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Matching of PV Power Systems with Electrical Loads Using Graph Theoretic Modeling Approach.

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MATCHING OF PV POWER SYSTEMS WITH ELECTRICAL LOADS USING GRAPH THEORETIC MODELING APPROACH

مواعمة نظم القوى الشمسية الفوتوفولتية مع الأحمال الكهربية باستخدام طريقة نمذجة المخططات النظرية

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<u>خلاصة:</u>

تعتبر المواعمة بين الخلايا الفوتوفولنية والأحمال الكهريية التي تغذيها من أهم العوامل التي تؤثر في كفاءة أداء المنظومة الفوتوفولتية والاستفادة القصوى من الطاقة الناتجة عن الخلايا. وفي حالة المواعمة الجيدة بين الخلايا والأحمال يكون منحنى التحميل قريبا من منحني القدرة القوى الناتجة عن الخلايا عند قيم إشعاع مختلفة.

ويقدم هذا البحث طريقة جديدة لمواعمة نظام شمسي مكون من منظومة خلايا فوتوفولتية مستقلة تغذى حمل ميكانيكي من خلال محرك تيار مستمر. وقد تم استنباط وتطوير برنامج كومبيوتر بلغة MATLAB 6 لتمثيل المكونات المختلفة للنظام بطريقة نمذجة المخططات النظرية. ومن ثم تطبيق هذا البرنامج على عدد من دراسات الحالة لأنواع مختلفة من محركات التيار المستمر والأحمال الميكانيكية والمقارنة بينها للوصول إلى افضل مواعمة بين الخلايا وكل نوع من أنواع الأحمال.

ABSTRACT

The quality of load matching in a photovoltaic power system (PVPS) determines the system performance and the degree or the solar cells utilization. In a good matched system, the operation of the load-line is close to the maximum power-line of the solar cell (SCA) generator. This paper presents a new methodology for modeling a stand alone PVPS using the Graph Theoretic Modeling (GTM) Approach. The studied system composed of a directly connected SCA generator-dc motor supplying different load types. A computer program (written in MATLAB 6) has been developed to model the studied system. The computer program is then applied to nine case studies for different types of dc-motors and various mechanical loads. A comparison between these cases is introduced to indicate the appropriate motor type for each load.

1. INTRODUCTION

The quality of load matching in a photovoltaic power system (PVPS) determines the system performance and the degree or the solar cells utilization. In a good matched system, the operation of the load-line is close to the maximum power-line of the solar cell (SCA) generator. Computer simulation for the operation and sizing of photovoltaic (PV) components is a very thorough method of determining the behavior of PVPS. Using simulation methods the electrical power output can be optimized with respect to component sizes. A method of detailed modeling and simulation must be available before the issue of optimum sizing is adequately pursued. The topics of modeling and simulating PV powered systems which, include PV array, DC motor and mechanical load was well documented in [1], [2], and [3]. An investigation of directly coupled photovoltaic pumping connected to a large absorber field through modeling and simulating PV array, dc motor,

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centrifugal pump and the absorber field was presented in [4]. Detailed modelings of Photovoltaic system components using TRANSYS program were analyzed in [5]. Whereas, Ref. [6] applied the TRNSYS program to a large scale PVPS used for water heating and expanded the model to add more components to the program. Ref [7] investigated the long-term performance of PV pumping system with a maximum power point tracker. The operation characteristics of dc-permanent, series motor and shunt motor with a centrifugal load was presented and compared in [8]. A mathematical methodology for the optimum configuration of photovoltaic pumping system in a solar domestic hot water was investigated in [9]. One of the widely accepted network theories is the Graph Theoretic Modeling (GTM) Approach. The GTM approach has been in use since 1955. It has emerged as a method that allows the modeling and solving of systems that are hydraulic, pneumatic, structural, mechanical and thermal or combination thereof [10]. A method for modeling the directly-connected stand-alone PVPS using GTM method was introduced in Ref. [11]. The paper presented an approach to reduce the computational efforts needed in setting up the required equations. The GTM approach was applied to a PV powered ventilator system and a PV powered pumping system [11].

This paper applies a comprehensive study of applying the GTM approach to a directly connected SCA generator to supply different load type. The load may be constant, ventilator or centrifugal pump. Whereas, the used dc motor may be series, separately excited or shunt motor. The system components are modeling using GTM approach to generate a nonlinear system of equations called Newton-Raphson Mixed Nodal Tableau (NR-MNT). The equations are then solved numerically by developing a computer program written in MATLAB 6. A comparison between the different case studies is achieved based on the quality of load matching for each case.

2- SOLVING NONLINEAR SYSTEMS USING GTM APPROACH

The GTM approach provides a set of equations that characterize the individual components of the system. The component is the smallest indivisible element of our interest within a system. The behavior of a component can be characterized by using two types of variables [11]:

- Through variables (y): quantify flow process such as current, torque and flow rate.
- Across variables (x): quantify the stimulus causing flow such as voltage, speed and hydraulic head.

