw wheel (10) which is used to adjust the spillway inclination. The water depth was measured by a hook gauge mounted on carriage (9) which could slide across the breadth of the channel. Also it could slide along two rails above the horizontal surface of the channel.

The velocity through the channel was measured by using the current meter. Some readinga of the current meter were checked by using the pitot tube.

Apair of ateel aide wells were erected in both aidea of the channel providing an equal distance to the centre line giving a transition part for the purpose of study. They were 2.0 m in

length and 0.2 m height (sudden contraction), plate (1). Another pair of steel wells were used with 0.5 m long and 0.2 m height (limited constriction), plate (2), four shapes of transitions are shown in Fig. (2).

The widths used for traosition section having contraction ratio  $ab/b = 0.1, 0.2, 0.3, 0.4, 0.5$  and 0.6.

The transition section, under test was Fixed at the channel by using water tight material. The water depth at the upstream of transition was fixed to the required depth at a steady flow condition.

### RESULTS AND ANALYSES

The analysis of transition is baaed on the asaumptions, the Flow is considered one dimensional Flow, both the energy coefficient and momentum coefficient are unity, the pressure is hydrostatically distributed and the channel is considered in horizontal oosition.

The following figures, from fig. (1) to Fig. (28) show the relationships between these parameters:

$$
F_1 = v_1 / \sqrt{gY_1}, \quad F_2 = v_2 / \sqrt{gY_2}, \quad Y_{*2} = Y_2 / E_1,
$$
  

$$
Q_{*2} = \sqrt{q^2 / 2g b_2^2 E_2^3}, \quad Y_s = Y_2 / Y_1, \quad B_{*2} = b_2 / E_2
$$

 $Y_{*1} = Y_1/E_1$ ,  $Q_{*1} = \sqrt{q^2/2g b_1^2 E_1^3}$ ,  $B_{*1} = b_1/E_1$  and  $E_2/E_1$  for contraction ratio  $ab/b = 0.1$ , 0.2, 0.3, 0.4, 0.5 and 0.6.

The relationships between the following parameters are the same for both the sudden contraction and limited constriction cases:

 $F_1 \longrightarrow F_2$ ;  $Y_{*1} \longrightarrow F_2$ ;  $Y_{*1} \longrightarrow B_{*2}$ ;  $Q_{*1} \longrightarrow F_2$ ;  $Q_{*1} \longrightarrow B_{*2}$ and  $B_{+1} \longrightarrow B_{+2}$ .

The relation between upstream Froude number  $F_1$  and the submer-<br>gence  $Y_3$ , dimensionless upstream depth  $Y_{*1}$  and  $Y_3$ , and the upstream<br>dimensionless breadth  $B_{*1}$  and  $Y_1$  have shown bigger values in the<br>case case of limited construction. The limited construction exhibited big-<br>ger value of the downstream dimensionless discharge  $\mathbb{Q}_*$  than the<br>corresponding one in a sudden contraction case for the same contr-<br>action ratio 0.25 and for contraction ratio  $\triangle b/b = 0.4$ , 0.5 and 0.6.

Values of  $Q_{*2}$  are bigger in the case of limited constriction<br>then the cese of Sudden contraction for the same value of  $Y_{*1}$  and

C. 18 Zidan, A.R.A : Owais, T.M. and Rashwan, I.M.

contraction ratio. On the contrary the valua of  $Y_{*2}$  is bigger in the sudden contraction for  $\blacktriangle b/b = 0.4$ , 0.5 and 0.6.

A limited constriction has bigger value of  $Q_{*2}$  and smaller value<br>of  $Y_{*2}$  for the same value of  $Q_{*1}$  undar the same contraction ratio<br>Ab/b<sup>2</sup> = 0.4, 0.5 or 0.6.

 $\mathbf{r}_\perp$ 

The value of efficiency  $E_2/E_1$  increases with the decreasing<br>value of contraction ratio under the asme value of both the upstream Froude number  $F_1$ , depth  $Y_{*1}$  and discharge  $Q_{*1}$ . Also with the same<br>value of contraction rstio, the value of efficiency  $E_2/E_1$  increases<br>with the decreasing value of both the upstream Froude number and  $Q_{*1}$ and with the increasing value of  $Y_{*1}$ .

The sudden contraction case exhibited higger values of efficiency  $E_2/E_1$  than the limited constrictinn mainly due to less energy  $_{\text{losses}}$ .

#### Velocity Distribution

Change in shape and values of velocity contours (isovels) was<br>obaerved by changing the contraction ratio Figs. (29 a and 29 b) or the channel bed from plain to gravel bed Figs. (30 s and 30 b).

Calculation of energy coefficient X varies with the contraction ratio, bed roughness and position of section.

The momentum coefficient  $B$  is slightly affected by both contraction ratio and bed roughness.

#### Effect of Flared Entrance

An improvement of flow through constriction has emergged due to increasing the degree of flaring at entrance from 1:1 sudden, 1:2,<br>1:3 and 1:4. It is noticed from Fig. (31a) that increasing the degree of flaring decreases the value of  $\Delta E_T/E_T$  as the flow in the flaied entrance will deflect gradually to pass downstream than the case of sudden entrance plate (3). Fig. (31b) gives the relation-<br>ship between degree of flaring and the downstream Froude number for different values of water depths.

#### Chaking Phenomenon

Various profiles of water surface occur in horizontal transition probleme. These different profiles are dependent on the state<br>of approach of flow and horizontal transition conditions.

