

9-1-2021

Determination of Electromechanical Transient Process Characteristics Using Equation of Variable.

Ibraheem Mansy

Electrical Engineering Department., Faculty of Engineering., El-Mansoura University., Mansoura., Egypt.

Follow this and additional works at: <https://mej.researchcommons.org/home>

Recommended Citation

Mansy, Ibraheem (2021) "Determination of Electromechanical Transient Process Characteristics Using Equation of Variable.," *Mansoura Engineering Journal*: Vol. 21 : Iss. 3 , Article 5.

Available at: <https://doi.org/10.21608/bfemu.2021.159793>

This Original Study is brought to you for free and open access by Mansoura Engineering Journal. It has been accepted for inclusion in Mansoura Engineering Journal by an authorized editor of Mansoura Engineering Journal. For more information, please contact mej@mans.edu.eg.

DETERMINATION OF ELECTROMECHANICAL TRANSIENT PROCESS CHARACTERISTICS USING EQUATION OF VARIABLES

تحديد خصائص الحالات العابرة الكهروميكانيكية باستخدام معادلة المتغيرات

I.I.I.Mansy

Department of Electrical Engineering, Faculty of Engineering
Mansoura University, Mansoura - Egypt.

ملخص البحث:

نتيجة لصعوبة حل المعادلات اللاخطية وكذلك طول الفترة الزمنية المطلوبة لحل مثل هذه المعادلات ، بالإضافة إلى زيادة التعقيدات في الشبكات الكهربائية كان لابد من البحث عن طرق رياضية أخرى عبر تقليدية. لذلك يقدم هذا البحث حلاً جديداً لهذه المشكلة مستخدماً طريقة معادلة المتغيرات. وهذه الطريقة تقريبية تعتمد على فرض قيمة للحل غير خاضعة لأي تغيير. وتتكون هذه المعادلة من عدد من المعاملات، كل معامل له معادلة تتوقف على درجة الحل ويسمى الحل الأول وبتزايد درجة الحل يكون الحل الثاني وهكذا. وفي النهاية يكون الحل التقريبي باستخدام هذه الطريقة عبارة عن مجموع الحل المفروض مضافاً إليه المعاملات. عليه يكون هناك فرق عن الحل المضبوط يسمى بالإنحراف في قيمة المتغير. وباستخدام هذا الإنحراف يمكن الوصول إلى حل دقيق نسبة خطأ لا تتجاوز 2.5% عن الحل المضبوط. وباستخدام هذه الحلول يمكن تحديد الخصائص الكهروميكانيكية للحالات العابرة ويسر وسرعة كبيرة وبدقة عالية.

ولقد تم تقديم وصفاً كاملاً للطريقة المقترحة وكذلك التحليلات الرياضية الخاصة بها، وأيضاً تم ترجمة النتائج التي توصل إليها البحث في حالتي الخطأ البسيط والمتسبب فيه تغير أحد عناصر الشبكة الكهربائية وكذلك الخطأ الكبير نتيجة حدوث قصر أحادي الوجه. وتمت المقارنة بين الطريقة المقترحة وطريقتين أخريتين لتوضيح سرعة الحل. وأيضاً تمت المقارنة بين هذه الطريقة والطريقة المضبوطة والتي وضح منها مدى دقة الطريقة المقترحة.

ABSTRACT

The equation of variables (EV) is an approximation of a mathematical method. It is used to linearize nonlinear equations. It is simple and accurate method and it offers quick solutions. This paper explains this equation and uses it to determine the characteristics of electromechanical transient process (EMTP) in electrical power systems.

The characteristics of EMTP are studied in this paper in two cases: first, simple disturbance (as a result of parameter variation) and second, large disturbance (as a result of occurring single S.C.) In this paper also, a comparison between the proposed method and another three methods is presented. One of these methods has exact solution and the others have an approximate one.

Accepted August 25 / 1996

INTRODUCTION

Due to rapid growth of electrical power systems, over the past few years, stability analysis of the system became extremely difficult, even, using the present day computer facilities. Dynamic stability of electrical power systems stands as a subject of theoretical and practical interest.

Solution of non-linear equations, describing transient processes in power systems using method of optimal control theory directly, is too tedious to apply [1&2].

The output of a conventional transient stability program is analyzed using transient energy functions for individual machines [3].

The stability of power systems can be deduced from the roots of the system characteristic equation [4]. On the other hand, in a nonlinear system, such an inference is invalid [5] because its stability depends upon the initial conditions, as well as, the system parameters.

This paper illustrates the characteristics of EMTP using EV and presents the comparison between EV and those methods introduced in [6].

ANALYSIS SOLUTION OF EV

The error of determination EMTP characteristics with the help of EV may be evaluated. The solution of EV is analyzed in the case of selecting undisturbed and parameter variation system [6]. Using this EV, the nonlinear differential equations will be transformed into second order linear differential equations with constant coefficients. These coefficients are illustrated and determined in [7].