For modeling a combined PV-dc motor system, components of electrical, mechanical and hydraulic are encountered. When the components are replaced by their terminal graphs, the resulting diagram is called **system graph**. The system graph depicts the connectivity of components without any ambiguity. The system graph can be easily converted into a matrix form *(incident matrix)* to indicate the connectivity of the system components. The incident matrix performs this task through the use of +1, -1&0's. Rows and columns represent the individual nodes and edges, respectively. With the help of the incident matrix both the *vertex* and the *nodal transformation* equations are evolved. The vertex equations stem from a generalization of Kirchoff's current law (to incorporate systems other than electrical networks). This matrix ensures the conservation of flow at each node and appears as:

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$$\begin{bmatrix} A_o & A_c & A_r & A_t \end{bmatrix} \begin{bmatrix} Y_o \\ Y_c \\ Y_r \\ Y_t \end{bmatrix} = \begin{bmatrix} 0 \end{bmatrix}$$
(1)

Where: A_a and A_r are across and variable sources respectively. A_c and A_r , are conductive and resistive portions of constitutive components respectively. The vectors with Y represent the set of all the through variables y partitioned analogous to the incidence matrix A corresponding to the component types. The nodal transformation equations provide the relationship between component across variables (X_a, X_c, X_r, X_t) to the nodal across variables (X_n) . The vectors with X represent the collection of across variables X partitioned analogous to the incidence matrix A corresponding to the component type.

$$\begin{bmatrix} X_o \\ X_c \\ X_r \\ X_i \end{bmatrix} = \begin{bmatrix} A_a^T \\ A_o^T \\ A_i^T \\ A_i^T \end{bmatrix} * X_n$$
(2)

These two sets of equations give rise to a system of equation known as *Mixed Nodal Tableau (MNT)* [11]. The MNT system of equations is formulated to find a set of variables that once solved, is sufficient to calculate all other system variables. For linear systems the MNT is a system of equations summarizing the behavior of the system. For nonlinear systems the same set of equations is used to formulate the *Newton Raphson Mixed Nodal Tableau (NR MNT)*, which have to be solved iteratively, explained later. Expanding Eq. (1) and substituting for Y_c with the conductive vector G_c , the vertex equation can be rewritten as:

$$A_a Y_a + A_c G_c + A_t Y_t + A_t Y_t = 0$$
(3)

Where the values of through sources Y_t are known. Using the identity for X_c in Eq. (2), and substituting X_r for the resistive vector P_r , the following can be written as :

$$A_r^T X_n - P_r = 0 \tag{4}$$

By using the identity of X_a from Eq.(3), a third set of equations using a generalization of Kirchoff's voltage law, can be written as:

$$A_a^{\ \prime} X_n - Xa = 0 \tag{5}$$

Where the values of the across sources X_a are known. Equations (3)-(5) can consolidated and designated as the MNT F(z) which represent a set of nonlinear equations in which there are the same number of unknown variables $Z^T = [X_n^T Y_r^T Y_a^T]$ as the number of equations:

$$[F(z)] = \begin{bmatrix} f_1(z) \\ f_2(z) \\ f_3(z) \end{bmatrix} = \begin{bmatrix} A_c G_c + A_r Y_r + A_o Y_o + A_t Y_t \\ A_r^T X_n - P_r \\ A_o^T X_n - X_o \end{bmatrix}$$
(6)

The Newton-Raphson method is used to solve this system of non linear equations as follows:

$$\frac{\partial F(z)}{\partial z^{T}}\Big|_{z=z^{k}} \Delta z^{k-1} = -F(z)\Big|_{z=z^{k}}$$

$$\tag{7}$$

where Δz^{k+1} is given by $(z^{k+1} - \Delta z^k)$ in which z^k is the $k \stackrel{th}{=}$ iterative guess for z. The Jacobian can be written as:

$$F^{1z} = \frac{\partial F(z)}{\partial z^{T}} = J\{F(z)\} = \begin{bmatrix} \frac{\partial f_{1}(z)}{\partial X_{n}^{T}} & \frac{\partial f_{1}(z)}{\partial Y_{r}^{T}} & \frac{\partial f_{1}(z)}{\partial Y_{n}^{T}} \\ \frac{\partial f_{2}(z)}{\partial X_{n}^{T}} & \frac{\partial f_{2}(z)}{\partial Y_{r}^{T}} & \frac{\partial f_{2}(z)}{\partial Y_{n}^{T}} \\ \frac{\partial f_{3}(z)}{\partial X_{n}^{T}} & \frac{\partial f_{3}(z)}{\partial Y_{r}^{T}} & \frac{\partial f_{3}(z)}{\partial Y_{n}^{T}} \end{bmatrix}$$
(8)

Where F^{tz} is a notation for the first order partial derivative of the MNT equations F(z) with respect to the transpose of the vector z.

Throughout this paper a similar notation is used in which a^{lb} is the first order partial derivative of a with respect the transpose of vector b. Using this notation (7) can be expanded and written as:

$$F^{1z}\Big|_{z=z^{k}} z_{k+1} = -F(z)\Big|_{z=z^{k}} + F^{1z}\Big|_{z=z^{k}} z_{k}$$
(9)

By performing the operation indicated in Eq. (9) on Eq. (6), the NR MNT system of equations is found as:

$$\begin{bmatrix} A_{c}G_{c}^{1X_{c}}A_{c}^{T} & A_{c}G_{c}^{R_{r}} + A_{r} & A_{a} \\ A_{r}^{T} - P_{r}^{1X_{c}}A_{c}^{T} & -P_{r}^{1Y_{r}} & 0 \\ A_{a}^{T} & 0 & 0 \end{bmatrix}_{X_{r}=A_{r}^{T}X_{r}^{K}}^{X_{r}=A_{r}^{T}X_{r}^{K}} \begin{bmatrix} X_{n}^{k+1} \\ Y_{r}^{k+1} \\ Y_{a}^{k+1} \end{bmatrix} = \begin{bmatrix} -A_{c}G_{c} + A_{c}G_{c}^{1X_{r}}A_{c}^{T}X_{n} + A_{c}G_{c}^{1Y_{r}}Y_{r} - A_{t}Y_{t} \\ P_{r} - P_{r}^{1X_{r}}A_{c}^{T}X_{n} - P_{r}^{1Y_{r}}Y_{r} \\ X_{a} \end{bmatrix}_{X_{r}=A_{r}^{T}X_{n}^{k}}^{X_{r}=A_{r}^{T}X_{n}^{k}}$$
(10)

Where [NR MNT] or [NR R] is used, it refers to the left side matrix and the right side vector, respectively. When NR MNT is mentioned, it refers to the entire system of equations.