If the contraction becomes critical at the downstream section, the flow will be in a critical condition and the characteriatics of the upstream flow, depth and velocity will not be affected at this<br>stage. Whan the contracted width is less than the critical breadth,<br>chocking phanomenon will occur i.e. the breadth of the channel will not be able to pasa the energy per unit width of the channel and the upatream flow condition will be influenced.

the theoretical values of contraction ratio are bigger than the corresponding practical values which causes the chocking phenomenon mainly due to energy losses covering the transition in practical CASAS.

The pattern of standing waves was found approximately at centre line of the channel for contraction ratio more than the critical contraction ratio which causes the choking. It moves to the upstream position with an increasing value of contraction ratio b/b, Fig.  $(33)$ . Also the deflection angles of oblique standing waves are aho-<br>wn between 30 and 35<sup>9</sup>, Fig. (33). ,  $Fig. (33)$ .

Bed roughness (gravel bed), plate  $(4)$  causes the junction to move in the upstream position, Fig.  $(34)$  and decreases the negative disturbances at the downstream in comparison with the same contraction ratio for plain bed and it was observed that the deflection angle increases with  $\Delta b/b = 0.6$ .

Figure (35) shows the flered entrance decraases the water depths upstream section (2), Fig. (2). Water depths increases with flared<br>entrance from 12.5 cm downstream section (2) to about 37.5 cm at the constriction and downstream the transition, as the energy per unit width in case the flared entrance will have more chance to pass the downstream. The same behaviour, as before, can be obtained for flared entrance of gravel bed Fig. (36). This could mean that the fla-<br>red entrance is more effective in the chocking than the bed roughness.

### CONCLUSIONS

A set of graphical relationships has been deduced which could be used for design purposes to provide an accurate solution to the theoretical one.

Experimental value for the critical width of a channel is bigger than the corresponding theoretical value given by the equation:

$$
(b_c/b)^2 = F_1^2
$$
  $(1.5/(1 + F_1^2/2)^3)$ 

and the difference between the two values increases with the increasing value of the upstream Froude number.

It is hoped that this paper will be of value in the solution of problems involving horizontal transitions especially chocking phenomenon and cross wavee (coblique standing waves). However the successful design of transition depend on the designer ability to predict the deflection angle with reasonable degree of accuracy.

Zidan, A.R.A; Owais, T.M. and Rashwan, L.M.  $C.20$ 

## REFERENCES

- 1. Austin, L.H., Skogerboe, G.V. snd Bennett, R.S. "Outlet Transition with Triangular Sharped Baffles", Journal of the Irrigation and Drainage Div., ASCE, Vol.97, No. IR3 Sept. 1971.
- 2. Bagge, G. and Herbish, J.B., "Transition in Superciritical Open Channel Flow", Journal of the Hydraulic Oiv., ASCE, Vol.<br>93, No. No. HY5, Sept. 1967.
- 3. Chow, V.T., "Open Channel Hydraulics, McGraw Hill, 1959.
- 4. Henderson, F.M., "Ocen Channel Flow", The Macmillan Co., 1967.
- 5. Herbish, J.B. and Walsh, P., "Supercritical Flow in Rectangular<br>Expansions", Journal of the Hydraulic Div., ASCE, Vnl.<br>98, Nn. HY9, Sept. 1972.
- 6. Lokrai, V.P. and Shen, H.W., "Analysis of the Characteristics of Flow in Sudden Expansion by Similarity Approach", Journal of the Hydraulic Research, No. 2, 1983.
- 7. Rashwan, I.M., "Flow Characterstics Through Horizontal Transit-<br>ions", M.Sc. Theais, Faculty of Engineering, Mansoura<br>University, 1987.
- 8. Skoyerboe, G.V., Austin, L.H. and Bennett, R.S., "Energy Lose Analysis in Open Channel Expansion", Journal of the Hyd-<br>raulic Oiv., ASCE, Vol. 97, No. HY2, 1966.
- 9. Skogerhoe, G.V. and Hyatt, H.L., "Analysis of Submergence in Flow<br>Measuring Flumes", Journal of the Hydraulic Div., ASCE,<br>Vol. 93 No. HY4, July 1967.
- 10. Vittal, N., "Direct Solution to Problems of Open Channel Transitions", Journal of the Hydraulic Oiv., No. HY11, 1978.

#### NOTATION

The following symbols are used in this paper:

```
: croas sectional area:
\mathbf{A}= breadth of section;
\mathbf{h}\overline{b} \overline{c}= critical contraction breadth;
      = dimensinnless breadth;
E,
      = apecific energy;
Ė
      = Froude's number;= acceleration due to gravity;
g
Ō
      = water discherge;
\mathbf{u}_*= dimensionless discharge;
\mathbf{v}= water mean velocity;
Y
      = water depth;
\mathsf{Y}_\pm= dimensionleas depth;
Y_{\bf a}= Y_2/Y_1.
\propto= energy coefficient;
\beta = momentum coefficient;<br>b = contraction in breadth;
ΔE
    = energy loss; and
 \mathbf{a}= angle of flared entrance.
Subscripts
   1 = 1 upstream; end 2 = downstreem.
```


# FIG.( 1) EXPERIMENTAL APPARATUS.

 $\bar{\mathcal{I}}$ 

 $\ddot{\phantom{a}}$ 







٠.

FIGE 3 IVARIATION OF INJUNITHER LIFORAbib.





 $\blacksquare$ 





 $C.25$ 



 $\ddot{\phantom{0}}$ 

×.



 $C.27$ 



 $\overline{a}$ 

 $\ddot{\phantom{0}}$ 

l,

 $\ddot{\phantom{0}}$ 





 $\cdot$ 

 $\overline{\phantom{a}}$ 















Plate (1) Sudden contraction



Plate (2) Limited constriction



Plate (3) Flared entrance



Plate (4) Gravel bed