As, in the capacity of parameter variation, the admittance (y) is considered. From [6 & 8] the rotor angle (δ) is:

$$\delta(t, y) = \delta^* + L_1(t)\Delta y + \frac{1}{2!}L_2(t)\Delta y^2 + \dots + R_i, \quad (1)$$

where δ^* - the undisturbed value of δ
 R_i - the remainder of series (1)

$$= L_{i+1}^{(i)}(t)\Delta y^{(i+1)}/(i+1)! + \dots @ \epsilon \Delta y = y - y^* \quad (2)$$

$L_1(t), L_2(t)$ etc. are the first, second etc. solution of EV.

The first EV is presented in [6]. It has the following form:

$$L_1(t) = C_0^{(1)}(1 - \cos\sqrt{a_1}t), \dots C_0^{(n)} = K_0^{(n)}/a_1 = -\tan(\delta^*)/y^* \quad (3)$$

where

$$a_1 = \frac{2\pi f_0}{T_j} E' U^* y \cos \delta^* = \text{const.} \quad (4)$$

$$K_0^{(1)} = \frac{2\pi f_0}{T_j} E' U \sin \delta^* = \text{const.}$$

E' & U - the generator and infinite bus voltages (in p. u.);

T_j - the generator inertia constant ;

y^* the undisturbed value of y (in p.u.)

Analysis of EMTP characteristics is carried-out for the following cases:

i) Undisturbed stable(unstable) solution, standard solution, which is approximated with the help of variable coefficients method (VCM) [6];

ii) Undisturbed stable(unstable) solution, standard solution unstable (stable).

The second EV is

$$\ddot{L}_2 + a_1 L_2 = d_2(t), \quad L_2(0) = \dot{L}_2(0) = 0 \quad (5)$$

$$\text{where} \quad d_2(t) = \frac{\partial^2 f}{\partial \delta^2} L_1^2(t) + 2 \frac{\partial^2 f}{\partial \delta \partial y} L_1(t) \quad (6)$$

From Eq.(6) and Eq.(3)

$$d_2 = K_0^{(2)} + K_1^{(2)} \cos \sqrt{a_1} t + K_2^{(2)} \cos 2\sqrt{a_1} t \quad (7)$$

where; the upper index indicates the order of EV and the lower shows the ratio of argument.

From Eq.(6) and the initial conditions, $d_2(0) = 0$. From this, we get,

$$K_0^{(2)} + K_1^{(2)} + K_2^{(2)} = 0 \quad (8)$$

Integrating the second EV at the initial conditions and substituting in Eq.(7), we have

$$L_2(t) = C_0^{(2)} + C_1^{(2)} \cos \sqrt{a_1} t + C_2^{(2)} \cos 2\sqrt{a_1} t + R_1^{(2)} t \sin \sqrt{a_1} t, \quad (9)$$

where; $L_2(t)$ is determined from coefficients $k_0^{(1)}, k_1^{(2)}, k_2^{(2)}$ using the following expressions:

$$\begin{aligned} C_0^{(2)} &= K_0^{(2)}/a_1, & C_1^{(2)} &= -(C_0^{(2)} + C_2^{(2)}), \\ C_2^{(2)} &= -K_2^{(2)}/3a_1, & R_1^{(2)} &= -K_1^{(2)}/2\sqrt{a_1} \end{aligned} \quad (10)$$

For the third EV

$$\ddot{L}_3 + a_1 L_3 = d_3(t), \quad L_3(0) = 0, \quad (11)$$

where $d_3(t)$ is determined from the following formula:

$$d_3(t) = \frac{\partial^3 f}{\partial \delta^3} L_1^3(t) + 3 \frac{\partial^3 f}{\partial \delta^2 \partial y} L_1^2(t) + 3 \frac{\partial^2 f}{\partial \delta^2} L_1(t) L_2(t) + 3 \frac{\partial^2 f}{\partial \delta \partial y} L_2(t) \quad (12)$$

From Eqns.(12), (3) & (9), we find

$$\begin{aligned} d_3(t) &= K_0^{(3)} + K_1^{(3)} \cos \sqrt{a_1} t + K_2^{(3)} \cos 2\sqrt{a_1} t + K_3^{(3)} \cos 3\sqrt{a_1} t + \\ &M_1^{(3)} t \sin \sqrt{a_1} t + M_2^{(3)} t \sin 2\sqrt{a_1} t \end{aligned} \quad (13)$$