Eq. (10) can be solved iteratively by evaluating:

$$\begin{bmatrix} X_n^{k+1} \\ Y_r^{k+1} \\ Y_a^{k+1} \end{bmatrix} = \begin{bmatrix} NR & MNT \end{bmatrix}^{-1} \begin{bmatrix} NR & R \end{bmatrix}$$
(11)

3- APPLYING THE GTM APPROACH TO COMBINED PV-DC MOTOR SYSTEMS

Any system consists of different components; each component has its behavior and its special characteristics that can be replaced by a stamp on behalf this component. By modeling any component using the GTM approach we can create a stamp of each one by identifying the following items:

- · Schematic diagram,
- · Component type,
- · System terminal graph,

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- System incident matrix,
- · System terminal equation,
- · Newton Raphson Mixed Nodal Tableau [NR MNT] and
- Newton Raphson Reduction [NR R].

3-1 Steps of Applying GTM Approach to a System

In this paper we will apply the GTM approach to a combine PV-dc motor system supplying different mechanical load types to obtain the optimum utilization of solar radiation. Following are the main steps required to apply the GTM approach on any system:

1. Draw the terminal graph of the system.

- The "component terminal graph" represents the combination of all edges (line segments) and nodes (end points of edges) associated with a single component are drawn. The components are then replaced by terminal graph, and the resulting diagram of nodes and edges express "system graph".
- The "incident matrix" is formulated using the system graph, which depicts the connectivity of components without any ambiguity.
- The nodes are designated by letters and the edges are designated by numbers.

2. Identify the system terminal equations.

- The across and through variables mathematical relations for each component are expressed.
- The number of terminal equations of the system is equal to the dimension of "NRMNT" matrix.
- "Across variables" denotes the stimulus causing flow such as (V,H,ω)
- "Through variables" denotes flow process such as (LQ,T).

3. Create incident matrix:

• The incident matrix connects the system components through the use of +1, -1, and

0s. The individual a_{ij} th element of the incident matrix A is given a value as follows:

$$a_{y} = \begin{cases} 0\\ 1\\ -1 \end{cases} \text{ if the j th edge is } \begin{cases} not incident on\\ incident and towards\\ incident on and away from \end{cases} \text{ the i th node}$$

• If the component does not exist, the corresponding sub-matrix altogether is omitted from the matrix; the datum nodes are omitted from the matrix because they offer redundant information.

$$A = \begin{bmatrix} A_a & A_c & A_r & A_l \end{bmatrix}$$

4. Get the variables

The variables include the across, through, and nodal across variables: Across variables $[X_a: X_c: X_r(P_c): X_t]$

Through variables $[Y_a: Y_c(g_c): y_r: y_t]$ Nodal across variable $[X_n]$

Where

- (X_a, Y_a) complementary pair associated each other, (X_a) presents across source such as voltage source and static head [V_{in}], [H_{static}], (Y_a) complement pair of [X_a].
- (X_c, Y_c) (Y_c) conductive portion of constitutive component (motor or pump) such as: current, torque and flow rate related to the motor or the pump, (X_c) often not included.
- (P_r, Y_r) (P_r) resistive portion of constitutive component such as the input voltage of a motor or the input speed of a pump, (Y_r) complement pair array of (P_r) .
- $(X_t; Y_t)$ (Y_t) through sources such as current source (I_{ph}) or constant torque source (T_{const}) (X_t) complement pair of (Y_t) not included across variable (X_n) at each node such as $(V_a; \omega_h; H)$.

5. Formulate the [NR MNT] and [NR R]

Use the system equations and the variables of the system to substitute in the Jacobean matrix Eq. (8) to get the [NR MNT], then substitute in Eq. (9) to get Newton Raphson Reduction [NR R].

6. <u>Numerically Solve the problem</u>

The [NR MNT] and [NR R] are solved numerically by developing a MATLAB computer program to get the sufficient parameters to characterize the system (V, I, T, ω , H, Q). These parameters are then used to compute the electrical output power of SCA generator (P_{elect}), the mechanical output power of the dc motors (P_{mech}), the hydraulic power of the pump (P_{hyd}), and the system efficiency (η) and utilization (μ) as we will explain in the following sections.

3-2 Modeling of Combined PV-DC Motor Systems Using GTM Approach

Load types may be connected to the SCA generator-dc motor combination according to the required application. The main purpose of this paper is to indicate the quality of load matching for different mechanical load types connected to dc motors and powered by SCA generator for optimum utilization of solar radiation using (GTM) technique. The dc motors can be classified, according to the type of field excitation, into: series, permanent magnet, shunt and separately excited motors. Permanent magnet motors have similar equations as separately excited ones in case of constant field current. The widely used mechanical load types can be categorized as: constant load, ventilator load and centrifugal pump. The following section will analyze each of the three load connected to different motor types to compromise suitable matching. The results are used to compare between different case studies.

3-2-1 SCA generator modeling

 $\sigma = KT/q$

The SCA generator can be modeled as a current source in parallel to a diode. Series resistance (R_s) accounts for the total resistance at the PV cell/wire contact interface as shown in Fig. 1-a. The current through the diode can be expressed as:

$$I_1 = I_o(e^{V_1/\sigma} - 1)$$
(13)

Where:

- σ : Thermal voltage, 1/volt
- K : Botzman constant
- T : Absolute temperature in Kelvin
- q : Electron charge, Coulomb
- I_o : Reverse Saturation current, A

The current through the series resistance is $I_2 = V_2 / R_s$ as shown in Fig. 1-a.