From Eq.(13) and initial conditions, $d_3(0) = 0$. Then

$$K_0^{(3)} + K_1^{(3)} + K_2^{(3)} + K_3^{(3)} = 0 \quad (14)$$

Integrating Eq.(11) at initial conditions and substituting in Eq.(13), we have

$$\begin{aligned} L_3(t) &= C_0^{(3)} + C_1^{(3)} \cos \sqrt{a_1} t + C_2^{(3)} \cos 2\sqrt{a_1} t + C_3^{(3)} \cos 3\sqrt{a_1} t + \\ &R_1^{(3)} t \sin \sqrt{a_1} t + R_2^{(3)} t \sin 2\sqrt{a_1} t + S_1^{(3)} t^2 \cos \sqrt{a_1} t, \end{aligned} \quad (15)$$

where $L_3(t)$ is determined from coefficients $k_0^{(3)}, k_1^{(3)}, k_2^{(3)}, k_3^{(3)}, M_1^{(3)}, M_2^{(3)}$ using the following expressions:

$$\begin{aligned} C_0^{(3)} &= \frac{K_0^{(3)}}{a_1}, & S_1^{(3)} &= \frac{M_1^{(3)}}{4\sqrt{a_1}}, & R_1^{(3)} &= \frac{K_1^{(3)}}{2\sqrt{a_1}} + \frac{M_1^{(3)}}{4a_1}, & C_3^{(3)} &= \frac{K_3^{(3)}}{8a_1}, \\ R_2^{(3)} &= \frac{M_2^{(3)}}{3a_1}, & C_2^{(3)} &= \frac{4M_2^{(3)}}{9a_1\sqrt{a_1}} - \frac{k^{(3)}}{3a_1}, & C_1^{(3)} &= -(C_0^{(3)} + C_2^{(3)} + C_3^{(3)}) \end{aligned}$$

From the previous analysis, the solution of i^{th} EV (general form) is possible to write in the form

$$L_i(t) = \sum_{n=0}^i C_n^{(i)} \cos n\sqrt{a_1}t + t \sum_{n=0}^{i-1} R_n^{(i)} \sin n\sqrt{a_1}t + \dots + t^{i-2} \sum_{n=0}^{i-(i-2)} Y_n^{(i)} \cos n\sqrt{a_1}t + t^{i-1} \sum_{n=0}^{i-(i-1)} Z_n^{(i)} \sin n\sqrt{a_1}t \quad (16)$$

$n=0, 1, 2, \dots, i$

As follows from the obtained equations, the solutions of EV $L_2(t), \dots, L_i(t)$ increase without bound on time increase. These solutions pass unbounded period of time through its initial value.

The performance of the proposed approach is investigated by computer simulation of power system consisting of a single machine connected to an infinite bus through long transmission line. The data and figure of the system are given in [1].

EXAMPLE 1:

In this part, the obtained solutions of EV will be applied on a mathematical example to show the character of approximated standard characteristics. Data of this example are $P_0 = 0.6$ p.u.; $\dot{E}U = 1.2$ p.u.; $T_j = 7$ s.; $\delta = 26$ deg.; $y^* = 1.14$ p.u. Coefficient values of unbounded terms and obtained solutions of first three EV are listed in table 1. Solutions of first three EV depending on time are shown in Fig. 1. With the help of these solutions and the following formula

$$\delta(t, y) = \delta^* + L_1(t)\Delta y + \frac{1}{2!}L_2(t)\Delta^2 y + \frac{1}{3!}L_3(t)\Delta^3 y,$$

we shall consider three approximated standard characteristics EMTP: single phase short circuit (S.C.) $y = 0.34$ p.u., $\Delta y = -0.8$ p.u. (Fig.2); perturbation $y = 0.82$ p.u.; $\Delta y = -0.32$ p.u. (Fig.3); disturbance near to critical value for admittance $y_c = \frac{P_0}{\dot{E}U}$; $y = 0.6$ p.u.; $\Delta y = -0.54$ p.u. (Fig.4). Curves in these figures are obtained with the help of first, second and third EV. Also steady state undisturbed value of angle δ^* and standard characteristic $\delta_0(t)$.

On the basis of analyzed solutions EV, it is possible to describe the characteristics of EMTP. Thus, in the case of S.C., calculate first three EV exact values in large range of angle variations with time (divergence larger than 5 deg. step at 0.58 s. and angle value 160 deg.).

After recovery of S.C. (i.e. parameter variation is decayed), EV and its solutions are varied. Besides initial conditions of these new EV, will be greater than zero ($t = t_{dis}$) where t_{dis} is the removed fault time.

After decaying of parameter variations, the first EV have the following expressions:

$$\begin{aligned} \ddot{L}_1^{(0)} + a_1 \dot{L}_1^{(0)} = 0, \quad L_1^{(0)}(\tau = 0) = L_1(t = t_{dis}) \\ \dot{L}_1^{(0)}(\tau = 0) = \dot{L}_1(t = t_{dis}) \end{aligned} \quad (17)$$

where $\tau = t - t_{dis}$; upper index (0) is meaning that the solutions of EV are after recovery of S.C.

Solution of (17) has the following form

$$L_1^{(0)}(\tau) = A_0^{(1)} \cos(\sqrt{a_1} \tau - \phi_1^{(1)}) \quad (18)$$

where , the upper index indicates identity value for order data of EV; and lower index shows the ratio of solution argument. Solution of amplitude values $A_0^{(1)}$ and its angle $\phi_1^{(1)}$ depends on solution values of

$$\dot{L}_1 + a_1 L_1 = d_1 = k_0^{(1)}; \quad L_1(0) = \dot{L}_1(0) = 0$$

and its first derivative at ending variation moment (t_{dis}). These values are determined as:

$$\phi_1^{(1)} = \arctan \frac{\dot{L}_1(t_{dis})}{L_1(t_{dis})} = \arctan \frac{\sin \sqrt{a_1} t_{dis}}{1 - \cos \sqrt{a_1} t_{dis}}, \quad A_0^{(1)} = \frac{L_1(t_{dis})}{\cos \phi_1^{(1)}} \quad (19)$$

After a little manipulation in expression for solving first EV(18) it is possible to eliminate time τ as follows

$$L_1^{(0)}(t) = A_0^{(1)} \cos(\sqrt{a_1} t - \theta), \quad \theta(t_{dis}) = \sqrt{a_1} t_{dis} + \phi_1^{(1)} \quad (20)$$

Fig.5 shows the relations between coefficient L and time in the case of disconnected S.C. ($t_{dis} = 0.25$ s.). The solution of first EV is also shown in Fig.5 "curve no.1". This curve consists of two parts: first part represents Eq. (3) (from origin point to $t = t_{dis}$) and the second represents Eq.(18) (from $t > t_{dis}$). In Fig. 5, curve no.2 represents the same solution of EV without disconnecting S.C.. Bias quantity of extremal values of these two curves (1 & 2) is equal to

$$\Delta = (\pi - \phi_1^{(1)}) / \sqrt{a_1}$$

Curve no.3 represents the solution in the case of $t = t_{mdis} = \sqrt{a_1} = 0.4229$ s., at which extremal value of $L_m^{(1)} = 2C_0$, is reached.

For the second EV

$$\ddot{L}_2^{(0)} + a_1 L_2^{(0)} = d_2(\tau), \quad L_2^{(0)}(\tau=0) = L_2(t=t_{dis}) \quad (21)$$

$$\dot{L}_2^{(0)}(\tau=0) = \dot{L}_2(t=t_{dis})$$

where

$$d_2(\tau) = \frac{\partial^2 f}{\partial \delta^2} L_1^{(0)'}(\tau) = l_{0c}^{(2)} + l_{2c}^{(2)} \cos 2\sqrt{a_1}\tau + l_{2s}^{(2)} \sin 2\sqrt{a_1}\tau \quad (22)$$

The right hand side of Eq.(22) is accomplished with the substitution of solution in Eq.(18). Integrating the second EV at given initial conditions and using Eq.(22), we obtain

$$L_2^{(0)}(\tau) = A_0^{(2)} + A_1^{(2)} \cos(\sqrt{a_1}\tau - \phi_1^{(2)}) + A_2^{(2)} \cos(2\sqrt{a_1}\tau - \phi_2^{(2)}) \quad (23)$$

The solution of amplitudes and phases of Eq. (23) are determined through coefficients $l_0^{(2)}, l_{2c}^{(2)}, l_{2s}^{(2)}$ as follows:

$$A_0^{(2)} = \frac{l_0^{(2)}}{a_1}, \quad \phi_1^{(2)} = \arctan \frac{L_2(t_{dis}) + 2l_{2c}^{(2)}/3\sqrt{a_1}}{L_2(t_{dis})\sqrt{a_1} - (l_0^{(2)} - l_{2c}^{(2)}/3)/\sqrt{a_1}}$$

$$\phi_2^{(2)} = \arctan \frac{l_{2s}^{(2)}}{l_{2c}^{(2)}}, \quad A_1^{(2)} = [L_2(t_{dis}) - (l_0^{(2)} - l_{2c}^{(2)}/3)] / \cos\phi_1^{(2)}; \quad (24)$$

$$A_2^{(2)} = l_{2c}^{(2)} / (3a_1 \cos\phi_2^{(2)})$$

The solution of i^{th} EV after disconnecting S.C. may be written as follows:

$$L_i^{(0)}(\tau) = A_0^{(i)} + \sum_{n=1}^i A_n^{(i)} \cos(n\sqrt{a_1}\tau - \phi_n^{(i)}) + \tau \sum_{n=2}^i Q_{n-2}^{(i)} \cos[(n-2)\sqrt{a_1}\tau - \phi_{n-2,0}^{(i)}] +$$

$$\tau^2 \sum_{n=3}^i V_{n-3}^{(i)} \sin[(n-3)\sqrt{a_1}\tau - \phi_{n-3,1}^{(i)}] + \dots \quad (25)$$

where $n=1,2,\dots,i$.