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3-2-2 Terminal equations of dc motors

The (GTM) methodology deals with the motor as a 4-terminal constitutive component due to the transuding nature of the motor which, converts electrical energy to mechanical energy. The input of the motor is the voltage gained from SCA should be in resistive form i.e. $[P_r]=[V_3]$ whereas, the output of the motor (the electromagnetic torque delivered to the load) should be in conductive form i.e. $[G_c] = [T_4]$. The subscript (3) and (4) denotes to voltage and torque edges. The voltage and torque equations representing the dc motors can be drawn as [8]:

i) Séries motors

$$V_3 = M_{af} I_3 \omega_4 + R_a I_3$$

$$T_4 = -M_{af} I_3^2 + B \omega_4$$
(14)

ii) Separately exited motors

$$V_3 = c_e \omega_4 + R_a I_3$$

$$T_4 = -c_e I_3 + B \omega_4$$
(15)

iii) Shunt motors

$$V_{3} = \left(\frac{R_{a}R_{f}}{R_{a}+R_{f}-M_{af}\omega_{4}}\right)I_{3}$$

$$T_{4} = \left(\frac{M_{af}(R_{f}-M_{af}\omega_{4})}{R_{a}}\right)\left(\frac{R_{a}}{R_{a}+R_{f}-M_{af}\omega_{4}}\right)^{2}I_{3}^{2}$$
(16)

Where

 ω_4 , T₄: Motor output speed and torque (at edge 4),

3-2-3 Modeling of different load types

a) Constant Load Torque

In steady state operation, the electromagnetic torque value is the summation of the constant load torque plus mechanical losses so that: T_i = constant. The schematic diagram of the constant load torque and the system graph is shown in Fig 1-a, 1-b.



Fig. 1 Schematic diagram and system graph of constant load powered by SCA generator

The incident matrix of this system is:

The *variables* required to solve the NRT MN system of equations are:

$$P_{r} = \begin{bmatrix} V_{3} \end{bmatrix} ; \quad \mathbf{G}_{c} = \begin{bmatrix} I_{1} \\ I_{2} \\ T_{4} \end{bmatrix} ; \quad \mathbf{X}_{n} = \begin{bmatrix} V_{a} \\ V_{b} \\ \omega_{c} \end{bmatrix} ; \quad \mathbf{y}_{r} = \begin{bmatrix} I_{3} \end{bmatrix} ; \quad \mathbf{y}_{1} = \begin{bmatrix} I_{PH} \\ T_{6} \end{bmatrix}$$

The resistive portion variable and the conductive portion variable of each constitutive component such as the motor or the pump $[P_r]$, $[G_c]$ respectively, should be identified because they are the heart of the Jacobean matrix (as illustrated by Eq. (8)). The other variables $[X_n]$, $[y_r]$ and $[y_n]$ are the sufficient variables needed to characterize the system.

b) Ventilator load torque

This load consists of a dynamic torque T_5 and a static torque T_6 and is given by:

$$T_5 = b_f \omega_5^{c_f} \qquad \qquad T_6 = a_f \tag{17}$$

where:

 ω_5 , T₅ : Input speed and torque to the centrifugal pump (at edge 5),

a_f : Static torque constant

bf : Dynamic torque constant

cf : C factor

The schematic diagram and system graph are shown in Fig. 2.



Fig. 2 Schematic diagram and system graph of ventilator load powered by SCA generator

The incident matrix of this system is:

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The *variables* required to solve the NRT MN system of equations are: $\begin{bmatrix} r \\ r \end{bmatrix}$

$$P_{i} = \begin{bmatrix} I_{1} \end{bmatrix} \quad ; \quad \mathbf{G}_{e} = \begin{bmatrix} I_{1} \\ I_{2} \\ T_{1} \end{bmatrix} \quad ; \quad \mathbf{X}_{u} = \begin{bmatrix} V_{a} \\ V_{b} \\ \boldsymbol{\omega}_{v} \end{bmatrix} \quad ; \quad \mathbf{y}_{r} = \begin{bmatrix} I_{1} \end{bmatrix} ; \quad \mathbf{y}_{1} = \begin{bmatrix} I_{PH} \\ T_{b} \end{bmatrix}$$

c- Centrifugal pump load

The centrifugal pump is the most popular type used in a PV-pumping system. The motor converts the electrical energy into mechanical energy. The pump converts mechanical energy into hydraulic energy with static head. The terminal equations to represent the operation of the pump can by given by:

$$\omega_{5} = \omega_{ref} \sqrt{\frac{H_{6}}{a_{sT}}} \qquad \qquad Q_{6} = \frac{\eta \,\omega_{5} T_{5}}{\rho g H_{6}} \tag{18}$$

where:

Q6 Rated flow charge, liter/min

- η Pump efficiency, %
- p Fluid Density, KG/m3
- g Gravitational constant
- asr Static a factor

H₆ Rated head, m

The pictorial representation, schematic diagram and system graph are shown in Fig. 3.





The incident matrix of this system is:

		A_a		1	4,		Å	r	Α,	
		7	ł	2	4	6	3	5	8	
	а	0	1	1	0	0	0	0	-1	
	b	0	0	-1	0	0	Ιī	0	0	
A =	С	0	0	0	1	0	0	1	0	
	d	1	0	0	0	1	0	0	0	

The variables required to solve the NRT MN system of equations are:

$$\begin{bmatrix} P_r \end{bmatrix} = \begin{bmatrix} V_3 \\ \omega_5 \end{bmatrix}, \begin{bmatrix} G_o \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \\ T_4 \\ Q_6 \end{bmatrix}, \begin{bmatrix} X \end{bmatrix} = \begin{bmatrix} V_a \\ V_b \\ \omega_c \\ h_d \end{bmatrix}, \begin{bmatrix} X_a \end{bmatrix} = \begin{bmatrix} h_{sianc} \end{bmatrix}, \begin{bmatrix} Y_r \end{bmatrix} = \begin{bmatrix} I_3 \\ T_5 \end{bmatrix}, \begin{bmatrix} Y_a \end{bmatrix} = \begin{bmatrix} Q_7 \end{bmatrix}, \begin{bmatrix} Y_i \end{bmatrix} = \begin{bmatrix} I_{ph} \end{bmatrix}$$