The final admittance variations for i^{th} solution of i^{th} EV are

$$L_i = \begin{cases} L_i(t), 0 < t < t_{dis}, & \text{asin Eq.(16)} \\ L_i(t_{dis}) = L_i^{(0)}(\tau=0), t = t_{dis} \\ L_i^{(0)}(\tau), t_{dis} < t < t_{dr}, \tau = t - t_{dis} & \text{asin Eq.(25)} \end{cases} \quad (26)$$

Notice that the obtained expressions are possible to apply by considering a series number of iterations. Corresponding initial conditions are very necessary to be computed continuously.

EXAMPLE 2:

In this section, consider a numerical example to indicate the behaviour of approximate characteristics after decaying of parameter variations. We used the same data in the previous example. Fig.6 shows the solutions L_1, L_2 & L_3 , which are determined from Eq.(26), at $t_{dis} = 0.25$ s.. From this figure, we notice that the curves from origin point to $t=t_{dis}$ are as in Fig. 1. Amplitude and phase values of corresponding solutions, which are determined from Eqns.(19),(24),...,are given in table 2.

Fig.7 & Fig.8 show approximate curves(time interval 0.05 s) δ_0 with the help of L_1, L_2 & L_3 (curves 1,2&3). Fig.7 shows the disconnecting single phase S.C. process ($y=0.34$ p.u., $\Delta y=-0.8$ p.u.) within 0.25 s., but Fig.8 shows finishing parameter variations ($y=0.82$ p.u., $\Delta y=-0.32$ p.u.) within 0.25 s. Also, these figures show the undisturbed angle value δ^* .

A comparison between the proposed and exact solutions of the problem under study in the case of system parameter variation is shown in Fig. 9 This figure shows that the error of the proposed solution may be neglected.

FINAL RESULTS ANALYSIS:

As we conclude from figures, the obtained analytical solutions Eq.(26) permit, steady-state solutions give good approximate characteristics EMTP at disconnecting S.C. (finished admittance variations). In addition, in the case of small variations, curves L_2, L_3 practically coincide with standard curve in Fig.8. But in the case of S.C. Sequence of using EV may achieve an accuracy near to standard characteristics $\delta_0(t)$.

An approach to obtain the family of EMTP characteristics with the help of corresponding EV analytical solutions, at steady-state undisturbed values, have series of advantages in comparison with the other methods.

As shown from table 3, the proposed method solves the example under study in 1.5 sec.. Also, the method is very fast compared with the other methods.

CONCLUSIONS:

From the previous analysis, figures and results, we conclude the following:-

- 1-With the help of EV solutions, characteristics family may be rapidly obtained. Rapidity of this method is greater than interval sequence method (nearly 10 times) and from 20 to 25 times greater than conventional method in [6].
- 2-In the case of steady-state, undisturbed values can describe undisturbed transient process.
- 3- This method is simple, responding and accurate.
- 4- This method is applied on a simple electrical system (generator with infinite bus.).
- 5- Comparing the results of this method with the exact solution, we find that the error of this method may be neglected.

Table 1

i	$K_0^{(i)}$	$K_1^{(i)}$	$K_2^{(i)}$	$K_3^{(i)}$	$M_1^{(i)}$	$M_2^{(i)}$	
1	-1352.7						
2	2796.5	-2937.7	141.13				
3	-9484.8	10178.7	-707.9	47.9	-35632.4	-3424.7	
i	$C_0^{(i)}$	$C_1^{(i)}$	$C_2^{(i)}$	$C_3^{(i)}$	$R_1^{(i)}$	$R_2^{(i)}$	$S_1^{(i)}$
1	-24.51						
2	50.68	-49.83	-0.85		-198.19		
3	-171.9	164.11	7.91	-0.13	846.4	20.71	-1199.1

Table 2

i	$A_0^{(i)}$	$A_1^{(i)}$	$A_2^{(i)}$	$A_3^{(i)}$	$Q_1^{(i)}$	$\phi_1^{(i)}$	$\phi_2^{(i)}$	$\phi_3^{(i)}$	$\phi_{10}^{(i)}$
1	-39.25					36.6			
2	6.56	41.31	-2.19			-72.94	-73.55		
3	-16.73	38.51	-6.9	-0.45	72.21	65.4	70.25	70.35	53.19

Table 3

Excution time comparison for the proposed method and other methods

Methods	Time in sec.
proposed method	1.3
interval seq. method	14.35
approximation method in [6]	33.52