4- ANALYSIS OF LOAD MATCHING WITH DIFFERENT MOTOR TYPES USING GTM APPROACH

The quality of load matching for PVPS is a measure of performance quality and degree of the solar cell utilization efficiency. In good matched systems the operation of the load line is close to maximum power line. In this paper the quality of load matching, Q_l is defined as the area under the mechanical load curve with respect to the maximum power line curve. Nine case studies are presented in this section. For each case study, the system components are modeled using GTM approach. Then they are converted to NR MNT and NR R matrices and numerically solved to get (V, I, T, ω) which are sufficient to characterize the system. These parameters are then used to compute the electrical output power of SCA generator, the mechanical output power of the dc motors and the system efficiency and utilization. A computer program is developed to solve these equations numerically using MATLAB 6. The motor, load and SCA generator data used for this study are given in the Appendix.

Following are the final forms of NR MNT and NR R matrices, the input parameter used for each case study, and the results obtained after applying the computer program. Tables 1-3 illustrate the output results, whereas, Figs. 4-9 show the characteristics and the utilization curve for different case studies.

4-1 A Series Motor Connected to Different Load Types

4.1.1 Constant load

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]

$$\begin{bmatrix} I_{\underline{o}} e^{\frac{V_{a}^{k}}{a}} + g - g & 0 & 0\\ g & g & 0 & 1\\ 0 & 0 & B & -2M_{af}I_{3}^{k}\\ 0 & 1 & -M_{af}I_{3}^{k} & -R_{a} - M_{af}\omega_{c} \end{bmatrix} \begin{bmatrix} V_{a}^{k+1}\\ V_{b}^{k+1}\\ I_{3}^{k+1} \end{bmatrix} = \begin{bmatrix} I_{PH} + I_{o} + e^{\frac{V_{a}^{k}}{a}} (\frac{V_{a}^{k}}{a} - 1)\\ 0\\ T_{L} - M_{af}(I_{3}^{k})^{2}\\ -M_{af}I_{3}^{k}\omega_{c}^{k} \end{bmatrix}$$

Table (1-a) Parameters of a series motor connected to a constant load

	100 %	90%	80%	70%	60%
V _a ,Volt	154.1195	147,3917	138.064	122.768	80.5671
V_b , Volt	146.7197	140.014	130.6996	115.473	73.418
we, rad/sec	232.0414	220.7005	204.8	178.6588	104.493
I3 Amp.	8.222	8.1893	8.1549	8.098	7,9344
T, N.m	· 4.56	4,52	4.489	4.42	4.24

Table (1-b) Results of a series motor connected to a constant load

	100 %	90%	80%	70%	60%
Peleo Watt	1206.3	1146.57	1065.85	935.1	582.53
Pmech, Watt	1058.1	997.56	919.35	789.67	443
Pmax, Watt	1400	1245	1090.76	937.588	785.97
M %	86.16	92.1	97.71	99.73	74.11
Ĥ%	87.71	87	86.25	84.45	76.05

4.1.2 Ventilator load

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]

$\frac{I_o}{a}e^{\frac{V_a^t}{a}}+g$	-g	0	0	$\begin{bmatrix} V_a^{k+1} \end{bmatrix}$	$\begin{bmatrix} I_{PH} + I_o + I_o e^{\frac{V_a^k}{a}} (\frac{V_a^k}{a} - 1) \end{bmatrix}$	
-g	g	0	1		0	
0	0	$B + b_f c_f (\omega_c^k)^{c_f - 1}$	$-2M_{af}I_3^k$	W _c	$a_f + (b_f(c_f - 1)\omega_c^{c_f}) - M_{af}(I_3^k)^2$	
0	1	$-M_{af}I_3^k$	$-R_a - M_{af}\omega_c$		$-M_{af}I_{3}^{k}\omega_{c}^{k}$	

Table (2-a) Parameters of a series motor connected to a ventilator load

	100 %	90%	80%	70%	60%	\$0%	40%	30%	20%
Va	150.06	143.235	134.37	122.28	105.171	82.456	57.898	36.327	19.694
Vb	141.89	135.266	126.673	114.95	98.422	76.55	53.069	32.674	17.250
D,	199.285	193.982	186.925	176.94	162.04	140.48	114.064	86.674	61.624
13	9.066	8.845	8,549	8,128	7.49	6.56	5.366	4.0551	2.7125
T	5.55	5.28	4.93	4.46	3.76	2.9	1.944	1.109	0.4966

of a series motor connected to	a ventilator load
1	of a series motor connected to

	100 %	90%	80%	70%	60%	50%	40%	30%	20%
Pmax	1400	1245	1090.76	937.59	785.97	636.57	490.3	348.56	213.67
Pelect	1286.3	1196.36	1082.93	934.3	737.18	502,173	284.78	132,49	46.79
Pmech	1106.03	1024.22	921.54	789.15	609.27	407.39	221.74	96.12	30.6
μ%	91.88	96.09	99.28	99.65	93.79	78.88	58.12	38.01	21.9
η%	85.98	85.61	85.09	84.45	82.65	78.88	77,86	72.55	65.38

4.1.3 Centrifugal pump load

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]

Table (3-a) Parameters of a series motor connected to a centrifugal pump load

	100%	.90%	80%	70%	-60%	50%	40%	30%	20%
V_a	148	140	130	117	99	75	48,9	28.6	10.4
V_b	140	132	122	109	91.9	68.9	44.1	25.1	8.03
B ,	194	184	174	158	142	121	88.1	60	11
h _d	57.7	51.6	46.4	38.5	30.9	22.5	11.9	5.5	0.2
I.	9.15	9.05	8.75	8.45	7.8	6.65	5.4	4.01	2.72
T ₅	5.65	5.53	5.16	4.82	4.1	2.98	1.97	1.09	0.5
07	116	120	119	122	115	98.5	89.3	72	189