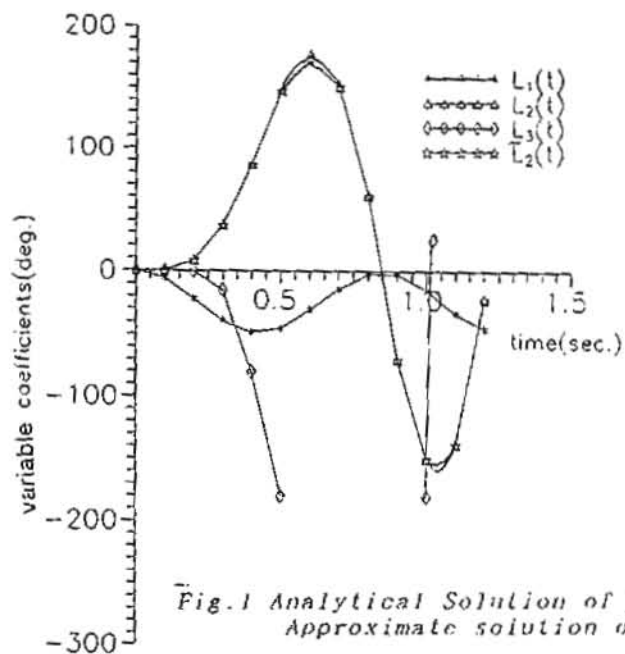


Fig.1 Analytical Solution of First EV and the Approximate solution of Second EV.

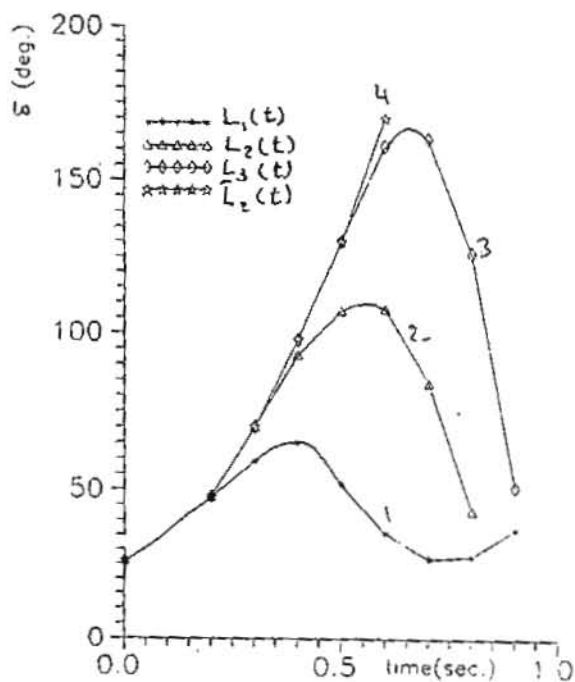


Fig.2 Approximate Characteristics of EMTP With the Help of Analytical solutions for a System Parameter Variation ($\delta y = -0.8$)

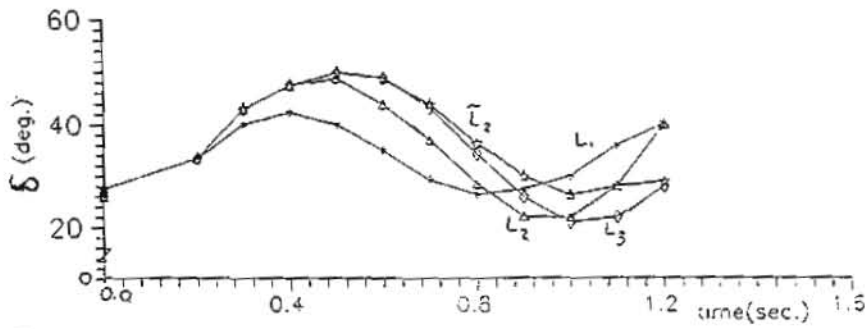


Fig.3 Approximate Characteristics of EMTF With the Help of Analytical solutions for a System Parameter Variation ($\Delta y = -0.32$)

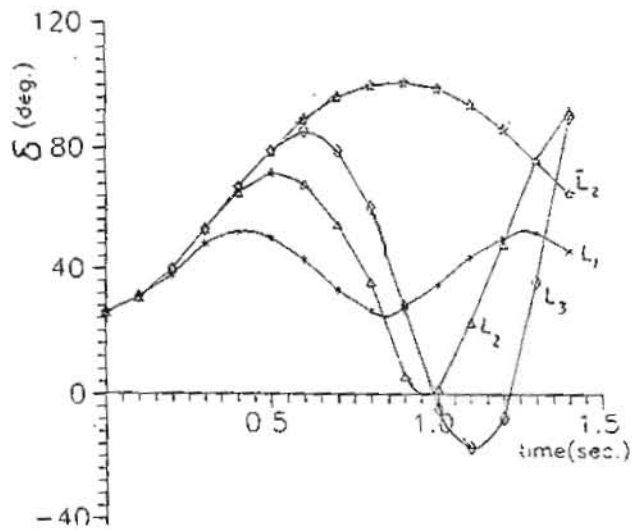


Fig.4 Approximate Characteristics of EMTF With the Help of Analytical solutions for a System Parameter Variation ($\Delta y = -0.54$)