Table (3-b) Results a	f a series motor connected	d to a centrifugal pun	up load

								A REAL PROPERTY AND A REAL	
	100%	90%	80%	70%	60%	50%	40%	30%	20%
Pmax	1400	1245	1090.7	937.6	785.97	636.57	490.3	348.56	213.67
Pelea	1281	1195	1067	921	717	458.2	238	100.4	21.7
Prech	1096	1017	897.8	761.6	582.2	360.6	173.6	65.4	5.5
Phyd	602.8	560	493.8	418.9	320.2	198	95.5	36	3
μ%	91.5	96	97.9	98.3	91.2	72	48.5	28.8	10
η%	85.5	92.3	84.1	82.7	81.2	78.7	72,9	65	25.3

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Fig. 4 I-V Characteristics for a series motor connected to different load types

Fig. 5 Utilization curves for a series motor connected to different load types

4.2 A Separately Excited Motor Connected to Different Load Types

4.2.1 Constant load

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]

$$\begin{bmatrix} I_o & \frac{V_o^k}{a} & g & -g & 0 & 0 \\ -g & g & 0 & 1 \\ 0 & 0 & B & -c_e \\ 0 & 1 & -c_e & -R_a \end{bmatrix} \begin{bmatrix} V_a^{k+1} \\ V_b^{k+1} \\ \omega_c^{k+1} \\ I_3^{k+1} \end{bmatrix} = \begin{bmatrix} I_{PH} + I_o + e^{\frac{V_a^k}{a}} & \frac{V_a^k}{a} - 1 \\ 0 \\ T_L \\ 0 \end{bmatrix}$$

Table (4-a) Parameters of a separately excited motor connected to a constant load

	100 %	90%	80%	70%	60%
V _a	157.7831	152.1904	144.9222	134.5736	116.7616
Vb	151.1982	145.6363	138.408	128.1163	110.4022
ω,	225.8203	216.9462	205.4135	188.976	160.7305
I,	7.3092	7.2821	7.2308	7.1748	7.059
Ť	4.539	4.5222	4.4903	4.4555	4.3836

Table (4-b) Results of a separately excited motor connected to a constant load

100 %	90%	120%	200/	1001
	the second se	1070	10%	00%
1400	1245	1090.76	937.588	785.97
1105.13	1060.5	1000.8	918.59	779.33
1025	981.07	922.37	841.98	704.57
78.93	85.18	91.75	97.97	99.155
92.75	92.51	92.16	89.8	90.4
	1400 1105.13 1025 78.93 92.75	1400 1245 1105.13 1060.5 1025 981.07 78.93 85.18 92.75 92.51	1400 1243 1090.76 1105.13 1060.5 1000.8 1025 981.07 922.37 78.93 85.18 91.75 92.75 92.51 92.16	1400 1245 1090.76 937.588 1105.13 1060.5 1000.8 918.59 1025 981.07 922.37 841.98 78.93 85.18 91.75 97.97 92.75 92.51 92.16 89.8

4.2.2 Ventilator load

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]:

$$\begin{bmatrix} \frac{I_{a}}{a}e^{\frac{v_{a}^{k}}{a}} + g & -g & 0 & 0\\ -g & g & 0 & 1\\ 0 & 0 & B + b_{f}c_{f}(\omega_{c}^{k})^{c_{f}-1} & -c_{e}\\ 0 & 1 & -c_{e} & -R_{o} \end{bmatrix} \begin{bmatrix} \mathbf{V}_{a}^{k+1}\\ \mathbf{V}_{b}^{k+1}\\ \mathbf{W}_{c}^{k+1}\\ I_{3}^{k+1} \end{bmatrix} = \begin{bmatrix} I_{pH} + I_{o} + I_{o}e^{\frac{v_{a}^{k}}{a}}(\frac{V_{a}^{k}}{a} - 1)\\ 0\\ a_{f} + (b_{f}(c_{f} - 1)\omega_{c}^{c_{f}})\\ 0 \end{bmatrix}$$

Table (5-a) Parameters of a sep. excited motor connected to a ventilator load

	100 %	90%	- 80%	70%	-60%	50%	40%	30%	-20%	10%
Va	148.819	143.675	137.717	130.74	122.5	112.703	101.025	87.106	70.429	49.835
Vo	140.443	135.765	130.336	123.966	116.415	107.411	96.628	83.707	68.111	48.662
O,	203.697	197.415	190.092	181.455	171.157	158.772	143.819	125.68	103,465	75.212
I_{j}	9,298	8.780	8.193	7.522	6.852	5.874	4.883	3.776	2.5729	1.303
T	5.774	5.4526	5.088	4.671	4,255	3.647	3.033	2.345	1.5977	0.809

Table (5-b) Results of a separately excited motor connected to a ventilator load

	100 %	90%	80%	70%	60%	50%	40%	30%	20%	10%
Pmax	1400	1245	1090.76	937.588	785.97	636.57	490.3	348,56	213.67	90.3
Pelect	1305.82	1192.07	1067.82	932,433	797.67	630.89	471.88	316.08	175.24	63.25
Pmech	1176.15	1076.42	967.13	847.57	728.27	579.04	436.146	294.7	165.3	60.85
μ%	93.27	95,75	97.9	99.45	101.49	99.1	96.24	90.68	82.2	70
H%	90.07	90.3	90.57	90.9	91.3	91.78	92.42	93.23	94.32	95.2