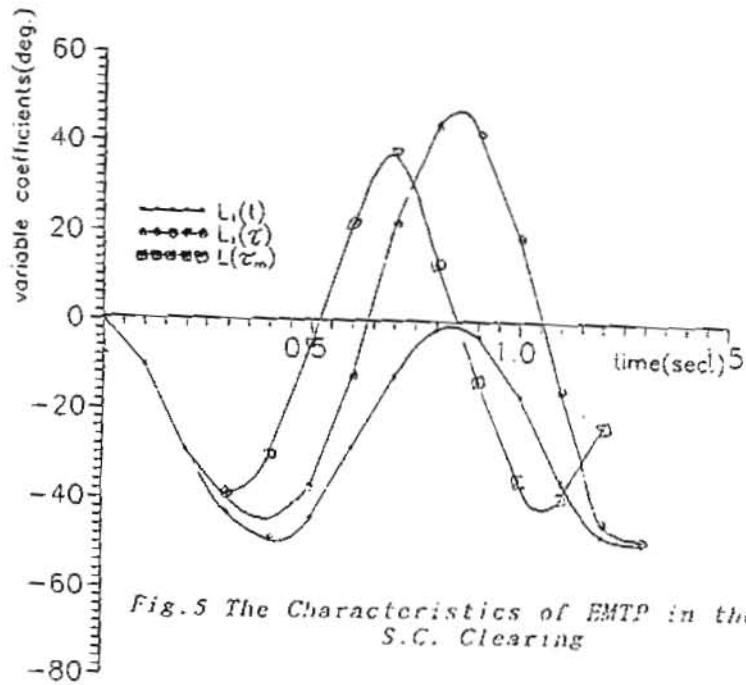


Fig.5 The Characteristics of FMTF in the Case of S.C. Clearing

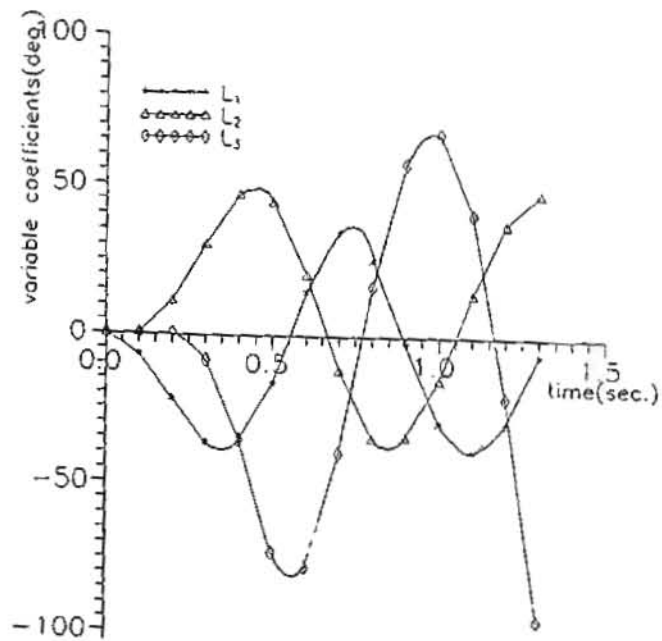


Fig.6 Analytical Solution of First IV at Disconnecting S.C.

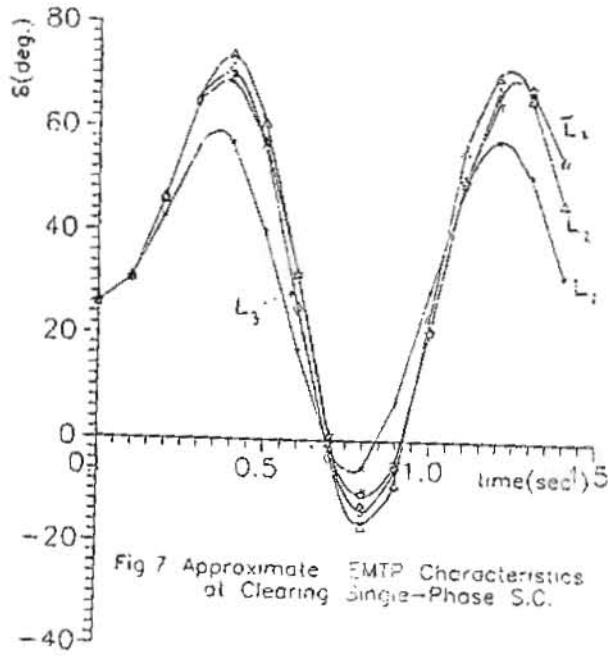


Fig 7 Approximate EMTP Characteristics of Clearing Single-Phase S.C.

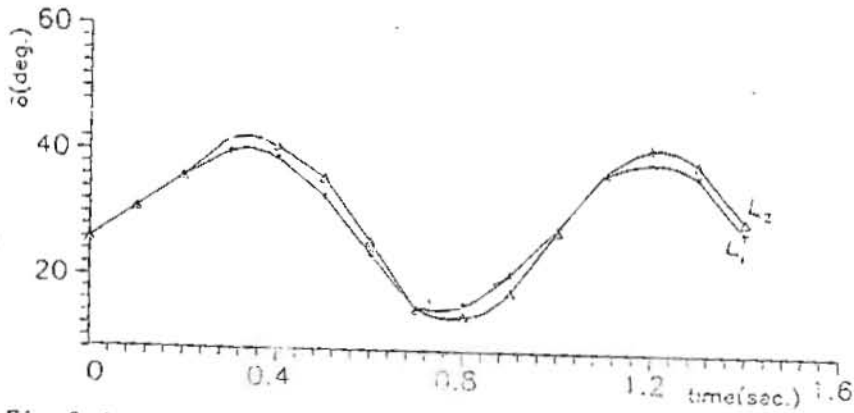


Fig.8 Approximate EMTP Characteristics following removal of Parameter Variations

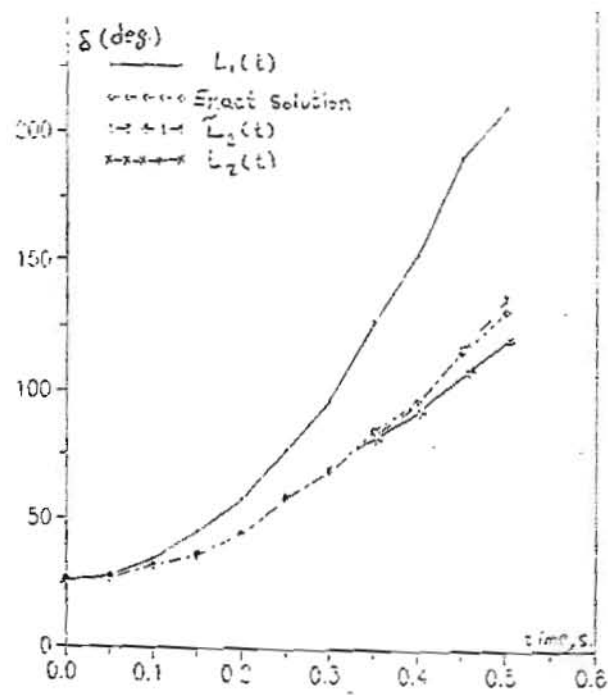


Fig.9 Approximate and Exact characteristics of EMTF

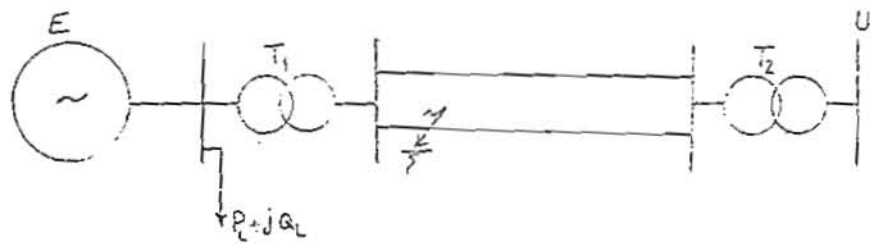


Fig.10 System under study (Generator and Infinite-Bus)

REFERENCES:

- 1- F.F. Areed and others " Optimal Control of Electrical Power Systems Using Maximal Principle." , 13th International Congress for Statistics, Computer Science, Social and Demographic Research, March, 1988, pp. 215-228.
- 2- V.A. Venikov "Electromechanical Transient Process in Electrical systems.", Higher School, 1985, 415 p.
- 3- A.A. Fouad and others "Transient Stability Program Output Analysis" IEEE Trans. on Power Systems, Vol. PWRS-1, No.1, Feb., 1986, pp. 2-9.
- 4- I.I.I. Mansy "Predicting the Transient Stability of Ceps Using AES Method." Mansoura Engineering Journal (MEJ), Vol.14, No.2, Dec., 1989, pp. E.30-E.39.
- 5- H.W. Dommel and N. Sato "Fast Transient Stability Solutions", IEEE Trans. Apparatus and Systems, Vol. PAS-86, July/Aug., 1972, pp.253-260.
- 6- I.I.I. Mansy "Method Development for Determining Control Actions, Which Improve Transient Processes in Egyptian Power System." PHD Thesis, 1985.
- 7- I.I.I. Mansy and A.E.E. Ibrahim "Stability Analysis of Power System Using DSM", Mansoura Engineering Journal (MEJ), Vol.14, No.2, Dec. 1989, pp. E.51 -E.62.
- 8- I.I.I. Mansy and A.M.M. Aiy "Electromechanical Transient Processe Analysis In Electrical Systems With the Help of Equation in Variations.", 19th International Conference on Statistics, Computer Science and Applications , April , 1994, pp.160-171.