4.2.3 Centrifugal pump Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]

$$\begin{bmatrix} I_{ph} - I_0 e^{V_a^k I_a} (1 - \frac{V_o^k}{a}) + I_0 \\ 0 \\ - \frac{\eta \omega_c^k \tau_s^k}{\rho g h_d^k} \\ \omega_{ref} \sqrt{\frac{h_d^k}{a_{st}}} - \frac{\omega_{ref} h_d^k}{2\sqrt{a_{st} * h_d^k}} \end{bmatrix}$$

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Table (6-a) Parameters of a sep. excited motor connected to a centrifugal pump load

	100%	90%	80%	70%	60%	50%	40%	30%	20%	10%
V_q	146	138	132	122	114	104	90.6	73.5	52,4	16.2
V_{b}	137	130	124	115	108	98	86	70	50	15
ω	197	186	178	166	157	143	126	103	74.2	21
h_d	59.2	53.3	48.8	42	37.6	31.3	24.4	16.4	8.43	0.67
13	9.9	9.4	8.8	8.1	7.15	6.1	5.1	3.87	2.62	1.34
T ₅	6.14	5.83	5.46	5.03	4.44	3.8	3.17	2.4	1.62	0.83
Q_7	124	125	121	121	113	106	100	93	87.7	159

Table (6-b) Results of a separately excited motor connected to a centrifugal pump load

	100%	90%	80%	70%	60%	50%	40%	30%	20%	10%
P _{max}	1400	1245	1090.7	937.58	785.97	636.57	490.3	348.56	213.67	90.3
Pelect	1356	1222	1089	931.5	772.2	543.4	438.6	271	131	20.1
Pmech	1209.6	1084.4	971.88	835	697	372.4	272.6	247.2	120.2	17.43
М %	665.28	542.2	534.34	459.25	383.35	204.8	150.1	135.99	66.11	10.5
Н%	86.35	98.15	99.1	99.35	98.25	85.63	89.45	77.75	61.3	22.26



Fig.6 I-V Characteristics for a sep. excited motor connected to different load types



Fig.7 Utilization curves for a sep. excited motor connected to different load types

4.3. A Shunt Motor Connected to Different Load Types

4.3.1 Constant load

-

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]

$$\begin{bmatrix} \frac{I_{a}}{a}e^{\frac{V_{a}^{k}}{a}} + g - g & 0 & 0 \\ g & g & 0 & 1 \\ 0 & 0 & B + \frac{M_{gf}R_{a}I_{3}^{2}}{(R_{a} + R_{f} - M_{qf}\omega_{4})^{2}} & \frac{2M_{qf}R_{a}I_{3}(R_{f} - M_{qf}\omega_{4})}{(R_{a} + R_{f} - M_{qf}\omega_{4})^{2}} \end{bmatrix}^{k+1} = \\ \begin{bmatrix} V_{a}^{k+1} \\ V_{b}^{k-1} \\ W_{b}^{k+1} \\ R_{c}^{k+1} \\ R_{f}^{k+1} \end{bmatrix} = \\ \begin{bmatrix} I_{PH} + I_{a} + e^{\frac{V_{a}^{k}}{a}} (\frac{V_{a}^{k}}{a} - 1) \\ 0 \\ T_{L} - \frac{M_{qf}R_{f}R_{a}I_{3}}{(R_{a} + R_{f} - M_{qf}\omega_{4})^{2}} \\ - \frac{R_{f}R_{a}I_{3}\omega_{4}}{(R_{a} + R_{f} - M_{qf}\omega_{4})^{2}} \end{bmatrix}$$

'n

For the shunt motor connected to constant load torque the motor does not produce sufficient torque to start the system even for the full insolation

4.3.2 Ventilator load

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]

$$\begin{bmatrix} \frac{I_{a}}{a} e^{\frac{y_{a}^{*}}{a}} + g - g & 0 & 0 \\ g & g & 0 & 1 \\ 0 & 0 & B + \frac{M_{af}R_{a}I_{3}^{2}}{(R_{a} + R_{f} - M_{af}\omega_{a})^{2}} + b_{f}c_{f}(\omega_{c}^{*})^{c_{f}-1} & \frac{2M_{af}R_{a}I_{3}(R_{f} - M_{af}\omega_{a})}{(R_{a} + R_{f} - M_{af}\omega_{a})^{2}} & -\frac{R_{f}R_{a}}{(R_{a} + R_{f} - M_{af}\omega_{a})^{2}} \\ 0 & 1 & -\frac{R_{f}R_{a}I_{3}}{(R_{a} + R_{f} - M_{af}\omega_{a})^{2}} & -\frac{R_{f}R_{a}}{(R_{a} + R_{f} - M_{af}\omega_{a})} \end{bmatrix} = \\ \begin{bmatrix} I_{PH} + I_{a} + e^{\frac{y_{a}^{*}}{a}} (\frac{y_{a}^{*}}{a} - 1) \\ 0 \\ R_{f} - \frac{M_{af}R_{a}R_{f}I_{3}}{(R_{a} + R_{f} - M_{af}\omega_{a})^{2}} + (b_{f}(c_{f} - 1)\omega_{c}^{c_{f}}) \\ -\frac{R_{f}R_{a}I_{3}\omega_{a}}{(R_{a} + R_{f} - M_{af}\omega_{a})^{2}} \end{bmatrix}$$

Table (7-a) Parameters of a shunt motor connected to a ventilator load

	-100 %	- 90%	80%	70%	60%
Va	163.7	156.9	37.2	31	25.77
ν_b	157	150	27.5	22.5	18.5
0,	181.3	180.1	81.78	73.36	68.5
$\overline{I_3}$	7.4	7.7	10.75	9.45	8.08
T	5.64	5.506	1.507	1.085	0.763

Table (7-b) Results of a shunt motor connected to a ventilator load

	100 %		80%	70%	60%
Pmax	1400	1245	1090.76	937.6	785.97
Pelect	1160	1155	295.6	212.6	149.48
Pmech	1023.3	992.3	123.3	79.6	52.3
M %	96.5	85.9	27.1	22.7	18.5
Н%	88.2	86	41.7	37.41	35

4.3.3 Centrifugal pump

Newton Raphson Mixed Nodal Tableau [NR MNT] & [NR R]



	100%	90%	80%	70%	60%
V.	162.7	154.9	38.2	32.24	25.77
Vb	157	150	27.5	22.5	18.5
ω	181.3	180.1	81.78	73.36	68.5
ha	67.7	53	46.4	38.5	30.9
13	7.6	7.8	10.35	9.4	8.08
T_{5}	5.84	5.65	1.67	1.01	0.763
07	110	121	102	118	121

Table (8-b) Results of	fa shunt motor	connected to	a centrifugal p	ump load
	100%	90%	80%	70%	60%
Pmax	1400	1245	1090.76	937.6%	785.97
Pelect	1158	1145	292.6	210.6	149.48
Pmech	1020.3	991.3	122.3	81.6	52.3
Phyd	590	545.215	71.1	47.14	26.15
μ%	96.1	83.9	25.1	21.7	18.5
η%	87.2	85.8	41.4	37.21	35





Fig.8 I-V characteristics of a shunt motor connected to different load types



4-4 COMPARISON BETWEEN CASE STUDIES

A comparison between the nine case studies is presented in Table 9 and it shows that:

- The separately excited motor is the appropriate type for a different mechanical load types. Its efficiency and matching quality are better than other motors.
- Separately excited motor coupled to a ventilator load type is found to be the most suitable combination for SCA generator. The utilization of SCA output energy is 96.07% of its maximum output power.
- It is not preferable to use shunt motors with constant mechanical loads. However, the SCA generator can produce sufficient torque to start up the shunt motor to

supply both ventilator and centrifugal pump loads (at 59.6%, and 59% of insolation level respectively).

Motor type	Start up insolation level	Matching quality	efficiency
Series motor	57.94%	62,73%	89.96%
Separately motor	49.68%	65.84%	92.05%
Shunt motor			

Table_9-a Constant load

Table 9-b Ventilator load

Motor type	Start up insolation level	Matching quality	Efficiency
Series motor	19.99%	83.84%	84.17%
Separately motor	5.9%	96.07%	92%
Shunt Motor	59.6%	32,25%	· 81%

Table 9-c_Centrifugal pump

Motor Type	Start up insolation level	Matching quality	Efficiency
Series motor	20%	81.73%	82.75%
Separately motor	6%	93,5%	90.7%
Shunt Motor	59%	29.66%	81.08%

5- CONCLUSION

- The systematic mathematical methodology known as Graph Theoretic Modeling (GTM) was presented in details.
- The GTM technique has been applied to PVPS composed of different dc-motor types (series, separately excited and shunt motors) connected to different load types (constant, ventilator and pump loads) supplied by a SCA generator.
- A computer program using MATLAB 6 was developed to numerically solve the system matrix equations.
- The quality of load matching for each case was investigated as a measure of performance and system utilization efficiency.
- A comparison between different case studies was introduced to indicate the appropriate motor type for each load.
- Applying the GTM technique to PV systems results in many advantages:
 - GTM methodology is global and flexible enough to include linear or nonlinear components and replace them with a stamp.
 - □ GTM analyzes electrical and mechanical characteristics for combined PV-dc motor in addition to hydraulic characteristics in case of centrifugal pump.
 - GTM technique is a general integral promising methodology capable of providing PVPS with ready simulated stamps for any component.
 - GTM technique as a mathematical methodology can be used as a measure of matching quality, which reflect the performance of the system and exhibit the appropriate load connected to a dc motor powered by SCA generator.

• The paper presents a method for modeling SCA generator, different types of dc-motors and various mechanical loads. It provides an evaluation for any motor type connected to a mechanical load powered by a stand-alone PV power system.

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APPENDIX

Parameter Values

Component	Symbol	Nomenclature	Volua
Component	L	Reverse Saturation current	
	<u>40</u> I.	Cell photocurrent	0.756 A
	P P	Cell series resistance	0.05 ohm
PV Cell	<u>с</u>	Thermal voltage $(A = KT/c)$	1/13 68 1/Volt
17.00	v .	Betzman constant	1713.00 1740.0
	<u>T</u>	Absolute temperature	200 Kaluin
	1	Flectron charge	1.6 e ⁻¹⁹ coulomb
	<u>-</u>	Terminal valtage	1.0 e coulomo
	V	A motum cumpat	0.2 A (mtod)
	<u>la</u>	Sheet around	9.2 A (rateu)
Output Motor Data	ω		157.1 rad/sec
		Electromagnetic torque	5.7 N.m
	Α	Toque constant of rotational losses	0.2 N.m
	В	Viscous Torque constant of rotational losses	2.387e ⁻³ N.m /rad/s
Sarias Motor	R _a	Combined field and armature resistance	2.2 ohm
Series Motor	M _{af}	Mutual inductance between field and armature	6.75e ⁻² H
San Frailed Motor	R _e	Armature resistance	1.5 ohm
Sep. Exciled Motor	C,	Flux coefficient	0.621 V/rad/sec
	Mai	Mutual inductance between field and armature	0.518 H
Shunt Motor	R _a	Armature resistance	1.5 ohm
	R _f	Field resistance	100 ohm
Constant Load	T	Load torque	4.0 N.m
	a _f	Static torque constant	$3.0 e^{-1} N.m$
Ventilator Load	b _f	Dynamic torque constant	3.9 e
	G	C factor	1.8
	H	Rated head. m	37.795
	Q	Rated flow charge, liter/min	80
Centrifugal	η	Pump efficiency, %	55
Pump	ρ	Fluid Density, KG/m3	1000
-	g	Gravitational constant	9.8
	ast	Static a factor	37.795